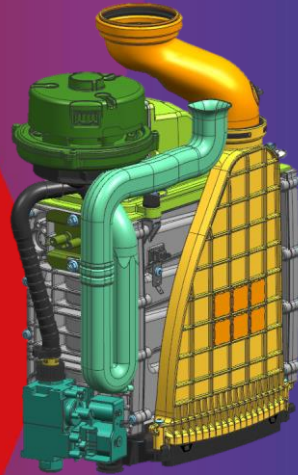
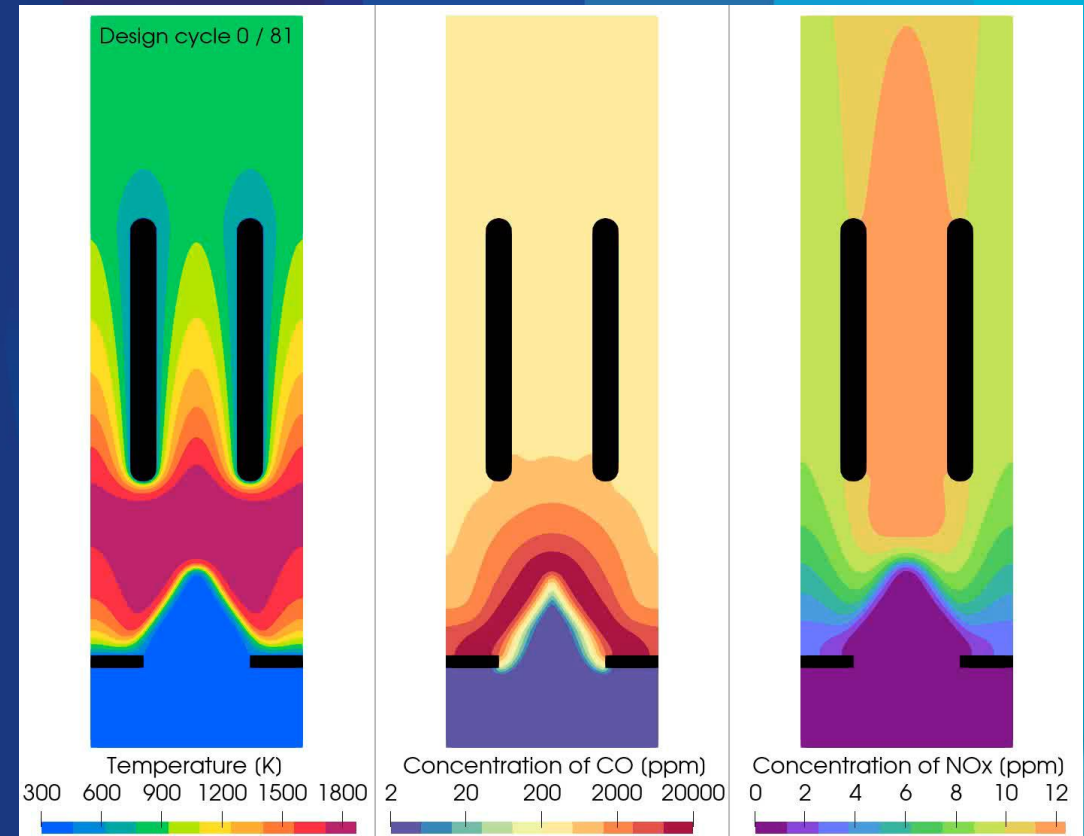


AUTOMATIC DESIGN OPTIMIZATION FOR HYDROGEN BOILERS



Nijso Beishuizen Bosch Thermotechnology Deventer, NL
Eindhoven University of Technology, NL

with major contributions from:
Daniel Mayer - Bosch Research and Technology Center, Sunnyvale, USA



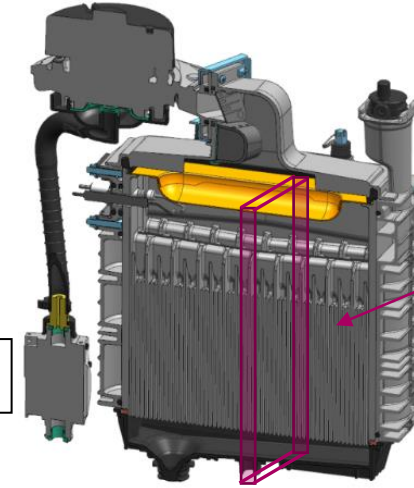
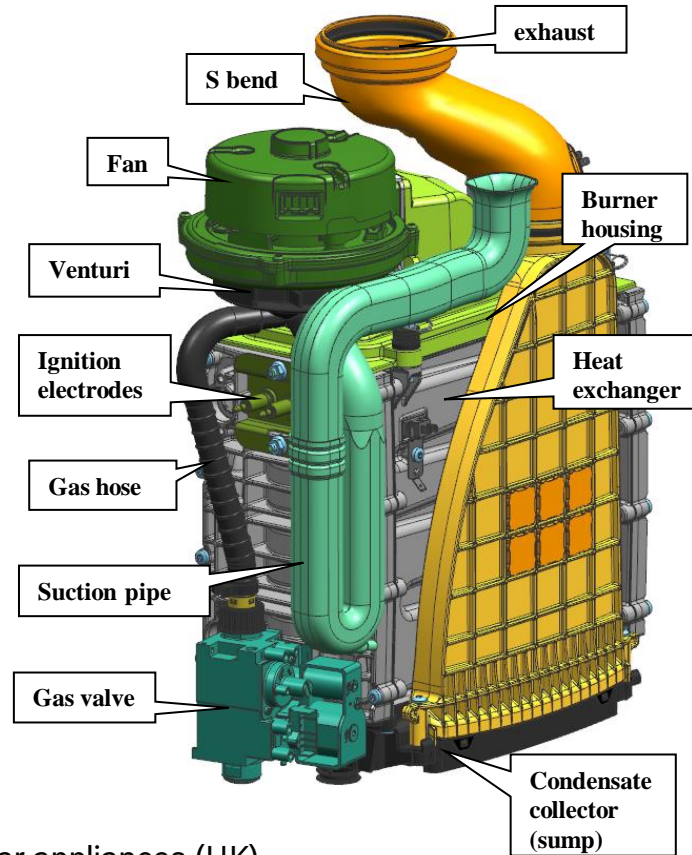
H₂ IN THE BUILT ENVIRONMENT

H₂ VS. NATURAL GAS

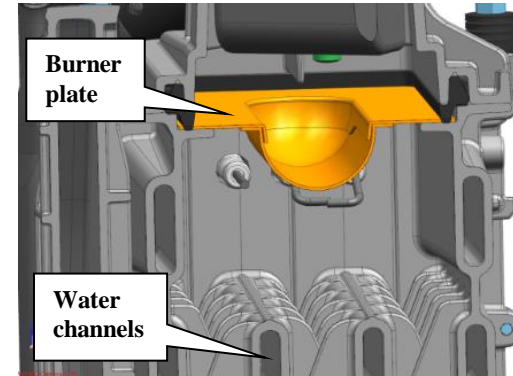
MODELLING H₂

ADJOINT DESIGN OPTIMIZATION

Introduction – domestic boilers



A slice of the heat exchanger is simulated to assess performance and improve design

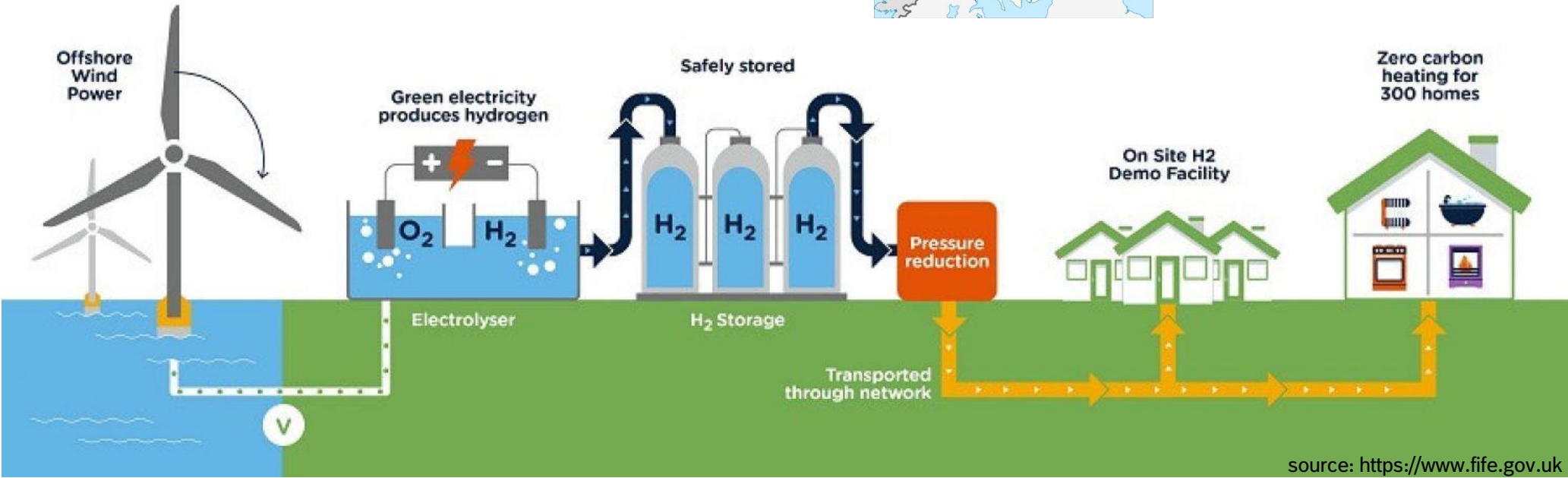


- WB7 Heat exchanger (7-37 kW)
- Used in Trendline (NL) and Greenstar appliances (UK)

H₂ in the built environment



county of Fife



source: <https://www.fife.gov.uk>

H₂ in the built environment



Full direct electrification of heating not feasible

Would require significant increase in power generation and grid capacity that is used only in the winter



Compatible with existing building stock compared to use of heat pumps

90% of all buildings emissions result from buildings older than 25 years



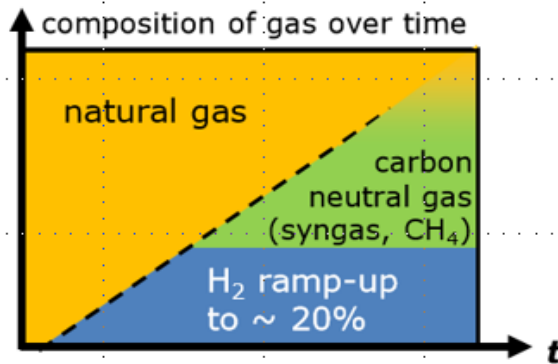
Infrastructure, skills and regulations already available and ready to be leveraged

40% of all European households have gas heating as of today making fast and convenient implementation possible

H₂ in the built environment

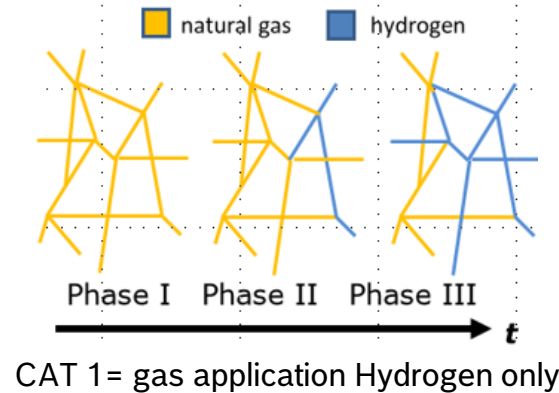
Scenario A: blending

- Use existing gas grid and make it suitable for H₂NG blends
- Increase share of syngas and biomethane + Hydrogen
- Use existing combustion technology and validate it against new gas quality spec.



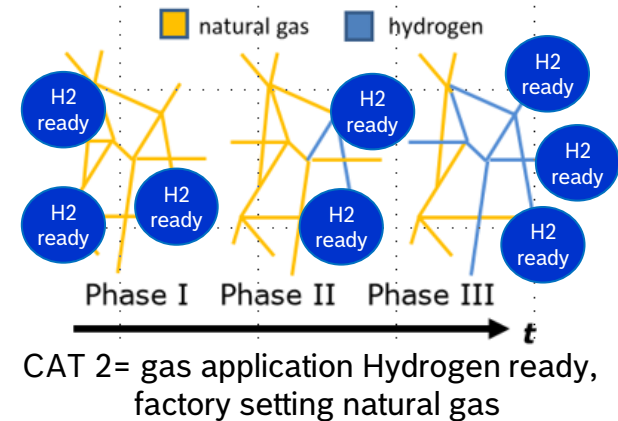
Scenario B: H₂-islands

- Successive upgrade of existing gas grid sections to closed local hydrogen nets.
- Increase islands step by step
- Boundary: H₂ supply & CAT 1 product installation at the same time



Scenario C: H₂-ready products

- Gas applications are designed for pure hydrogen combustion, but installed in natural gas setting: CAT 2 application
- Gas grid is upgraded step by step, installed stock is prepared



There are 3 scenarios to use hydrogen in the heating market to reduce CO₂ emissions.

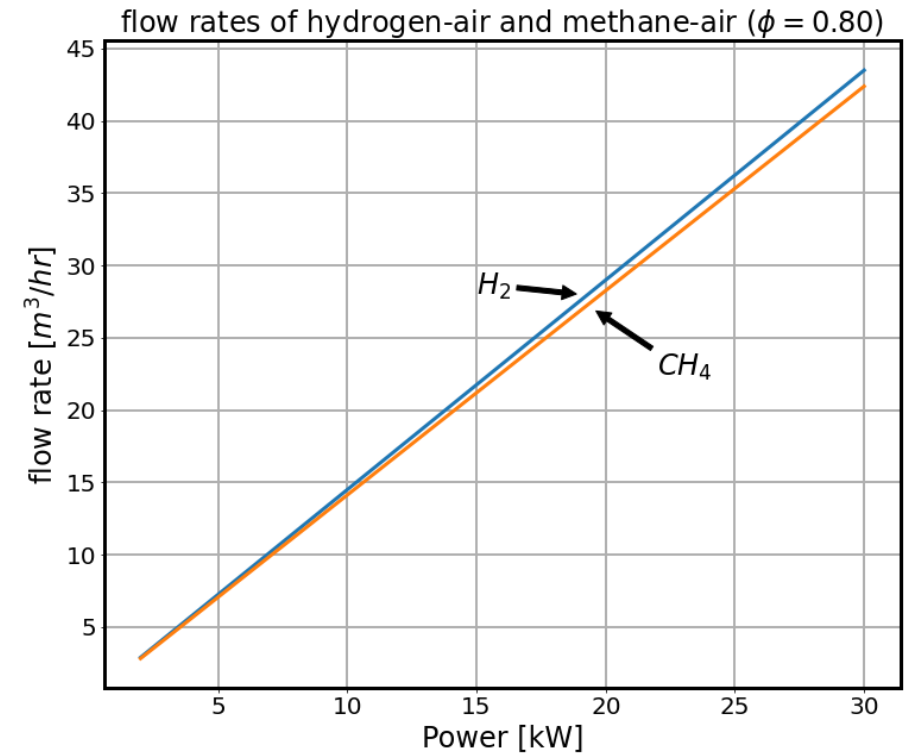
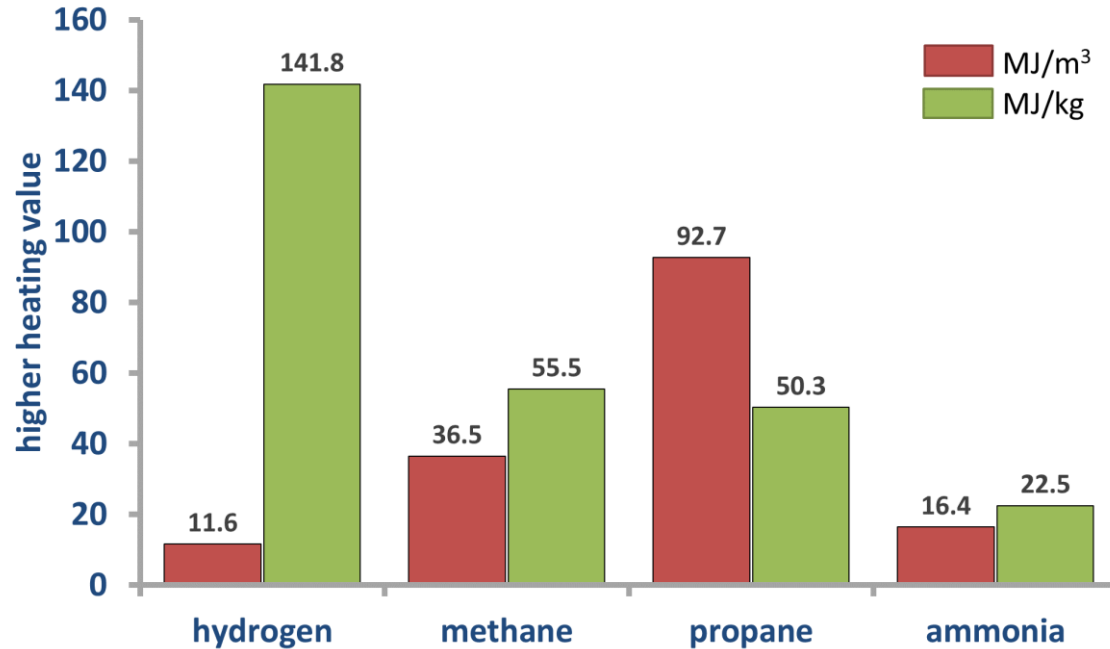
H₂ IN THE BUILT ENVIRONMENT

H₂ VS. METHANE

MODELLING H₂

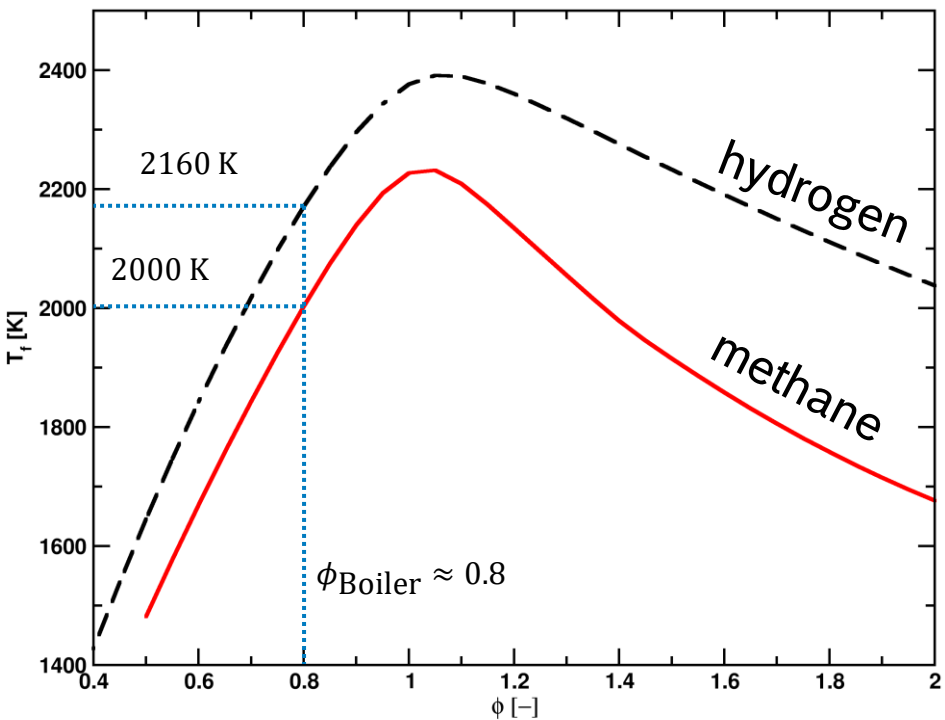
ADJOINT DESIGN OPTIMIZATION

Hydrogen vs. methane

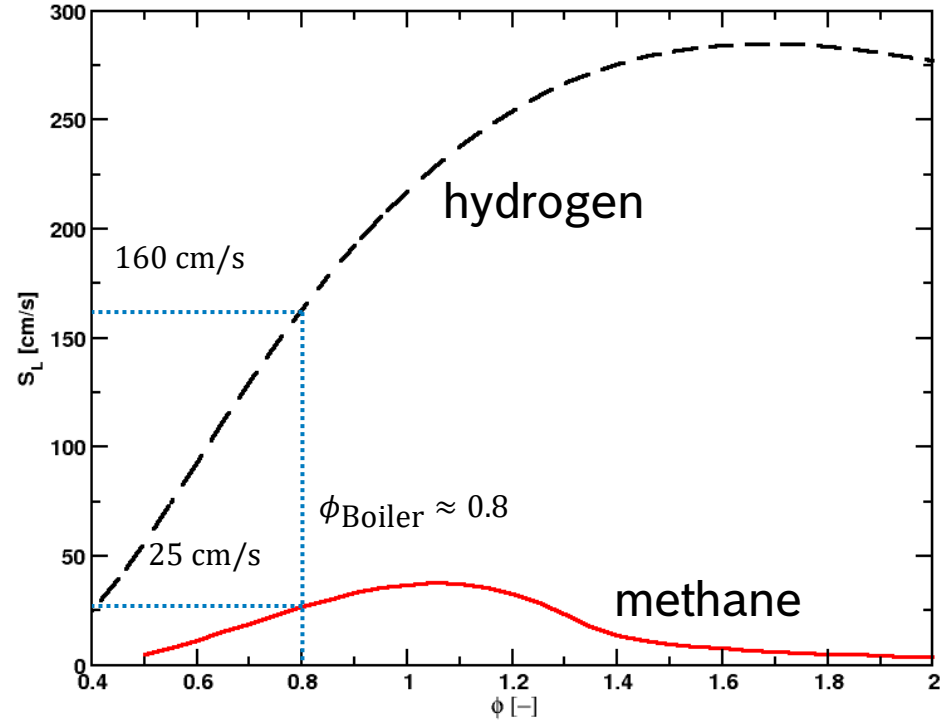


Hydrogen vs. methane

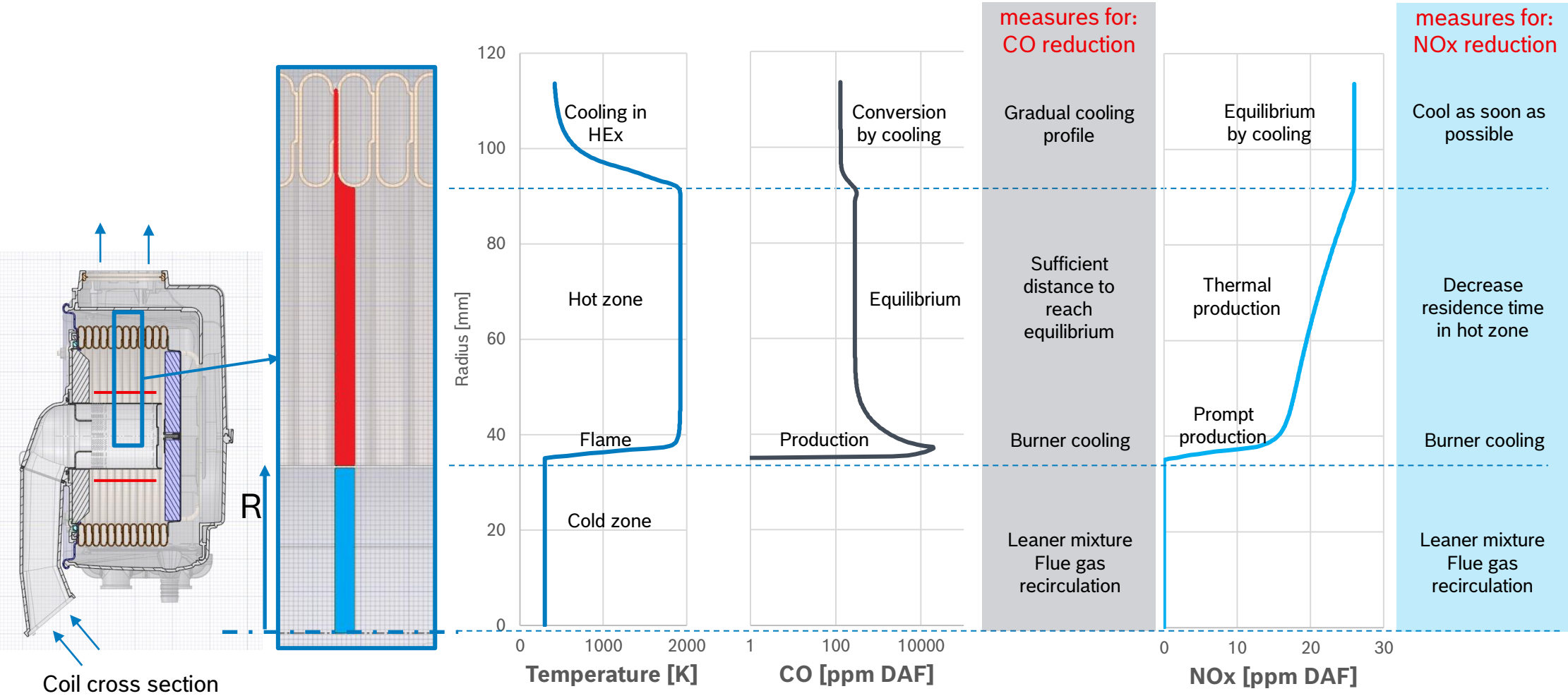
Flame temperature



Flame speed

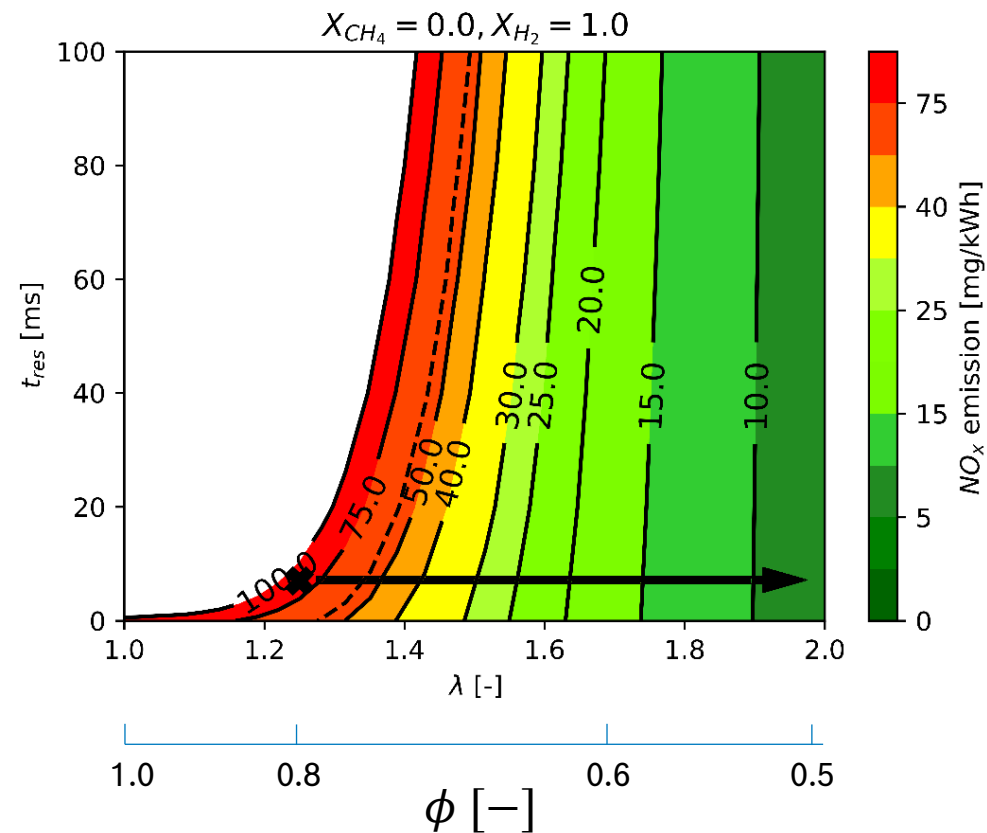
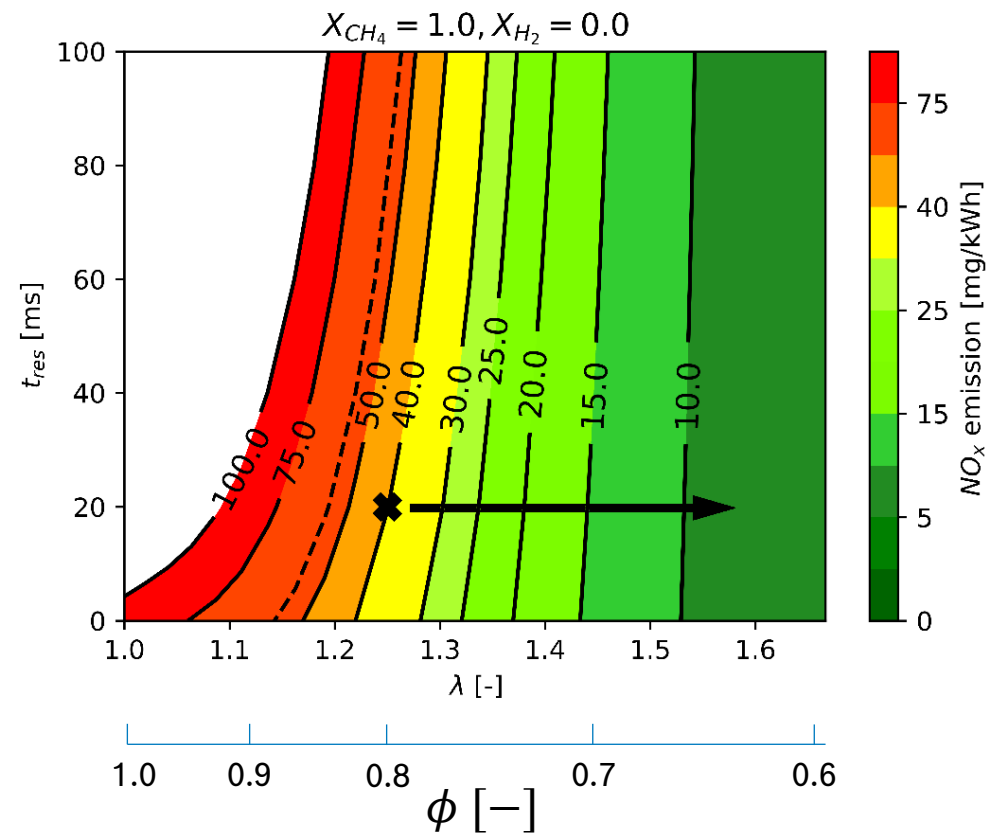


Hydrogen vs. methane - emissions



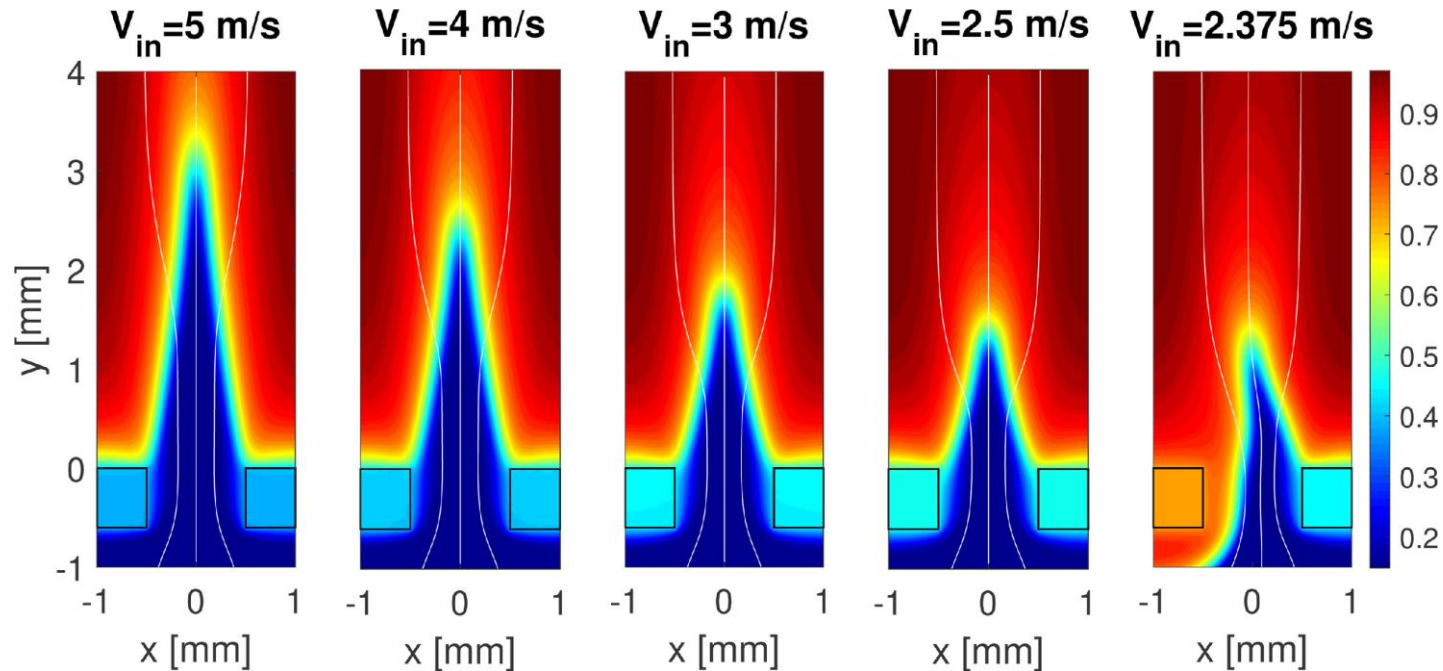
Hydrogen vs. methane

NO_x emissions



Hydrogen vs. methane

Hydrogen flash back



Vance et al. *Combust. flame* (2022)

For more on hydrogen flash-back, see the presentation of Sikke Klein

H₂ IN THE BUILT ENVIRONMENT

H₂ VS. NATURAL GAS

MODELLING H₂

ADJOINT DESIGN OPTIMIZATION

Modelling H₂

For combustion simulations we need the chemical reactions

One step reaction: $\text{H}_2 + \frac{1}{2} \text{O}_2 \rightarrow \text{H}_2\text{O}$

But: Detailed description of hydrogen-air combustion consists of many reactions involving many species being produced during the reaction, e.g. The mechanism from Galway:

44 SPECIES: AR N2 HE H2 H O2 O H2O OH OHV H2O2 HO2 CO CO2 HOCO CH4 CH3 OCHO C2H6 N NO
NOV NO2 N2O NH3 HNO HON HONO H2NO NNH NH2 NH HNOH NO3 HONO2 HNO3 N2H2
N2H3 N2H4 H2NN NH2OH HNO2 N2O4 N2O3

► 251 reactions:



► ...



Modelling H₂

Detailed chemistry simulations

Conservation equations:

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{u}) = 0,$$

$$\frac{\partial(\rho \mathbf{u})}{\partial t} + \nabla \cdot (\rho \mathbf{u} \otimes \mathbf{u}) + \nabla p - \nabla \cdot \boldsymbol{\tau} = 0,$$

Species transport

$$\frac{\partial(\rho Y_i)}{\partial t} + \nabla \cdot (\rho \mathbf{u} Y_i) + \nabla \cdot (\rho \mathbf{V}_i Y_i) = \dot{\omega}_i,$$

$$\frac{\partial(\rho c_p T)}{\partial t} + \nabla \cdot (\rho \mathbf{u} c_p T) - \nabla \cdot (\lambda \nabla T) + \rho \nabla T \cdot \sum_{i=1}^n c_{p,i} Y_i \mathbf{V}_i = \dot{\omega}_T$$

Coupled system:

$$\dot{\omega}_i = W_i \sum_{r=1}^{n_r} \nu_{i,r} K_r \prod_{j=1}^{n_{sp}} \left(\frac{\rho Y_j}{W_j} \right)^{\nu'_{j,r}}$$

difficulty:

- large number of equations
- stiffness of equations
- small mesh size (thin reaction zones)

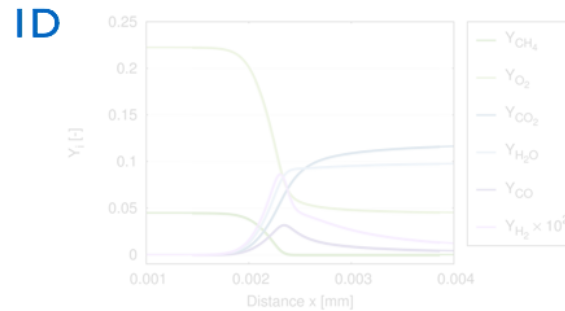
high computational cost

Modelling H₂

Combustion modeling: The flamelet approach

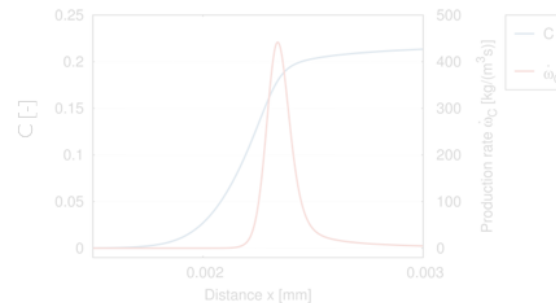
Idea: Map detailed 1D simulation results in 3D space using problem specific parameters:
here: **progress variable C** and **enthalpy h**

- Compute 1D simulations
- Tabulate 1D solutions as functions of progress variable C and enthalpy h
- Solve 3D transport equations for C and h using table look-ups to obtain values for source terms and physical quantities



$$C = Y_{\text{CO}_2} + Y_{\text{H}_2\text{O}}$$

$$\dot{\omega}_C = \dot{\omega}_{\text{CO}_2} + \dot{\omega}_{\text{H}_2\text{O}}$$



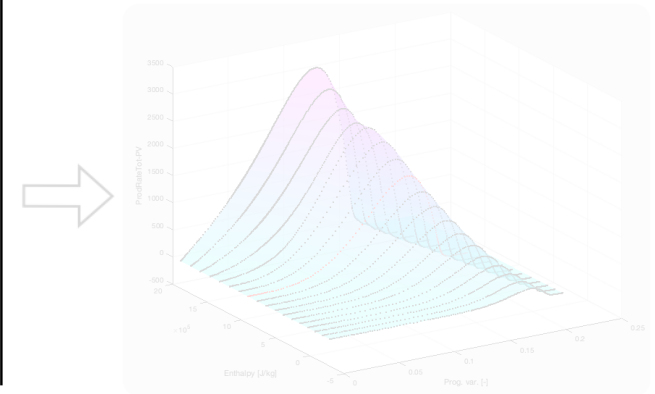
3D

$$\frac{\partial(\rho C)}{\partial t} + \vec{\nabla} \cdot (\rho \vec{v} C) - \vec{\nabla} \cdot (\rho D_C \vec{\nabla} C) = \rho \dot{\omega}_C$$

$$\frac{\partial(\rho h)}{\partial t} + \vec{\nabla} \cdot (\rho \vec{v} h) - \vec{\nabla} \cdot (\rho D_h \vec{\nabla} h) = \rho \dot{\omega}_h$$

$C, \text{ Enthalpy } (h)$ ↓

↑ $\dot{\omega}(C, h)$
 $\nu(C, h)$
 $\rho(C, h)$
 $D(C, h)$
...



Modelling H₂

Emission models

Accuracy of Y_{CO} and Y_{NO} in the lookup table can be low for strong cooling.

➔ Transport equations for Y_{CO} and Y_{NO} with source term correction^[2]

Consider generic reaction equation for emission consumption:

Reaction # c : $EM + B \rightarrow C + D$, with $EM = \{CO, NO\}$

$$\dot{\omega}_{EM} = W_{EM} \sum_{r=1}^{n_r} v_{EM,r} K_r \prod_{j=1}^{n_{sp}} \left(\frac{\rho Y_j}{W_j} \right)^{v'_{j,r}} = \underbrace{W_{EM} \sum_{r=1, r \neq c}^{n_r} v_{EM,r} K_r \prod_{j=1}^{n_{sp}} \left(\frac{\rho Y_j}{W_j} \right)^{v'_{j,r}}}_{\dot{\omega}_{EM}^+} + \underbrace{W_{EM} K_c \rho^2 \frac{Y_{EM}}{W_{EM}} \frac{Y_B}{W_B}}_{\dot{\omega}_{EM}^-}$$

$$\dot{\omega}_{EM}^{3D} = \boxed{\dot{\omega}_{EM}^{+,1D}} + \boxed{\frac{\dot{\omega}_{EM}^{-,1D}}{Y_{EM}^{1D}}} \boxed{Y_{EM}^{3D}}$$

Stored in chemistry table

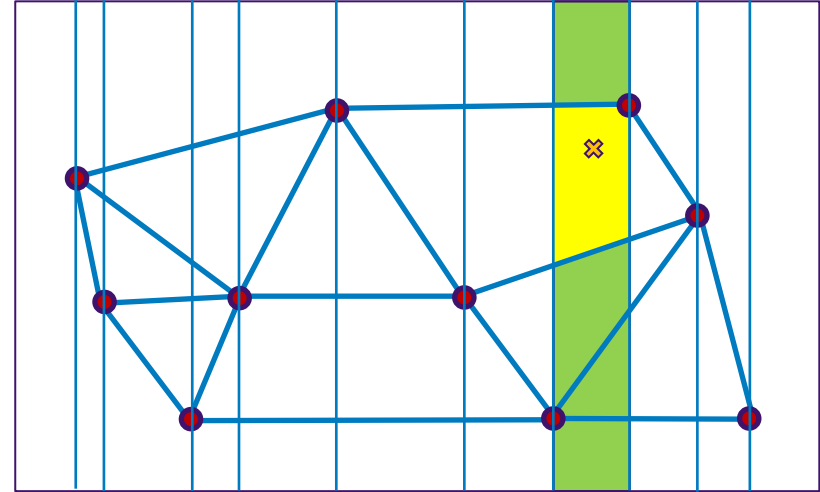
Solved using transport equation

[2]: M. Ihme, H. Pitsch, Physics of Fluids 20, 055110 (2008)

Modelling H_2

tabulation: slab approach

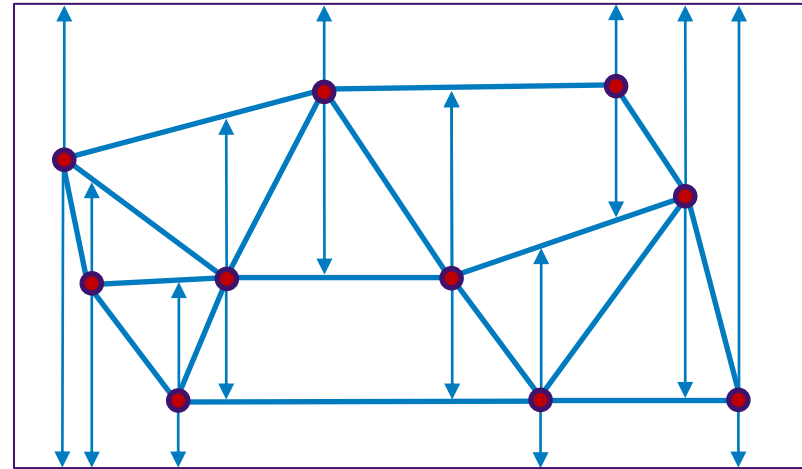
- ▶ We need point location in a table
- ▶ We want to be smarter than loop over all cells and check if the point is inside
- ▶ first idea: partition into vertical slabs
 - ▶ find correct slab (binary search over the slabs)
 - ▶ loop over the segments inside the slab to determine point location (also binary search)
 - ▶ time to find cell: $O(\log(n))$
 - ▶ memory requirement: worst case $O(n^2)$



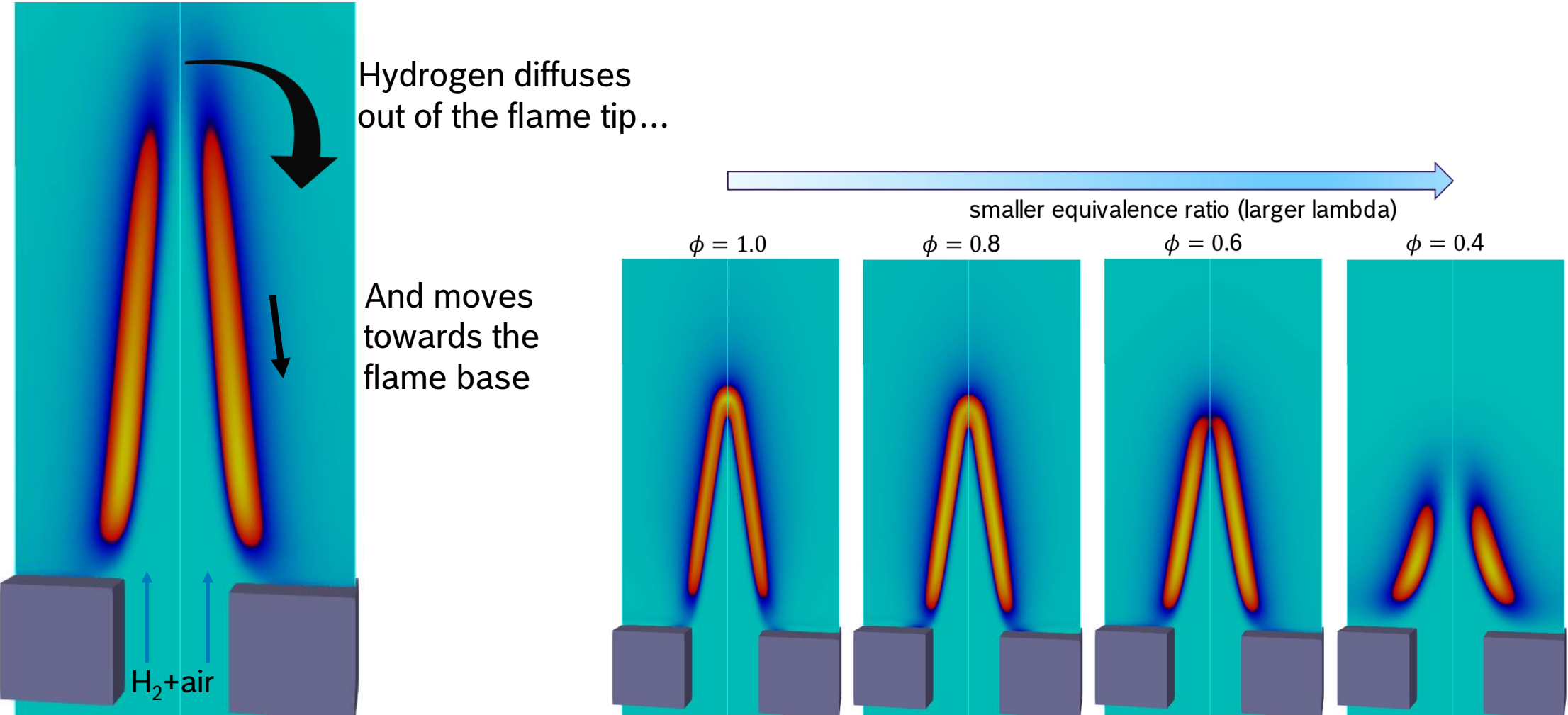
Modelling H_2

smarter tabulation: trapezoidal map

- ▶ divide into trapezoids:
 - ▶ from each node, create a vertical edge up and down until you hit an edge
 - ▶ results in trapezoids or triangles (degenerate trapezoid)
 - ▶ Data stored in Directed Acyclic Graphs (DAG)
 - ▶ time to find cell: $O(\log(n))$
 - ▶ lower cell count
 - ▶ memory requirement: worst case $O(n)$
 - ▶ Points inside a cell: interpolation using barycentric coordinates
 - ▶ Points outside the mesh: projected onto the convex hull



Modelling H₂ – preferential diffusion



Modelling H₂ - preferential diffusion

$$\frac{\partial \rho Y_k}{\partial t} + \frac{\partial}{\partial x_i} (\rho (u_i + \boxed{V_{k,i}}) Y_k) = \dot{\omega}_k, \quad k = 1, \dots, N$$

diffusion velocity

Fick's law of binary diffusion:

$$Y_1 \bar{V}_1 = -D_{12} \nabla_x Y_1$$

binary diffusion of species 1
into species 2

Stefan-Maxwell equation:

$$\nabla_x X_i = \sum_{j=1}^N \frac{X_i X_j}{D_{ij}} (\bar{V}_j - \bar{V}_i), \quad i = 1..N$$

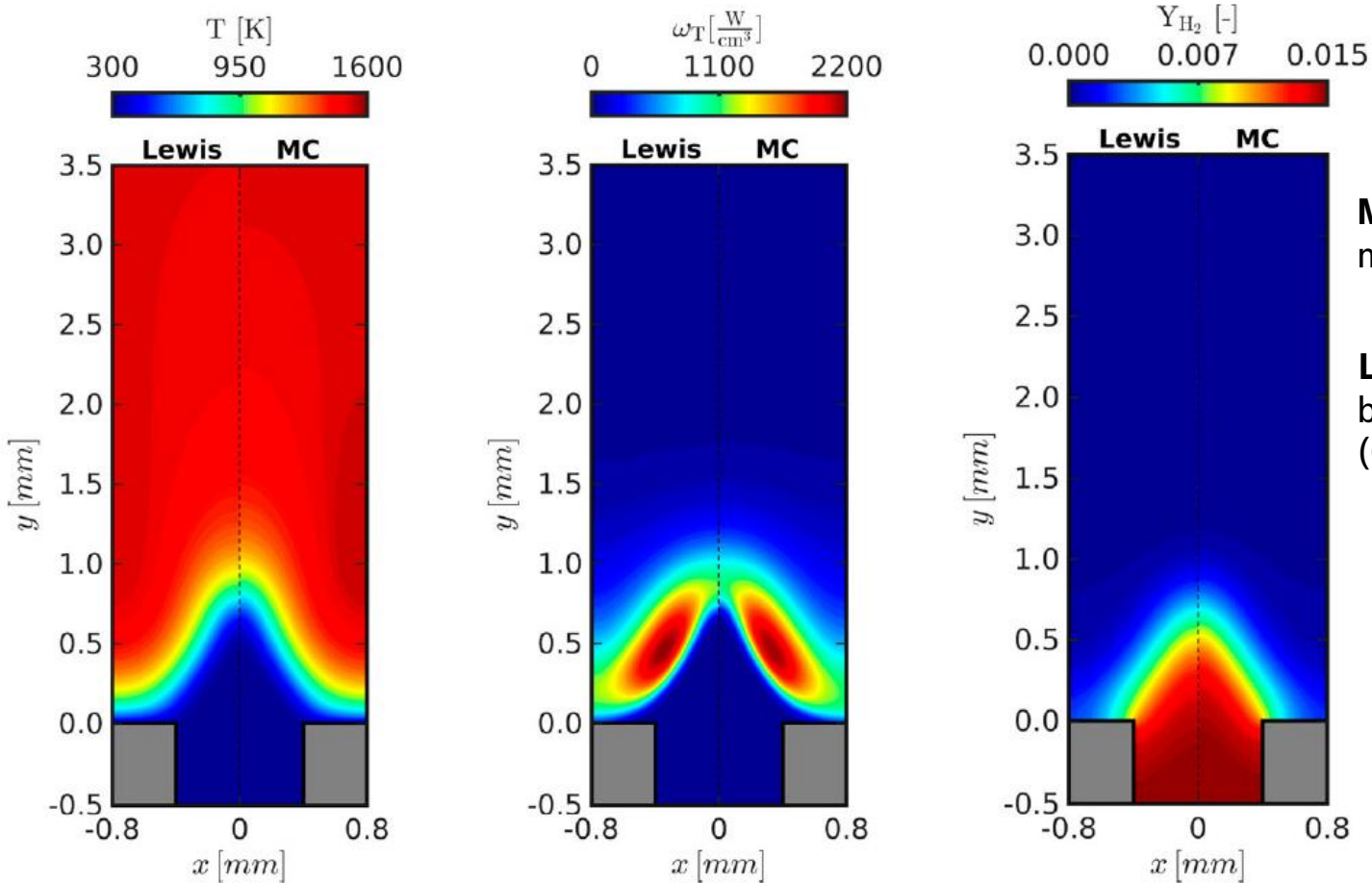
$$X_k = \frac{W}{W_k} Y_k$$

binary diffusion of species i
into species j

first order approximation:
Curtiss- Hirschfelder

$$X_k \bar{V}_k = -D_k \nabla_x Y_k$$

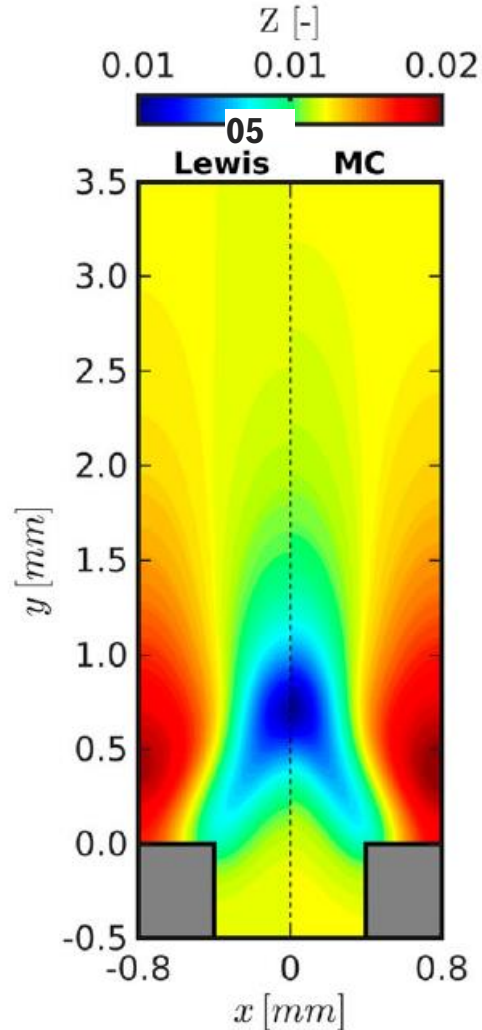
Modelling H₂ – preferential diffusion



MC: multicomponent diffusion model (Stefan-Maxwell equations)

Lewis: Lewis number is constant but varying for each of the species (Curtiss-Hirschfelder approximation)

Modelling H₂ – preferential diffusion



Mixture fraction Z: mixedness of the fuel and air

Z = 0 : pure air

Z = 1 : pure fuel

Z = constant everywhere: perfectly premixed and constant fuel/air ratio (= constant equivalence ratio)

Z ≠ constant: new independent variable!

$$\frac{\partial \rho Z}{\partial t} + \nabla \cdot (\rho \mathbf{u} Z) - \nabla \cdot \left(\frac{\lambda}{c_p} \nabla \beta_Z \right) = 0,$$

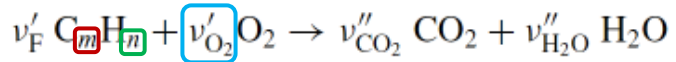
$$\frac{\partial \rho h}{\partial t} + \nabla \cdot (\rho \mathbf{u} h) - \nabla \cdot \left(\frac{\lambda}{c_p} \beta_{h1} \nabla T + \frac{\lambda}{c_p} \nabla \beta_{h2} \right) = 0,$$

$$\frac{\partial \rho C}{\partial t} + \nabla \cdot (\rho \mathbf{u} C) - \nabla \cdot \left(\frac{\lambda}{c_p} \nabla \beta_C \right) = \omega_C$$

Modelling H₂

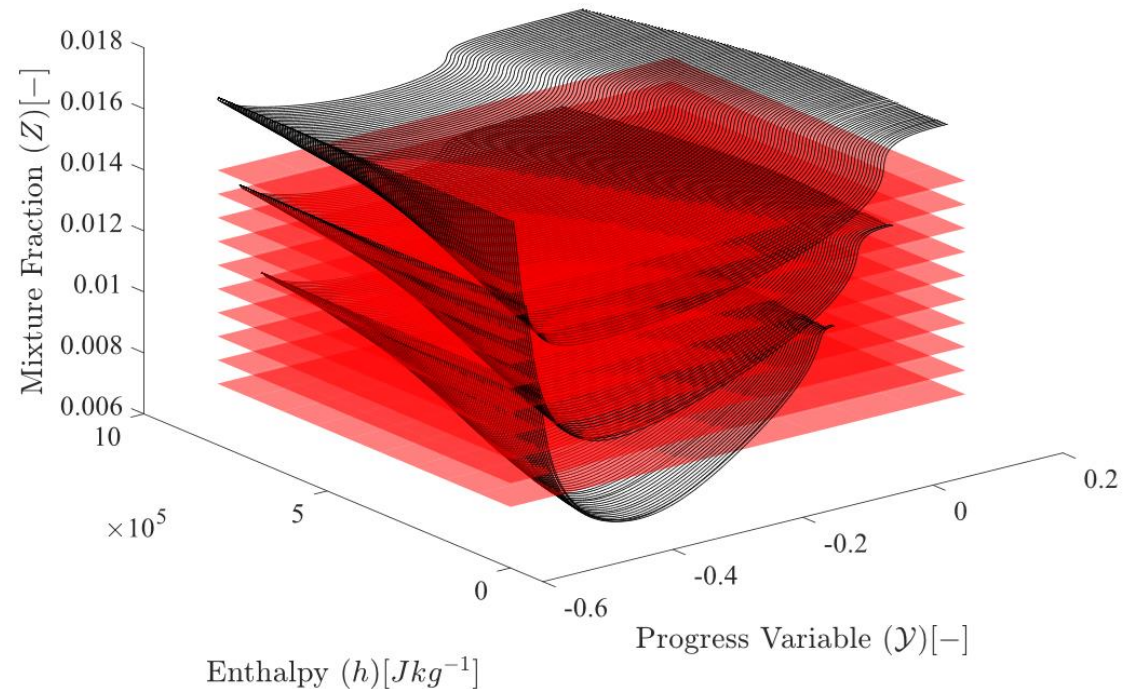
FGM - Extension to hydrogen combustion

General global reaction equation



$$Z = \frac{\frac{1}{mW_C} Z_C + \frac{1}{nW_H} Z_H + \frac{1}{\nu'_{\text{O}_2} W_O} (Y_{\text{O}_{2,2}} - Z_O)}{\frac{1}{mW_C} Z_{C,1} + \frac{1}{nW_H} Z_{H,1} + \frac{1}{\nu'_{\text{O}_2} W_O} Y_{\text{O}_{2,2}}}$$

➔ The equation for Z is fuel dependent.
Current implementation includes equations
for CH₄ and H₂.

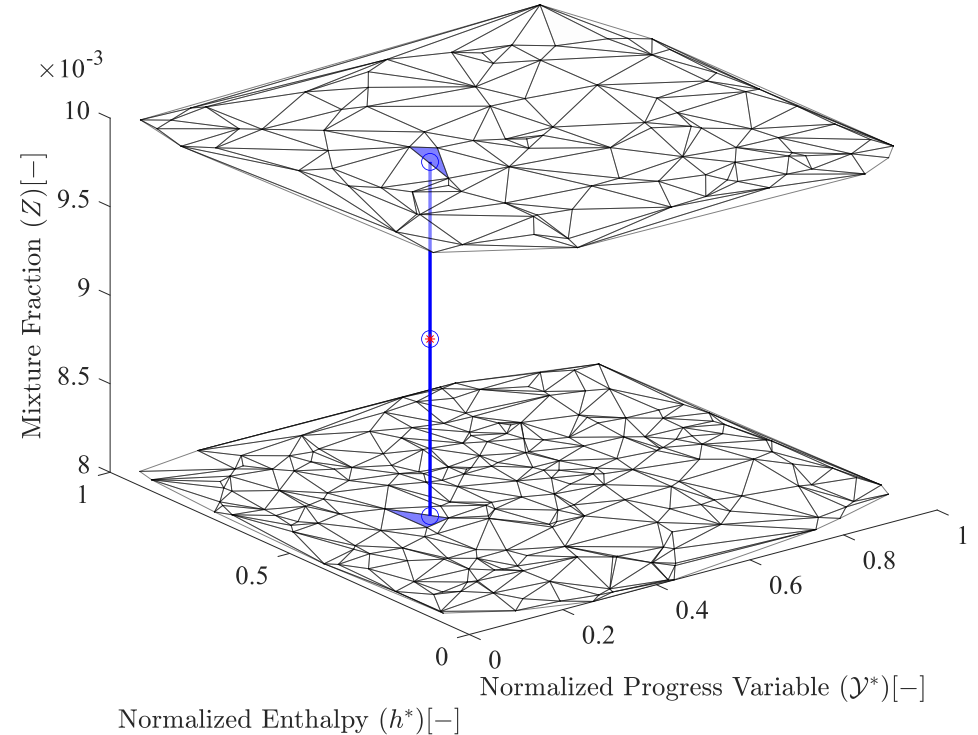


Modelling H_2

FGM – extension to hydrogen combustion

► 3D quasi-unstructured lookup:

1. Find inclusion cells on mixture fraction levels.
2. 2D data interpolation in inclusion triangles.
3. Linear data interpolation along mixture fraction direction.

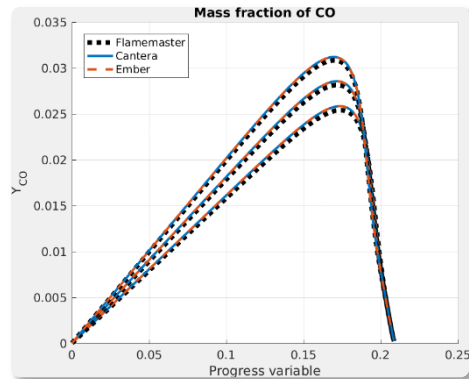


Modelling H₂

Combustion modeling: Tool chain

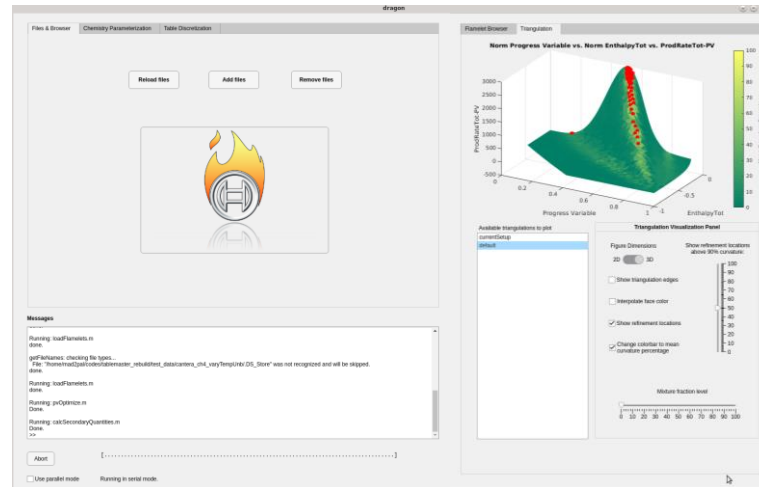
1. Perform 1D simulations with detailed chemistry

- ▶ Chem1D, Cantera & Ember
- ▶ Typically: ~50 PDEs coupled through ~300 coupled nonlinear reaction equations



2. Tabulate 1D solutions in look-up tables

- ▶ Tabulate as $f(C, Z, H)$
- ▶ Unstructured discretization
 - ▶ Local refinement for memory reduction
- ▶ In house developed MATLAB tool



3. Solve 3D transport equations

- ▶ SU2 solver suite
- ▶ Just 5 additional PDEs, reaction source terms from look-up tables
- ▶ C++ code base
- ▶ Automatic differentiation for adjoint gradients using CoDiPack



<https://su2code.github.io/>

H₂ IN THE BUILT ENVIRONMENT

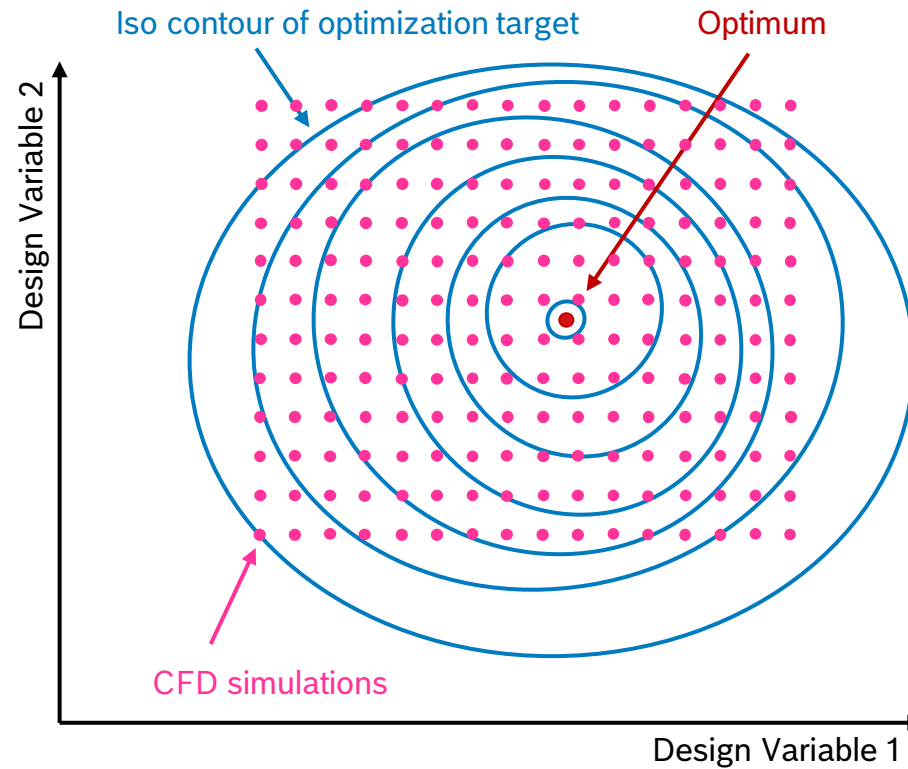
H₂ VS. NATURAL GAS

MODELLING H₂

ADJOINT DESIGN OPTIMIZATION

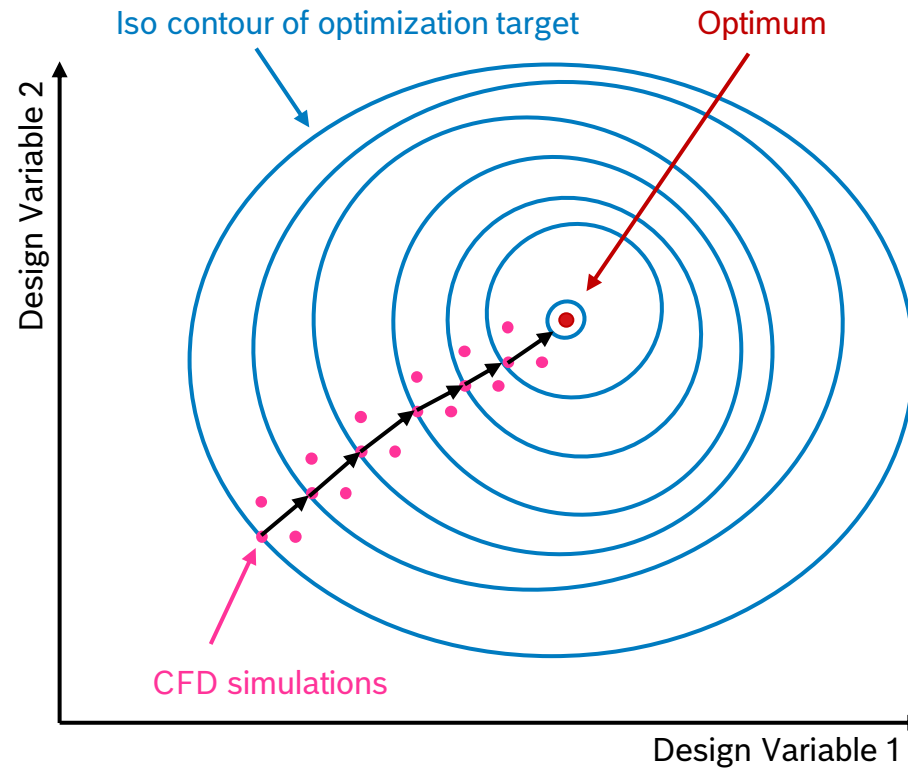
Adjoint design optimization

Design of Experiments (DOE)



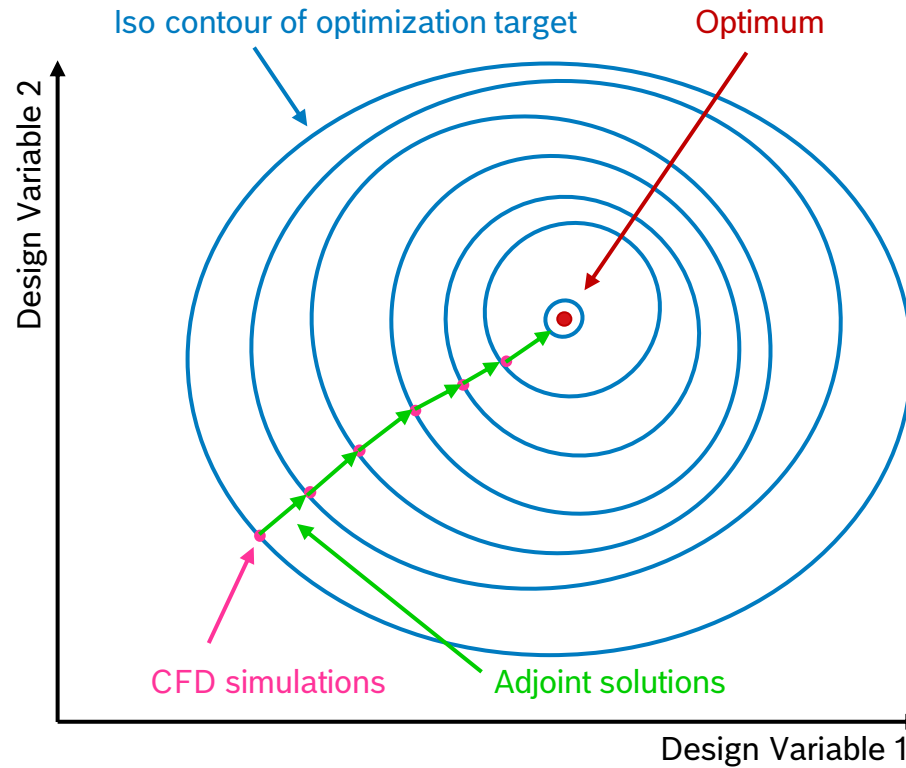
Adjoint design optimization

Gradient-based shape optimization



Adjoint design optimization

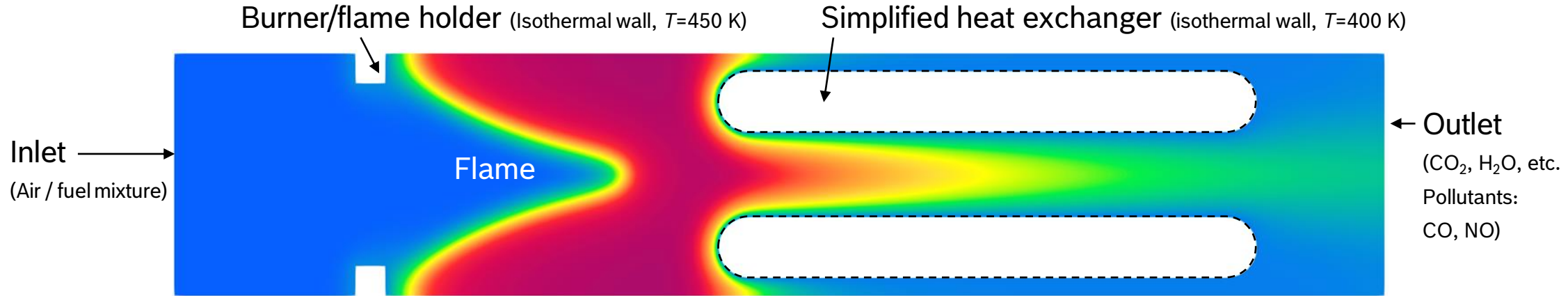
adjoint optimization



Adjoints can be used to very efficiently calculate gradients for an arbitrary number of design variables.

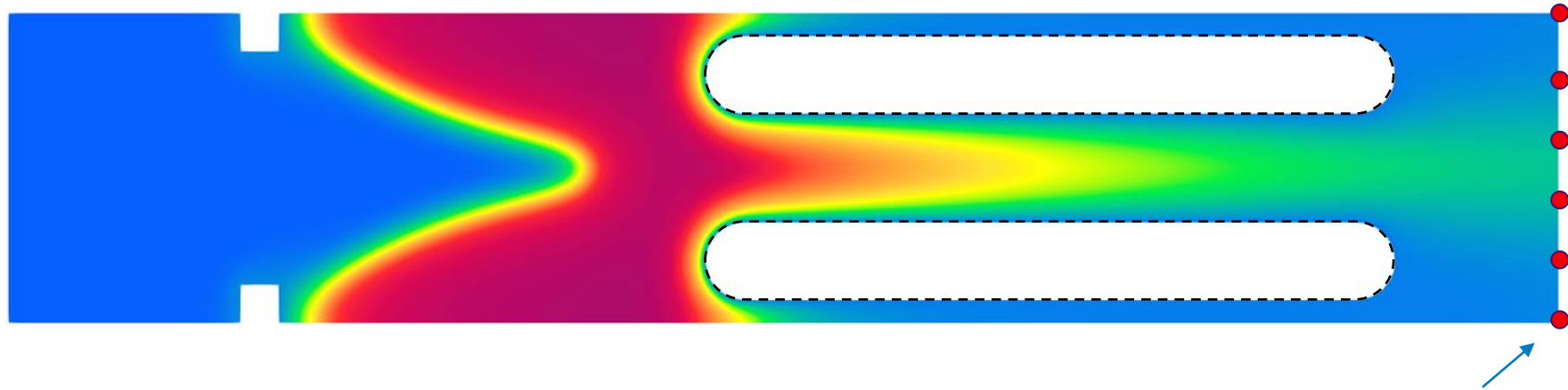
Adjoint design optimization

Objectives in design optimization



Adjoint design optimization

Objectives in design optimization



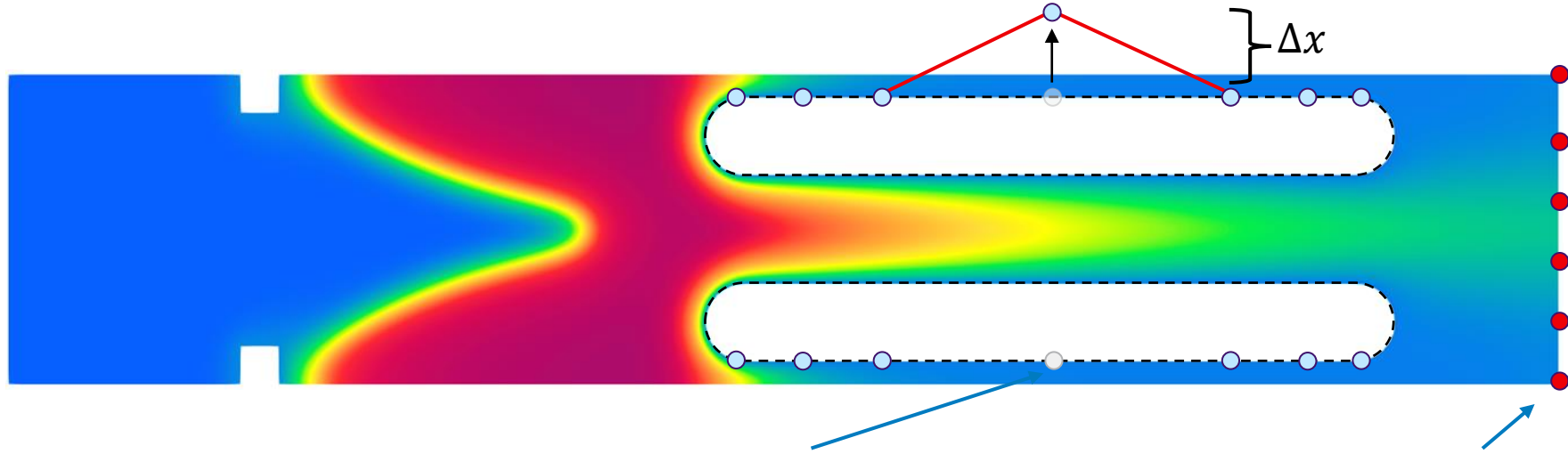
objective: minimize NO_x emissions at the outlet
objective: J

$$\min(J) = \sum Y_{\text{NO}_x}(x_{\text{out}}, y_i)$$

Adjoint design optimization

Objectives in design optimization

$$\frac{\partial J}{\partial x} = \begin{cases} > 0 : \text{move in opposite direction} \\ < 0 : \text{move in that direction} \end{cases}$$



control variables (design variables): surface nodes
 $\alpha = \bar{x} = (x_1, y_1, x_2, y_2, \dots)$

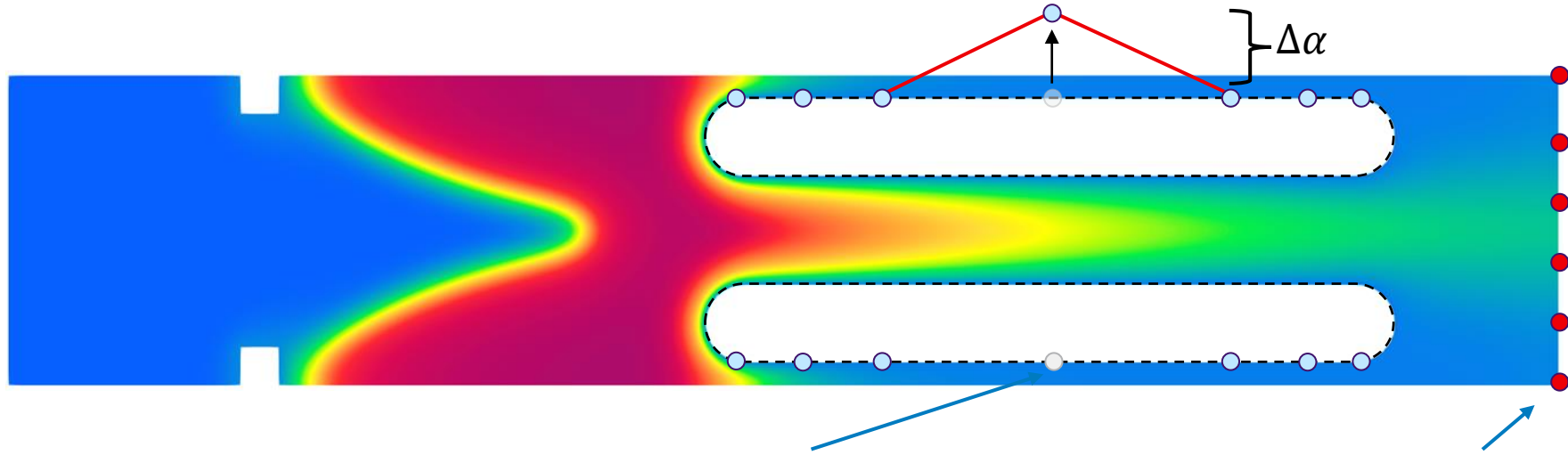
objective J: minimize NO_x emissions at the outlet

$$\min(J) = \sum Y_{\text{NO}_x}(x_{\text{out}}, y_i)$$

Adjoint design optimization

Objectives in design optimization

$$\frac{\partial J}{\partial \alpha} = \begin{cases} > 0 : \text{move in opposite direction} \\ < 0 : \text{move in that direction} \end{cases}$$



control variables (design variables): surface nodes

$$\alpha = (x_1, y_1, x_2, y_2, \dots)$$

Governing equations (Navier-Stokes, RANS):

$$R(W, X, \alpha) = 0$$

objective J: minimize NO_x emissions at the outlet

$$\min(J) = \sum Y_{\text{NO}_x}(x_{\text{out}}, y_i)$$

Adjoint design optimization

introduce Lagrange multiplier Λ and construct Lagrange function for the objective:

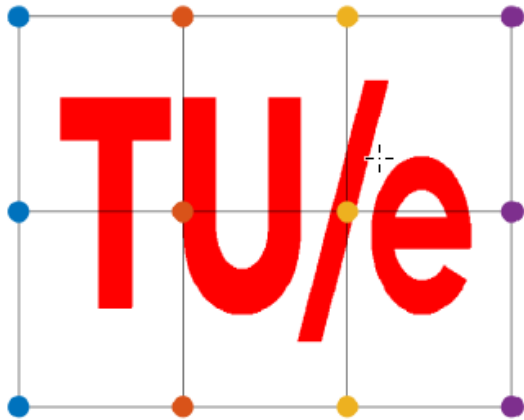
$$L = J + \Lambda^T R \quad \longrightarrow \quad \frac{dL}{d\alpha} = \frac{d}{d\alpha} (J(W, X, \alpha) + \Lambda^T R(W, X, \alpha))$$

$$\frac{dL}{d\alpha} = \left\{ \frac{\partial J}{\partial X} + \Lambda^T \frac{\partial R}{\partial X} \right\} \frac{dX}{d\alpha} + \underbrace{\left\{ \frac{\partial J}{\partial W} + \Lambda^T \frac{\partial R}{\partial W} \right\} \frac{dW}{d\alpha}}_{\text{change of Navier Stokes solution wrt. change in design variables}}$$

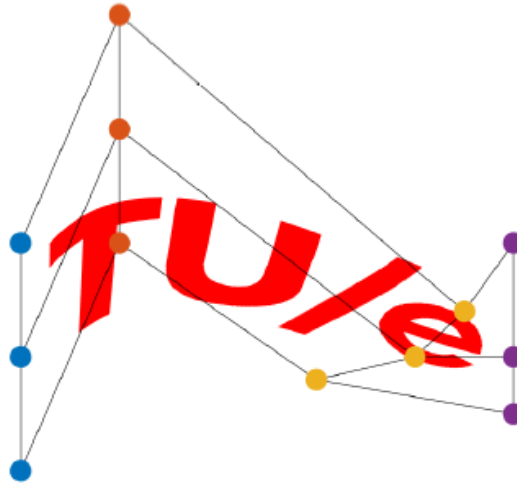
choose Lagrange multiplier such that $\frac{\partial J}{\partial W} + \Lambda^T \frac{\partial R}{\partial W} = 0$

Adjoint design optimization

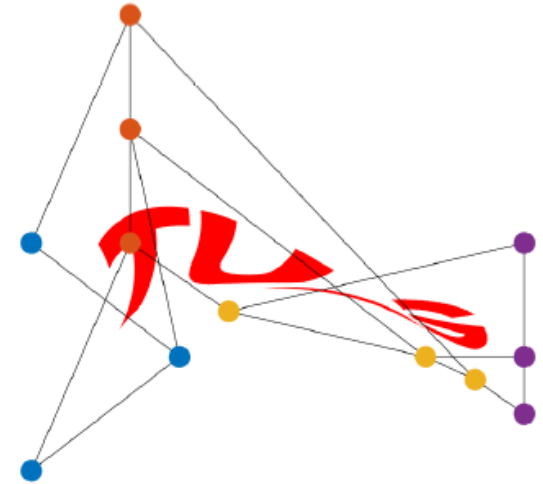
Free Form Deformation (FFD)



FFD box with 12 nodes



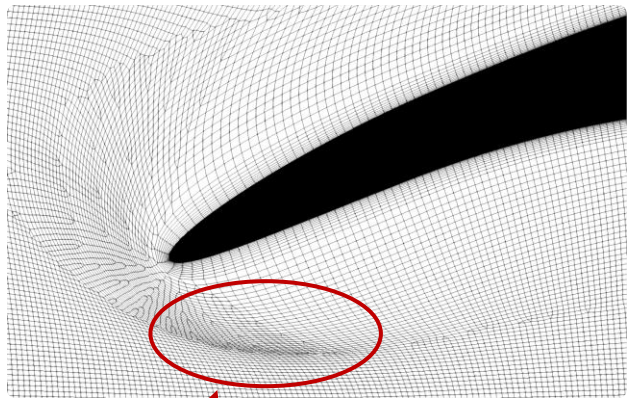
logo deformed by
moving the FFD nodes
of the FFD box



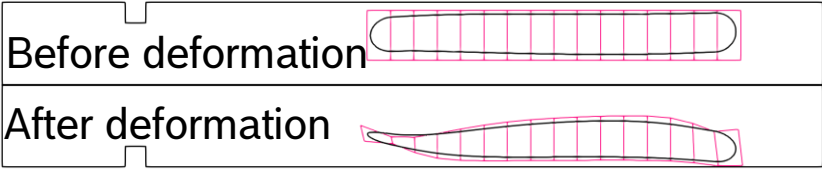
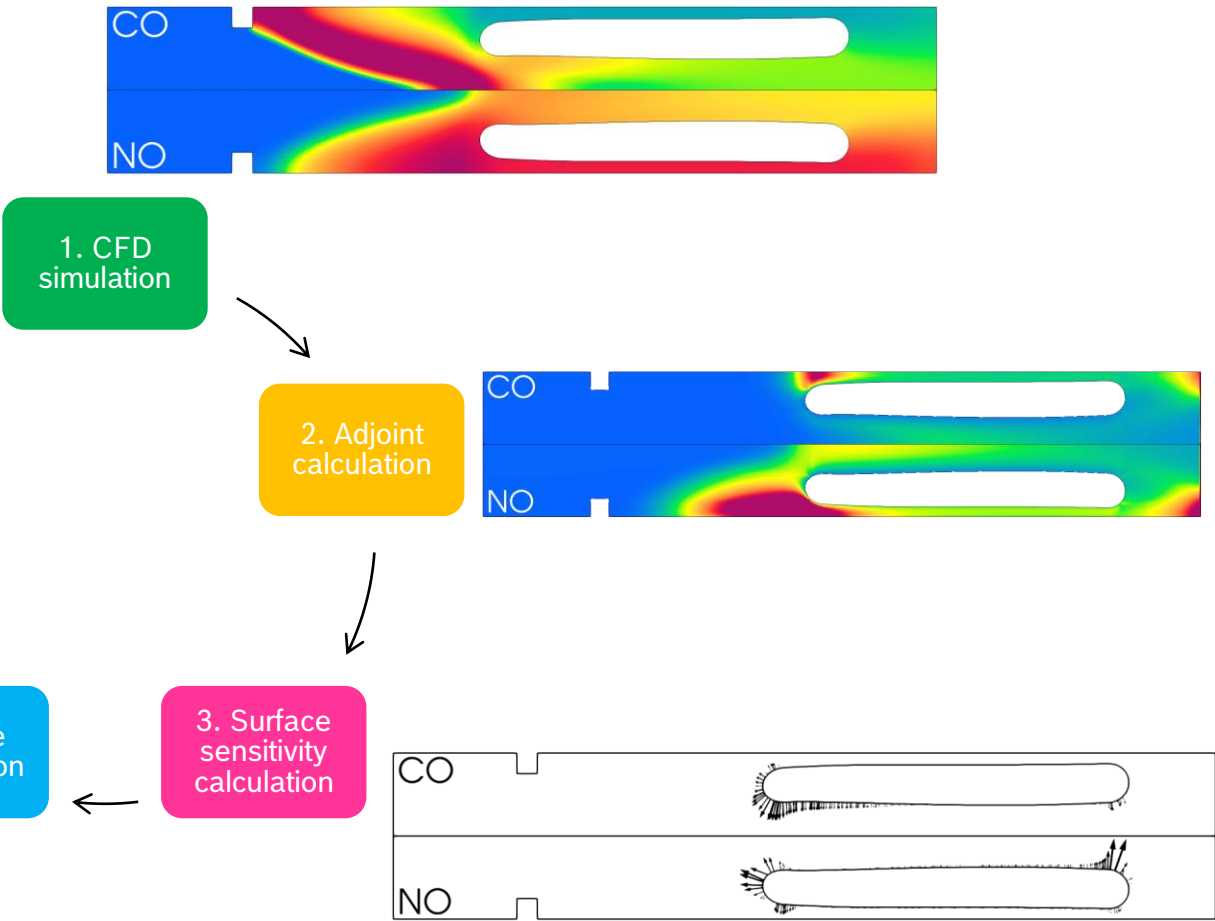
invalid deformation

Adjoint design optimization

Optimization loop



That's bad.

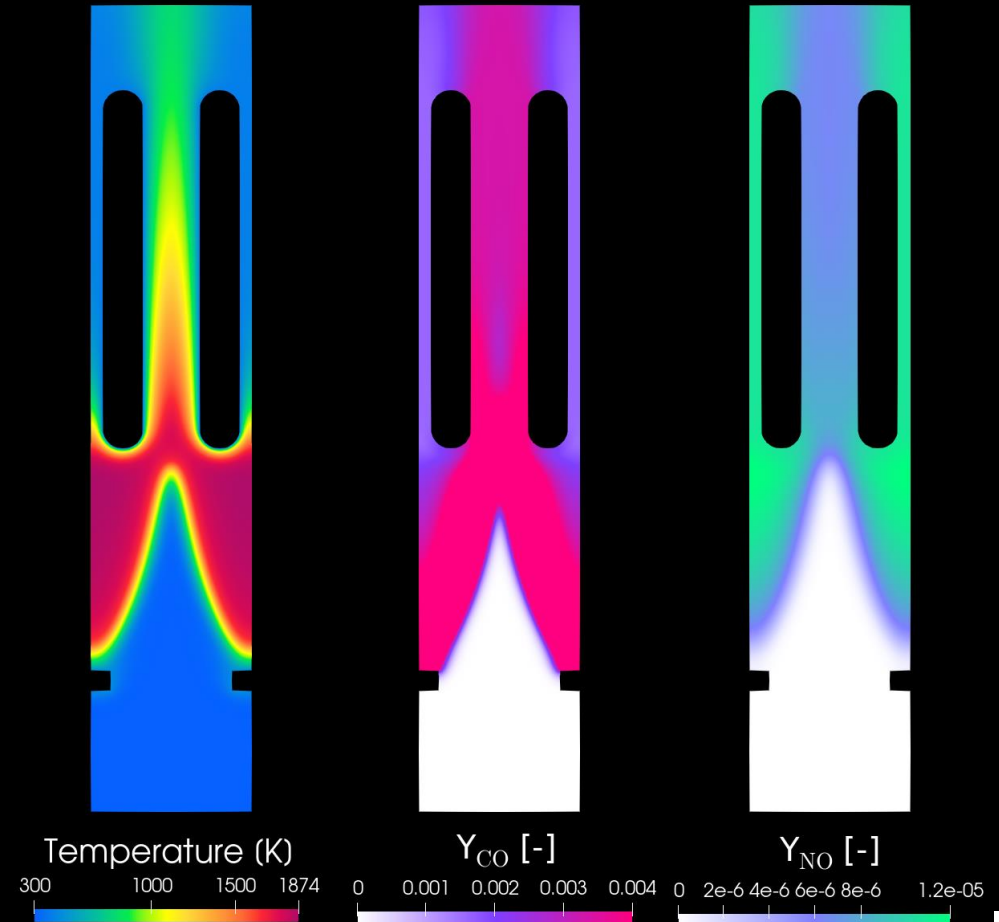


Adjoint design optimization

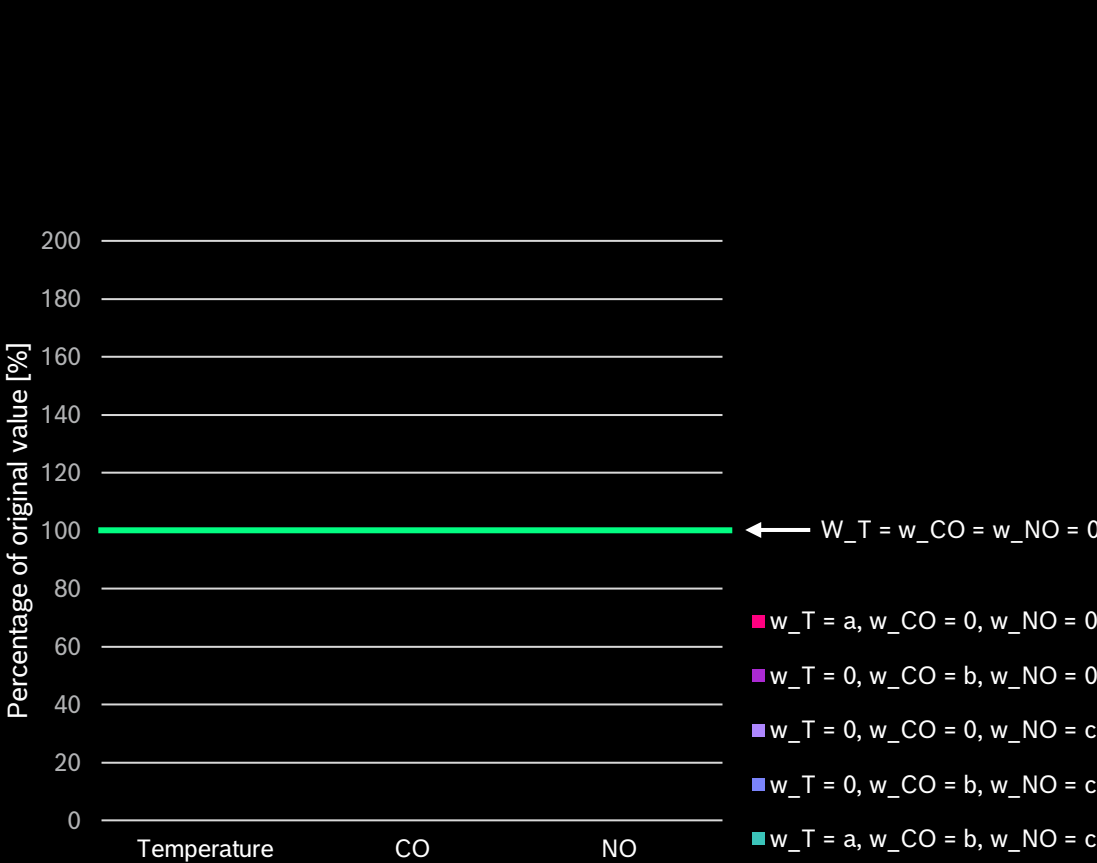
5 optimizations were performed with the following objective weights:

	T	Y_{CO}	Y_{NO}
1	$5e-10=a$	0	0
2	0	$1e-4=b$	0
3	0	0	$1e-2=c$
4	0	$1e-4=b$	$1e-2=c$
5	$5e-10=a$	$1e-4=b$	$1e-2=c$

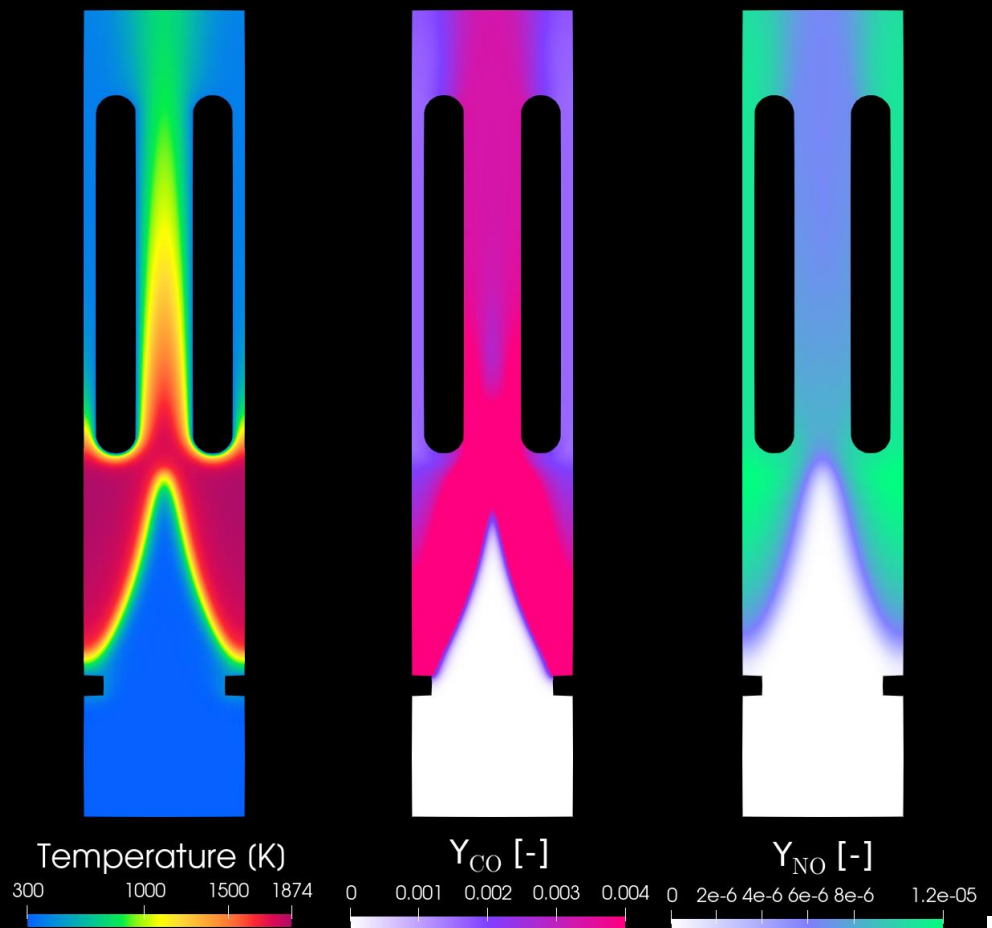
Baseline



Adjoint design optimization

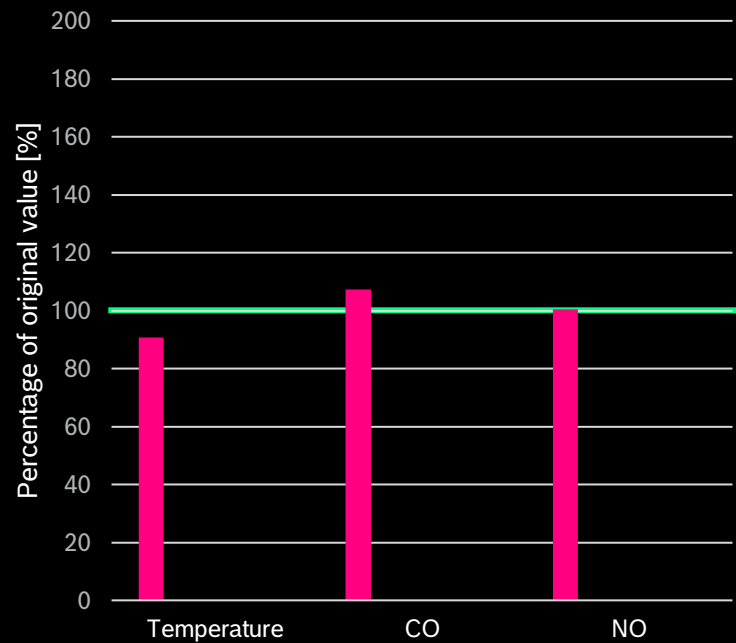


Baseline

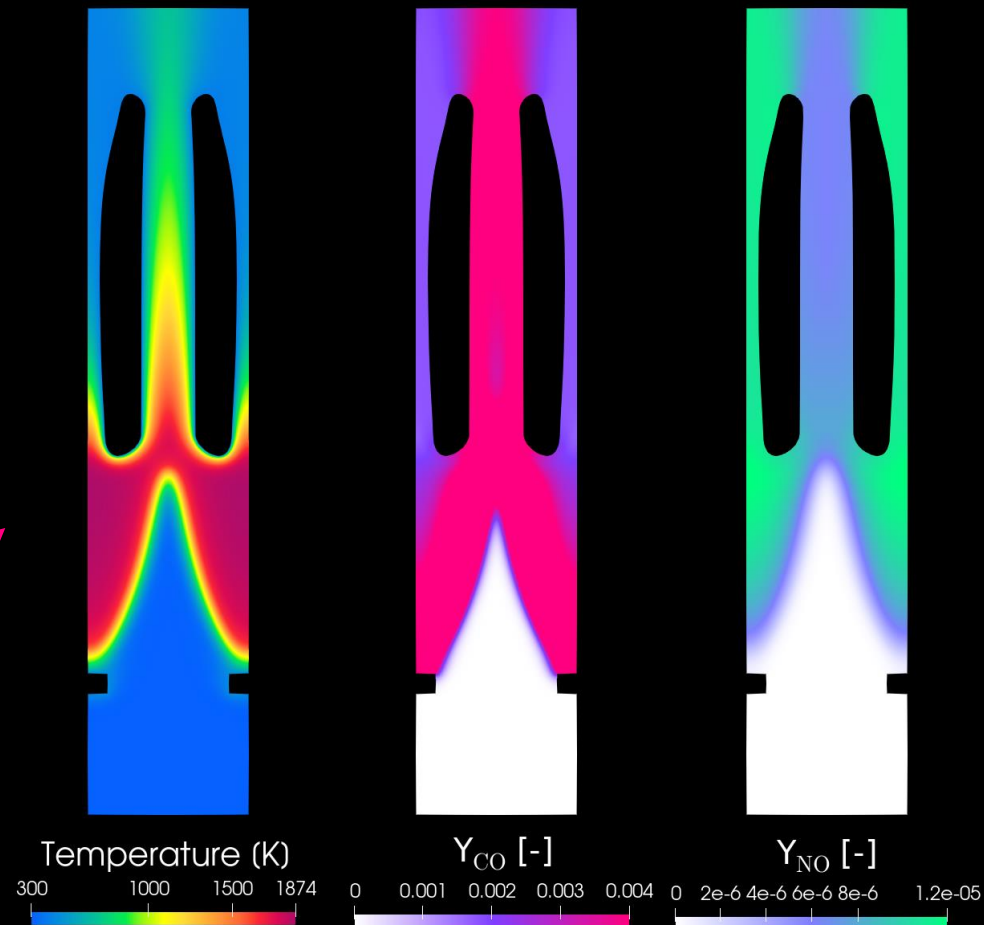


Adjoint design optimization

Optimize Temperature only

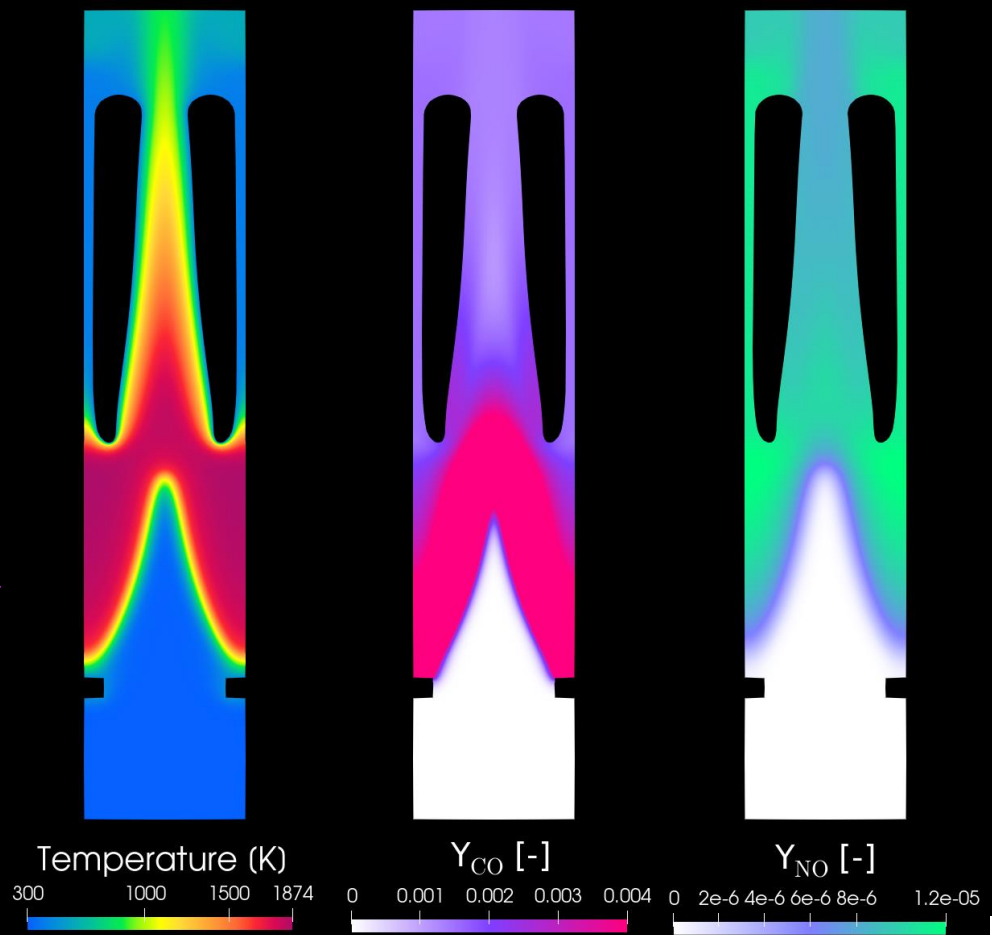
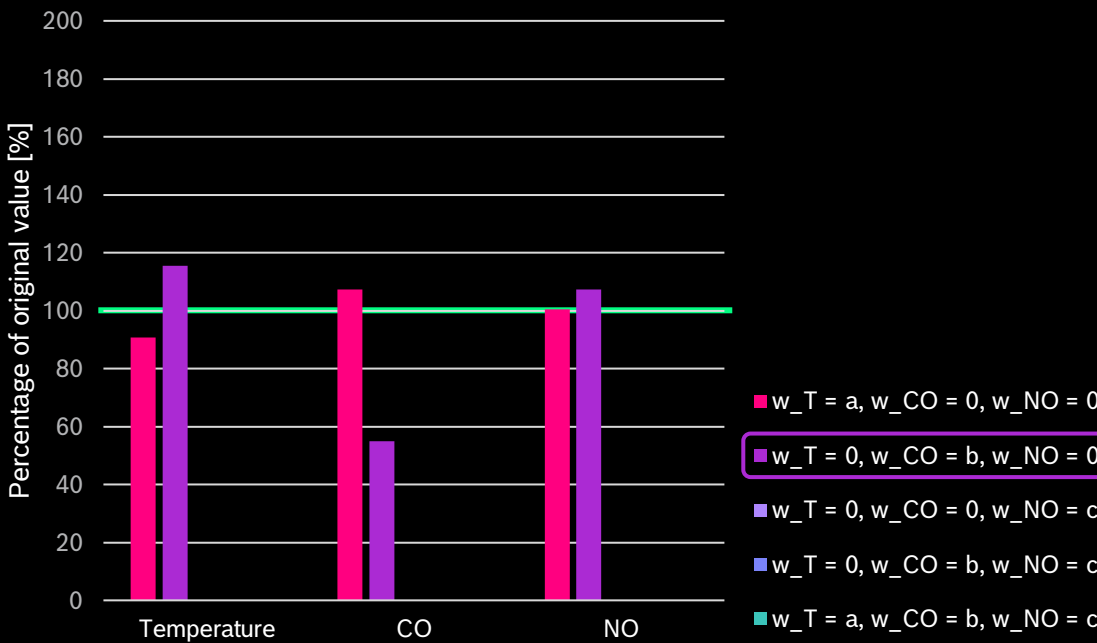


- $w_T = a, w_{CO} = 0, w_{NO} = 0$
- $w_T = 0, w_{CO} = b, w_{NO} = 0$
- $w_T = 0, w_{CO} = 0, w_{NO} = c$
- $w_T = 0, w_{CO} = b, w_{NO} = c$
- $w_T = a, w_{CO} = b, w_{NO} = c$



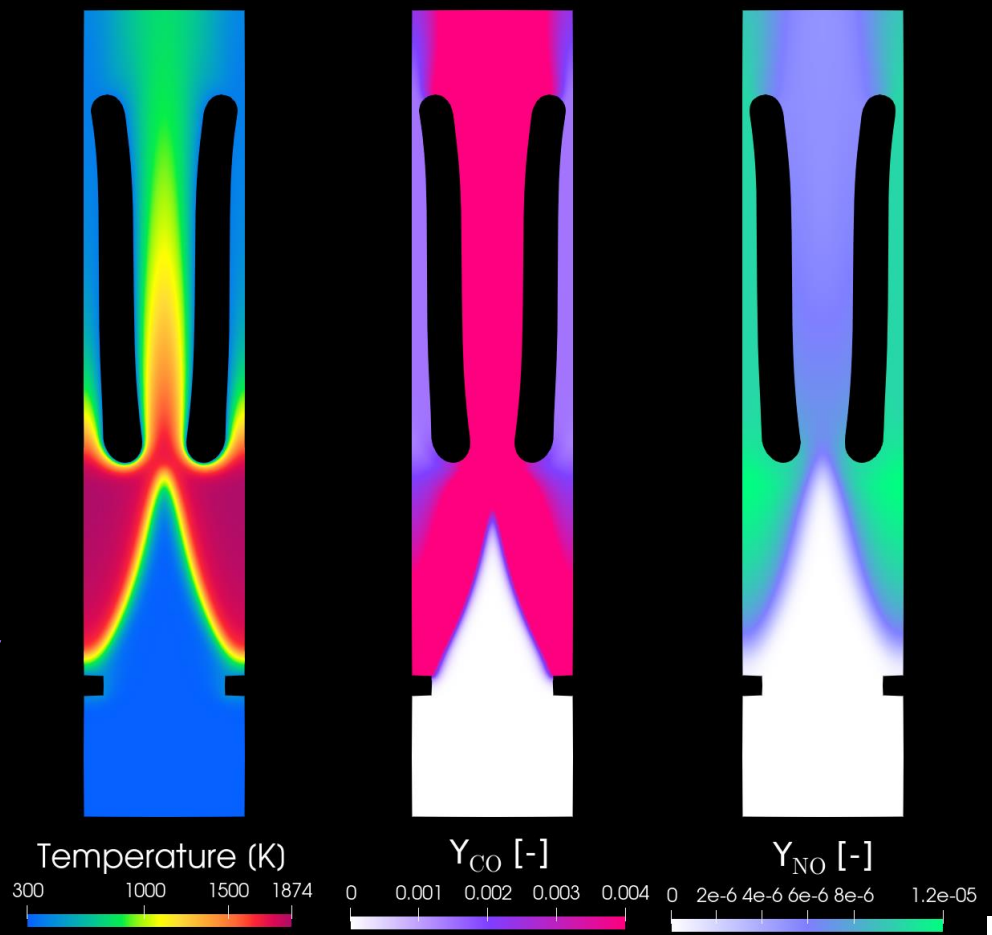
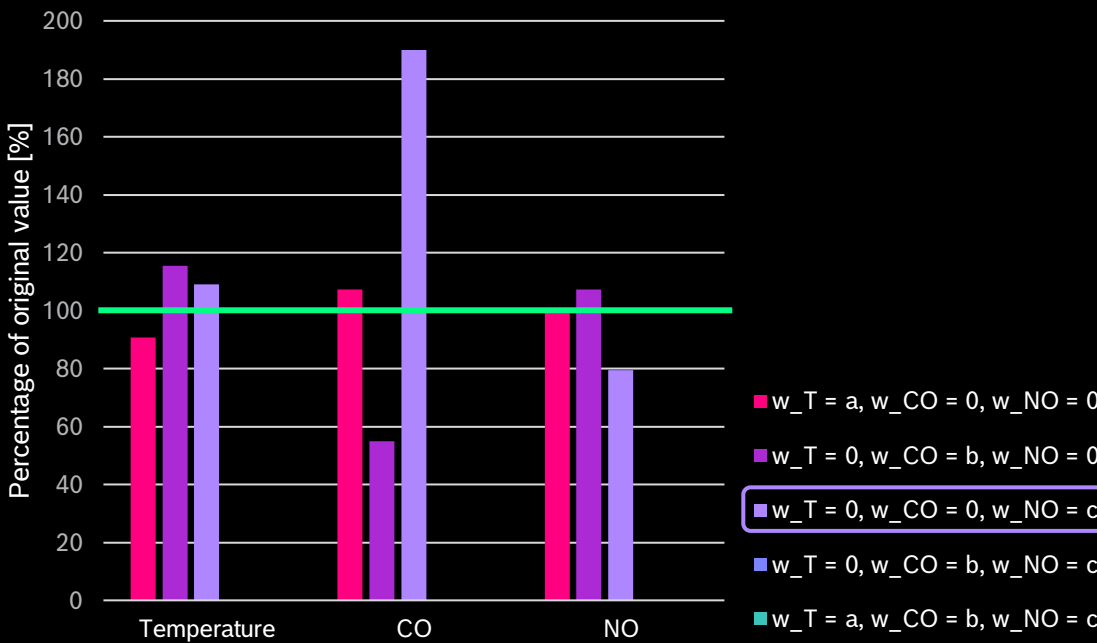
Adjoint design optimization

Optimize Y_{CO} only



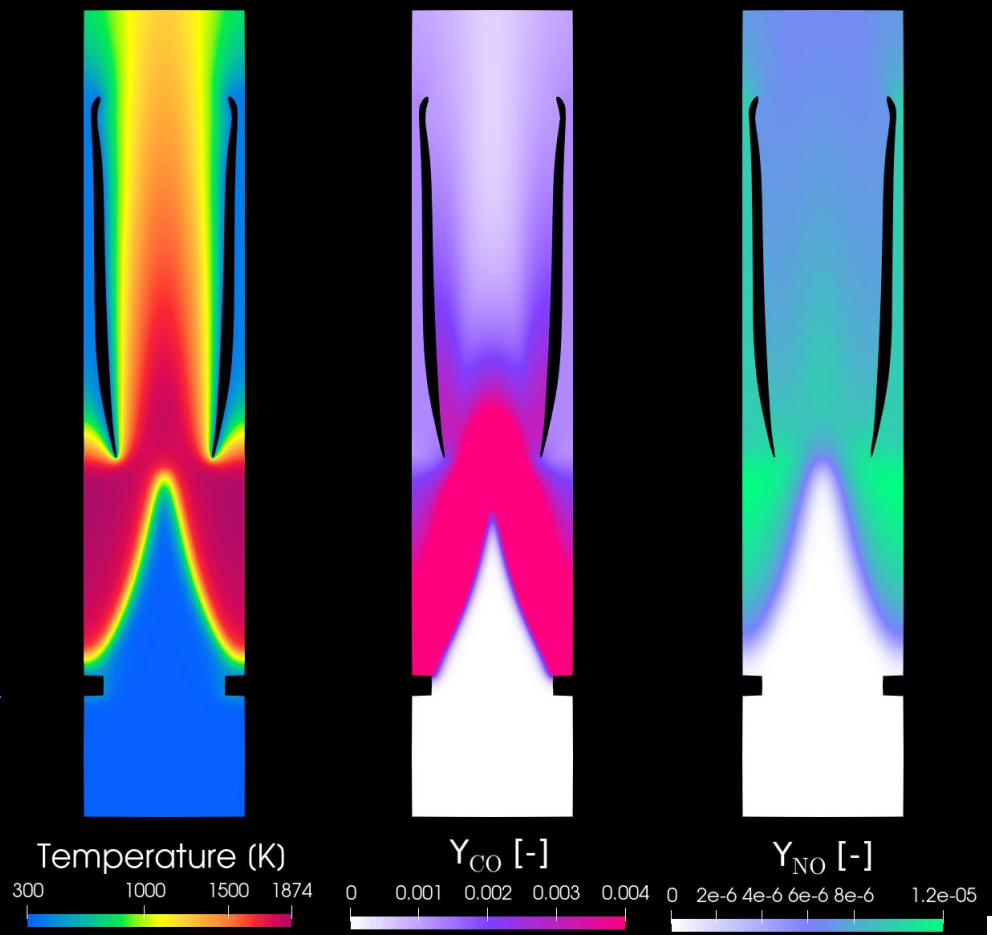
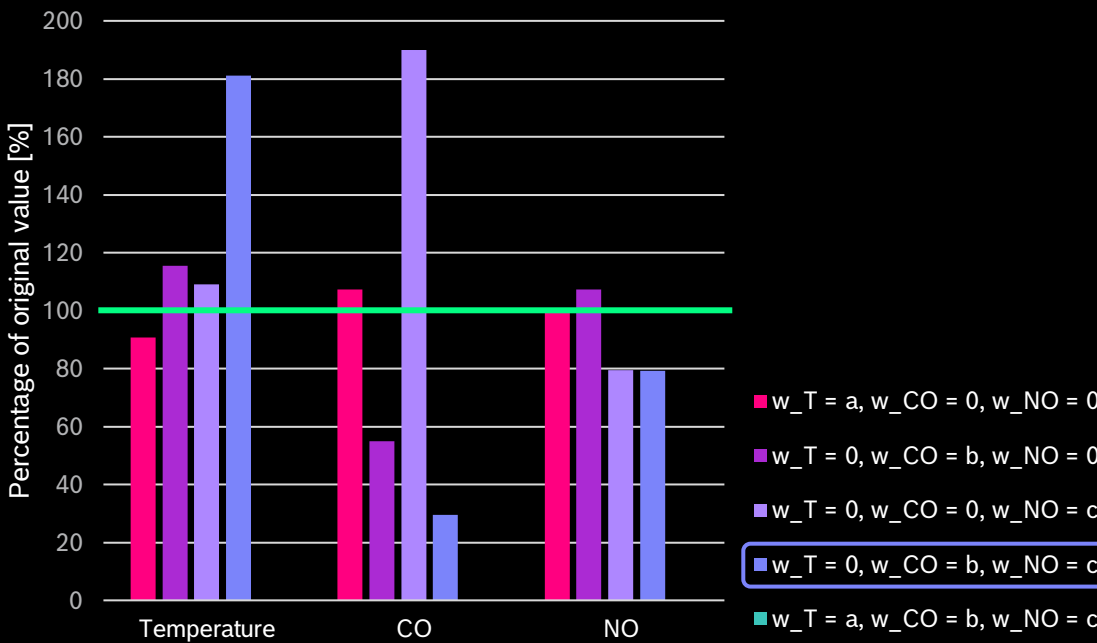
Application to Optimization

Optimize Y_{NO} only



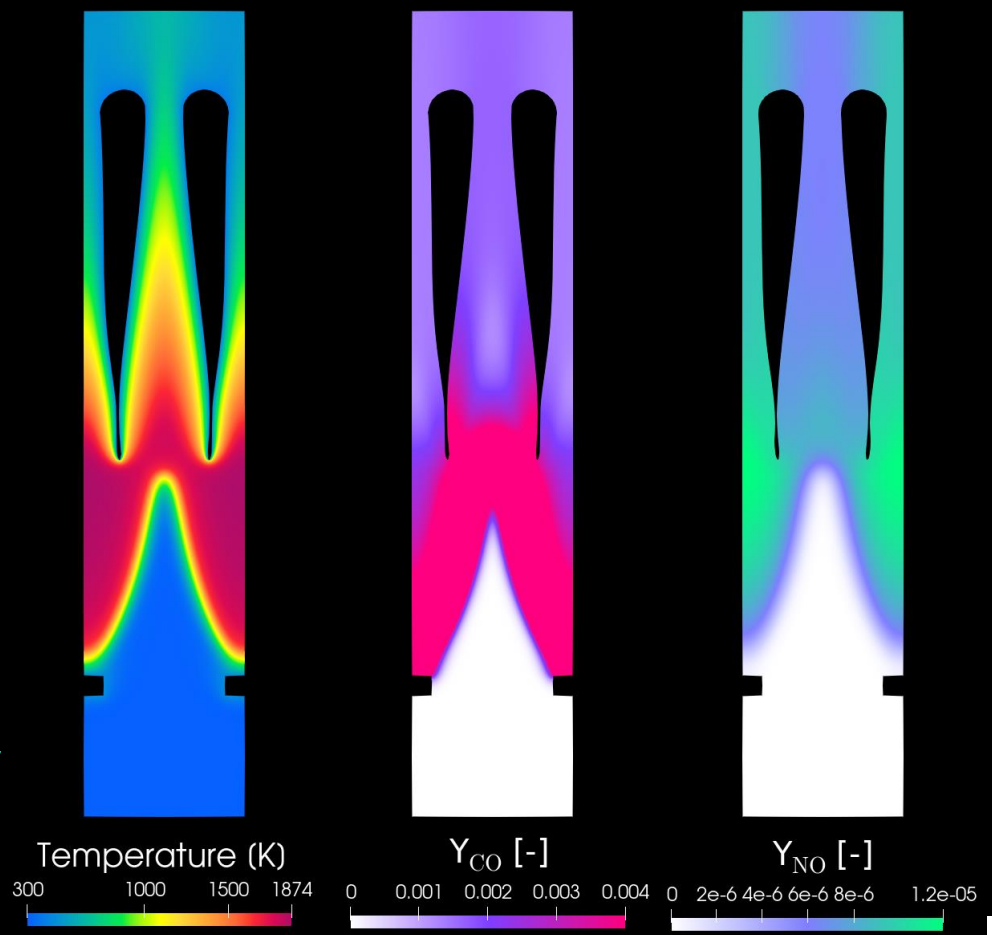
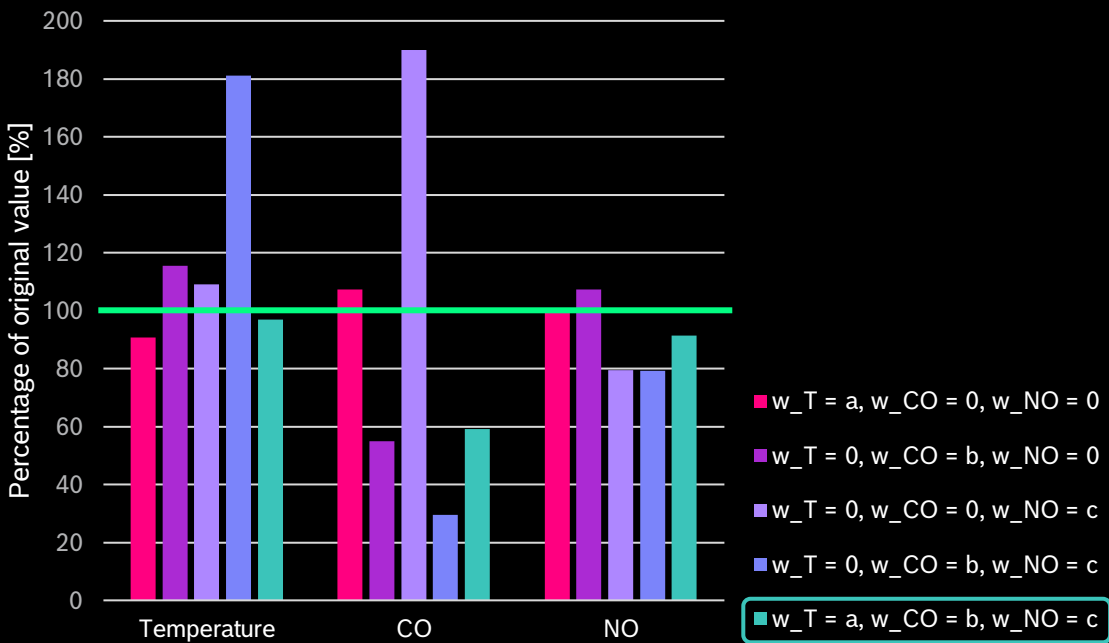
Adjoint design optimization

Optimize Y_{CO} & Y_{NO}

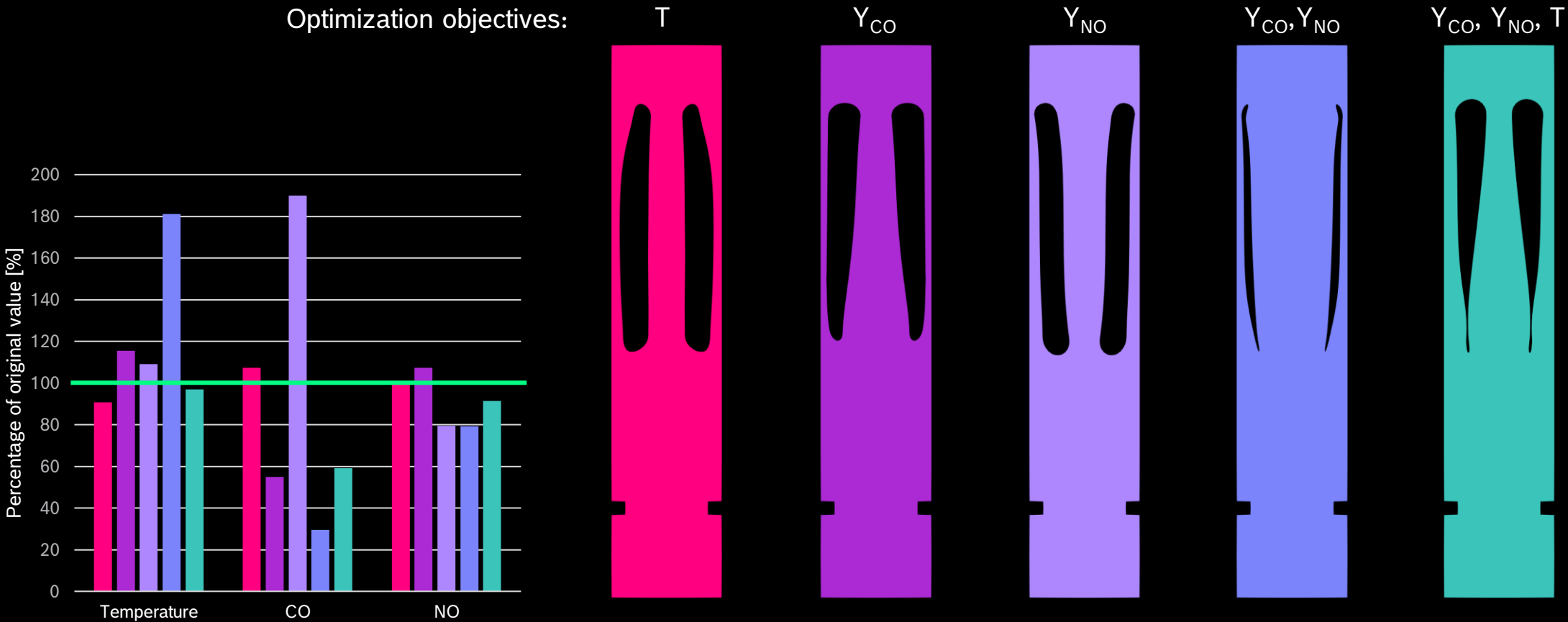


Adjoint design optimization

Optimize Y_{CO} , Y_{NO} , and Temperature

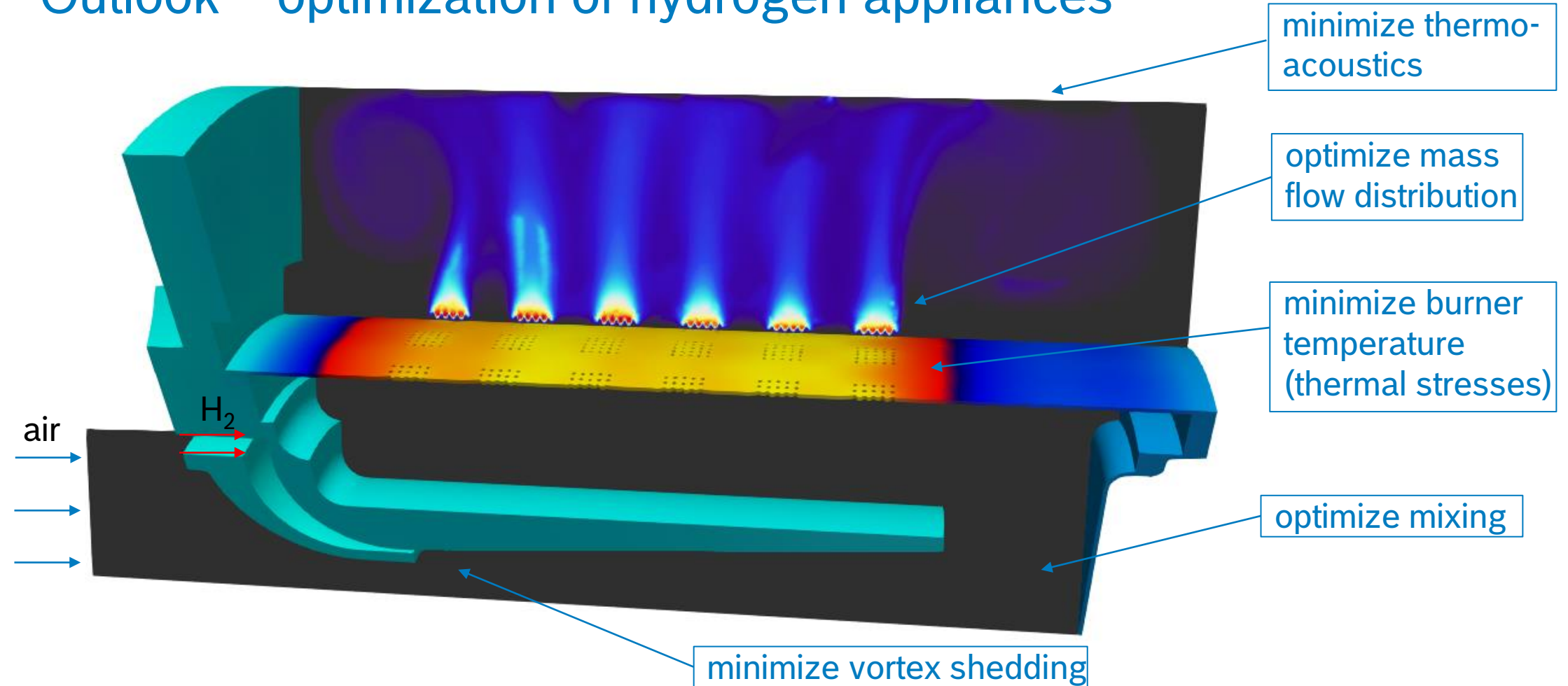


Adjoint design optimization



Adjoint design optimization

Outlook – optimization of hydrogen appliances



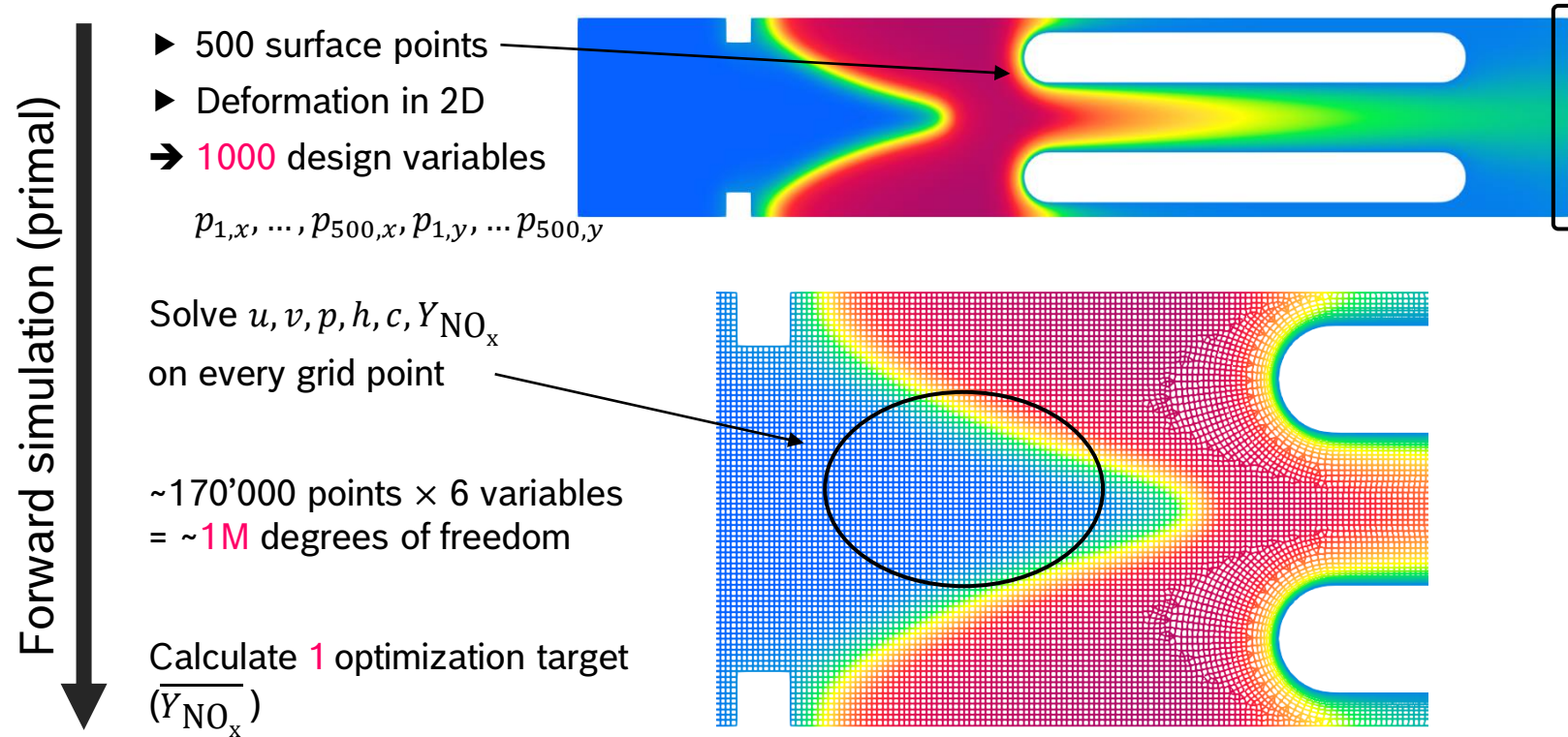
THANK YOU!

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Adjoint-based design optimization for combustion applications

The adjoint approach: Forward simulation (CFD)

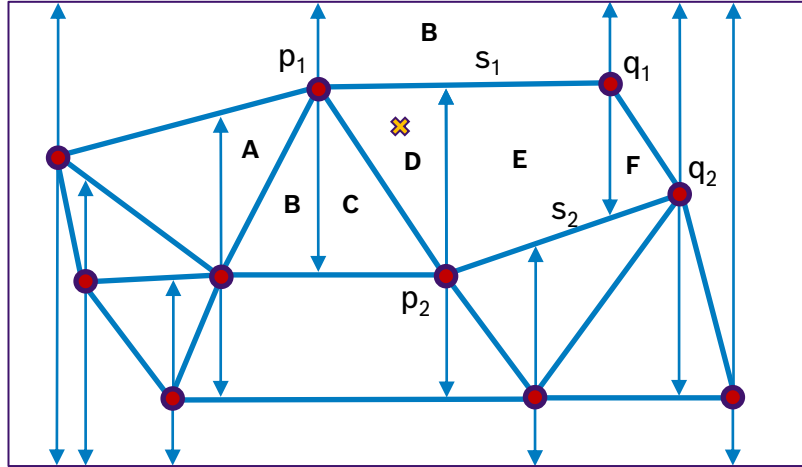


- ▶ 1000 primal solutions are needed to calculate the gradient of $\overline{Y_{\text{NO}_x}}$ with respect to the design variables (DVs).
- ▶ We are interested in the effect of 1000 DVs on 1 target and throw away 1M variables needed for the computation.

Adjoint-based design optimization for combustion applications

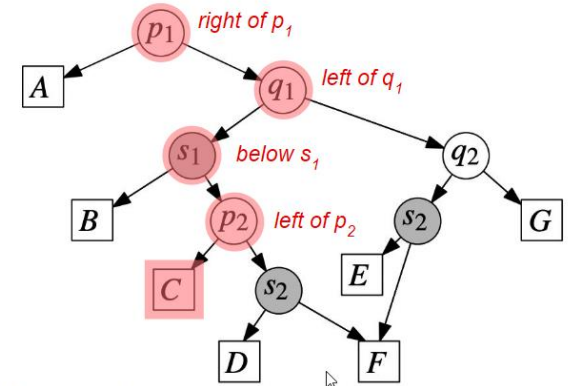
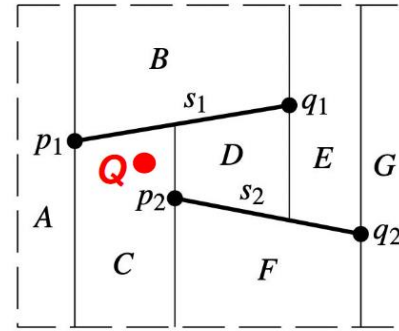
trapezoidal map – data structure

► Data storage: Directed Acyclic Graph

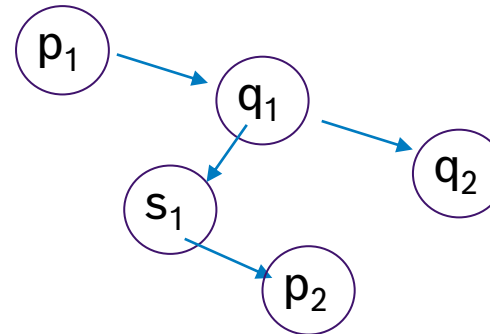


Directed Acyclic Graph (DAG)

- Intermediate notes are vertices (vertical lines) and line segments
- The leaves are the trapezoidal regions (map back to original polygons)



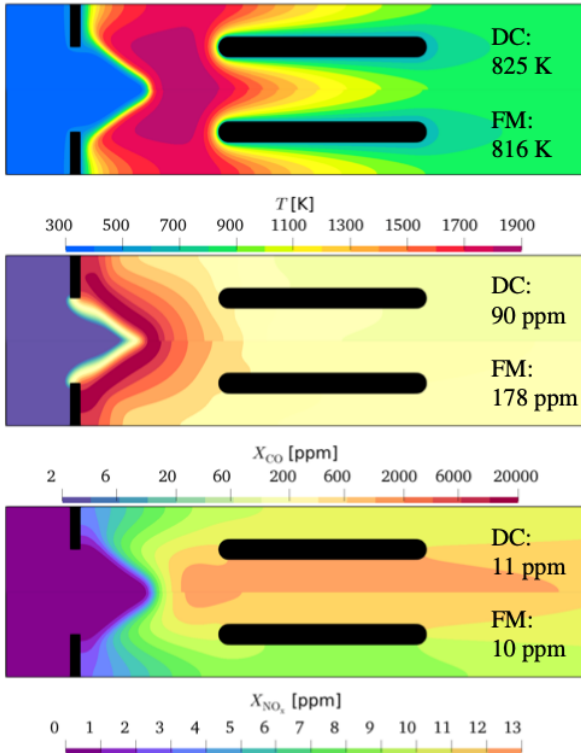
Computational Geometry Algorithms and Applications, de Berg, Cheong, van Kreveld and Overmars, Chapter 6



Adjoint-based design optimization for combustion applications

Methane/Air test optimization

Model validation^[1]:



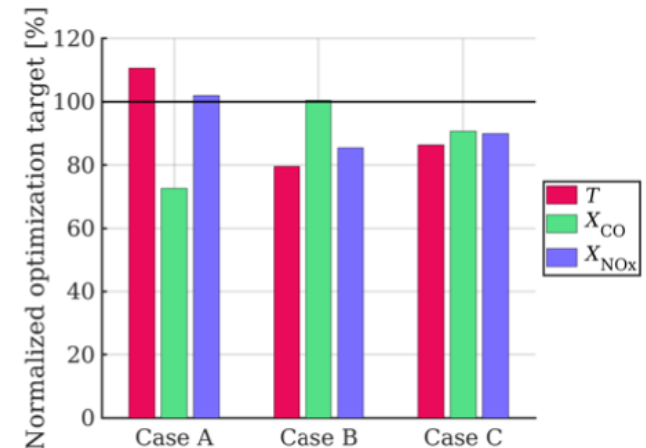
Multi-objective optimization:

- Reduction of temperature T
- Reduction of pollutant emissions X_{CO} and X_{NOx}
- Remeshing using Pointwise in case of no convergenc
- Adjoint: Discrete Adjoint using CoDiPack

► Driver: FADO^[2] framework

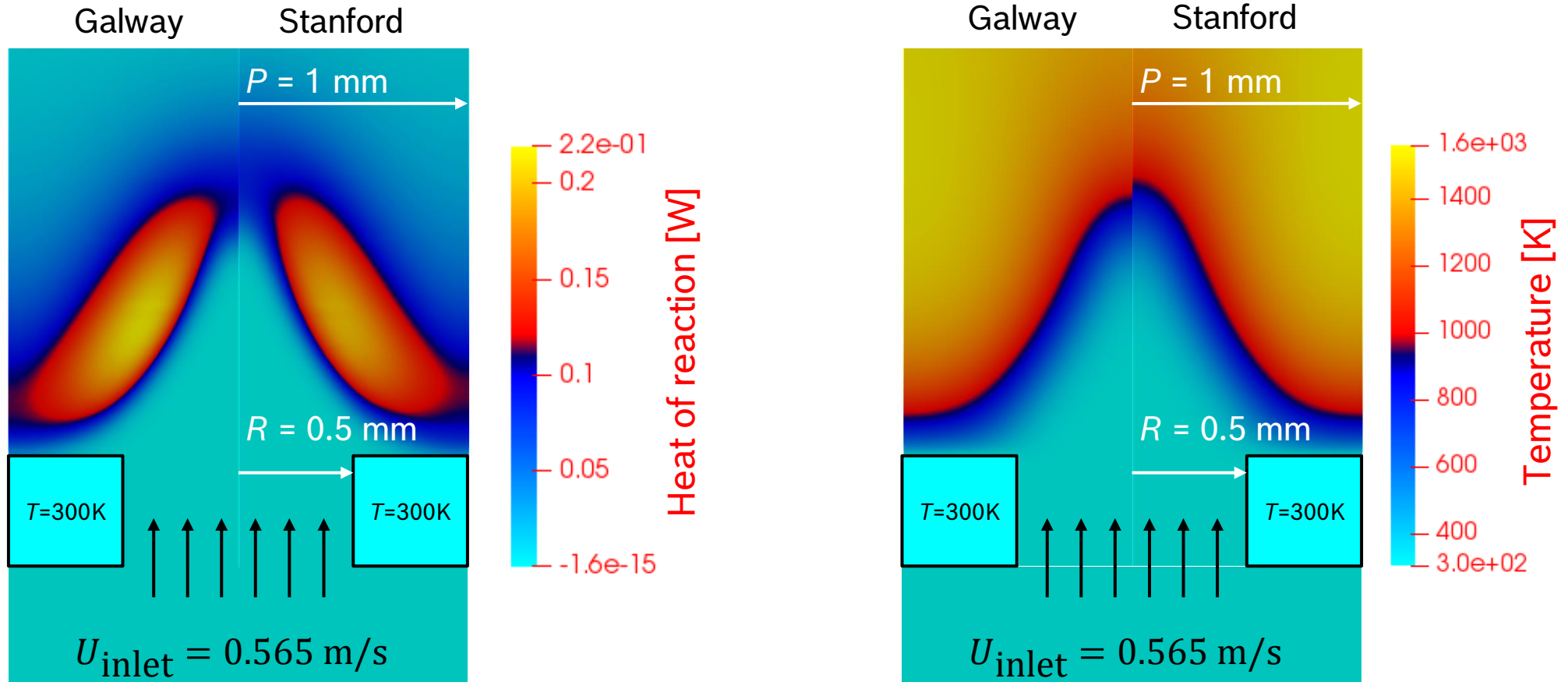
Case	Weight T	Weight X_{CO}	Weight X_{NOx}
A	1/2	4/3	1
B	1	2/3	1
C	1	1	1

Results:



Hydrogen vs. methane

2D planar H_2 -air simulations at $\phi=0.5$ (Fluent v19.2)



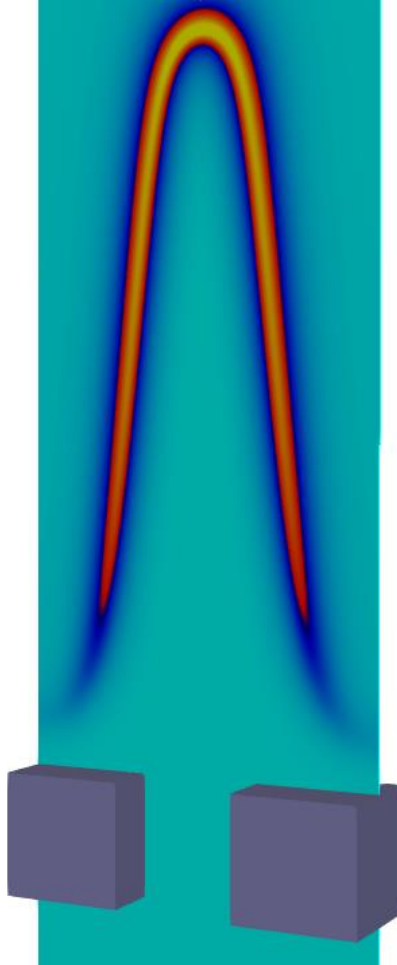
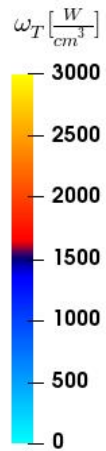
2D simulations show small differences in flame length, heat release rate and temperature

→ Cheaper mechanism (Stanford) is sufficient for this study

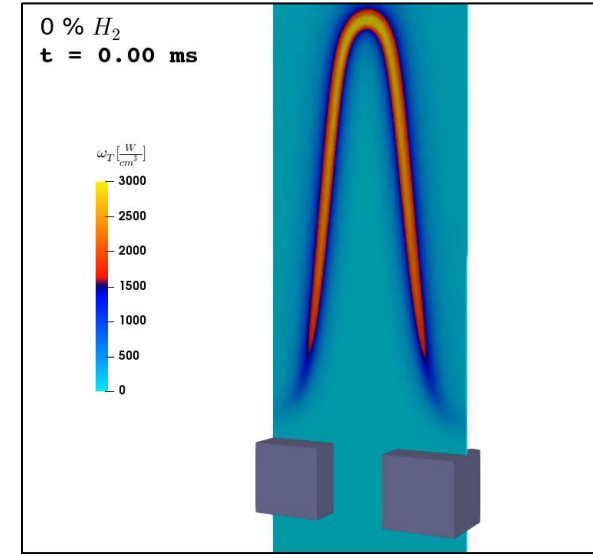
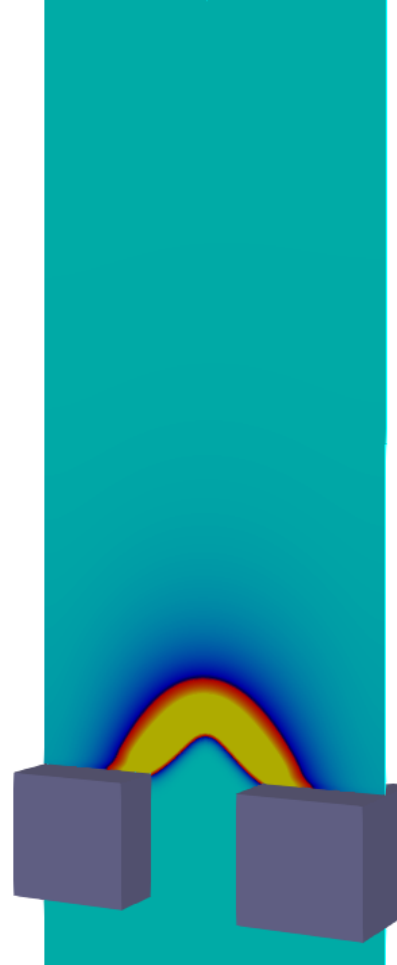
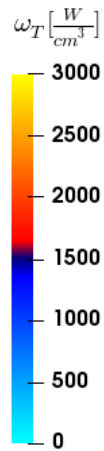
Hydrogen vs. methane

From natural gas to hydrogen

0 % H_2
 $t = 0.00$ ms



100 % H_2
 $t = 125.00$ ms



Hy4Heat

phi=0.80

100% hydrogen
hydrogen ready
hydrogen blend
hybrid

CH4	O2	CH4	H2	
100%	0.2226	0.0447	0.0	
80%	0.2229	0.04215	0.00132	x
60%	0.2233	0.03848	0.00321	x
40%	0.2240	0.03276	0.00615	x
20%	0.2251	0.02264	0.01134	x
10%	0.2265	0.01318	0.01481	
0%	0.2277	0.0	0.02290	

phi	O2	CH4	H2	SL	2*SL
1.0	0.2264	0	0.02847	2.17	4.34
0.8	0.2277	0	0.02290	1.63	3.26
0.6	0.2290	0	0.01728	0.93	1.86
0.5	0.2297	0	0.0144		
0.4	0.2303	0	0.01158	0.25	0.5

Hy4Heat

3D conjugate heat transfer – burner temperature (steel)

phi=0.8			
v=1.63	T=790.04		
v=	T=		

Hy4Heat

conjugate heat transfer – burner temperature (steel)

phi=0.4			
v=0.4	T=		
v=0.5	T=786.16		

Hydrogen vs. methane

from natural gas to hydrogen

here a movie of the 2D planar flame, showing the hydrogen concentration and the time, and 2D contours of the H₂ concentration, temperature, heat release rate, h₂o concentration(?)