

# Detonation-diffuse interface interactions: failure, re-initiation and propagation limits

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**Dutch Section of the Combustion Institute Webinar**

September 23, 2022



# Outline

- 1 PART I: Context and motivation
  - Why combustion?
  - Accidental combustion events
  - Combustion 101
  - Detonation fundamentals
  
- 2 PART II: Talk
  - Non-ideal detonation propagation

# Outline

## 1 PART I: Context and motivation

- Why combustion?
- Accidental combustion events
- Combustion 101
- Detonation fundamentals

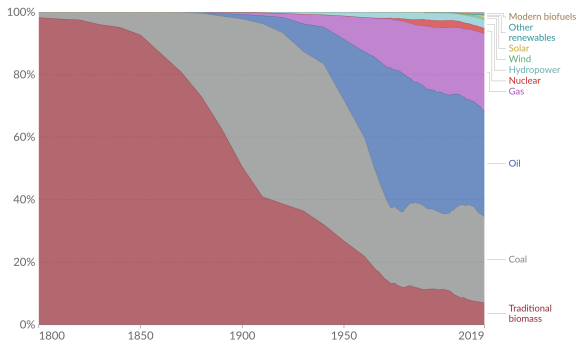
## 2 PART II: Talk

- Non-ideal detonation propagation

# Why combustion?

## Global direct primary energy consumption

Direct primary energy consumption does not take account of inefficiencies in fossil fuel production.



Source: Vaclav Smil (2017) and BP Statistical Review of World Energy

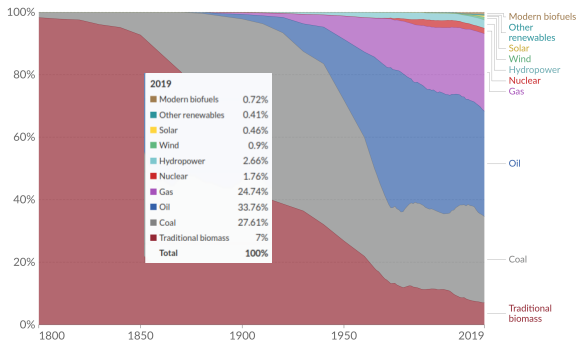
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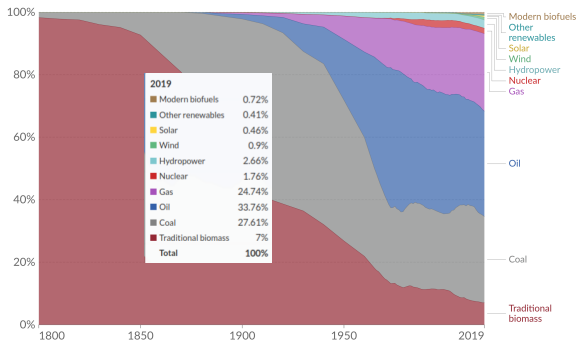
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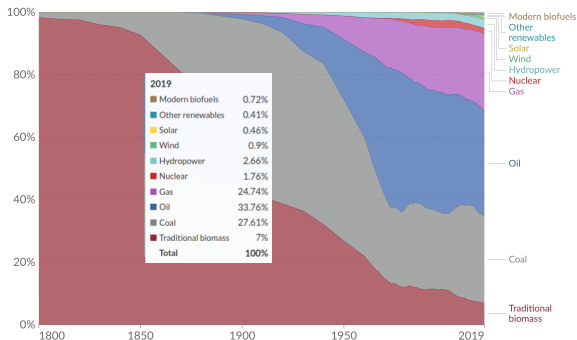
## Take aways

- Over ~ 90% comes from burning something
- Increase in renewables contained in consumption growth
- Picture unlikely to change

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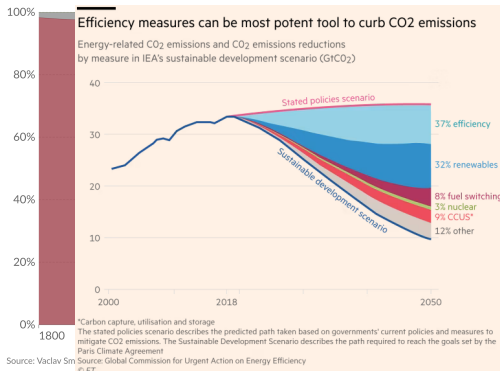
Push for efficiency through...

- Low-carbon bio-/H<sub>2</sub>-enriched
- Carbon-free (i.e., H<sub>2</sub>, NH<sub>3</sub>)

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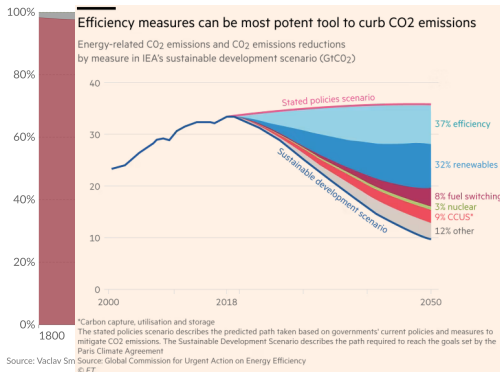
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Our World  
in Data

Modern biofuels  
Other renewables  
Solar  
Wind  
Hydropower  
Nuclear  
Gas

Oil

Coal

Traditional biomass

ng/energy • CC BY

## Take aways

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Push for efficiency through...

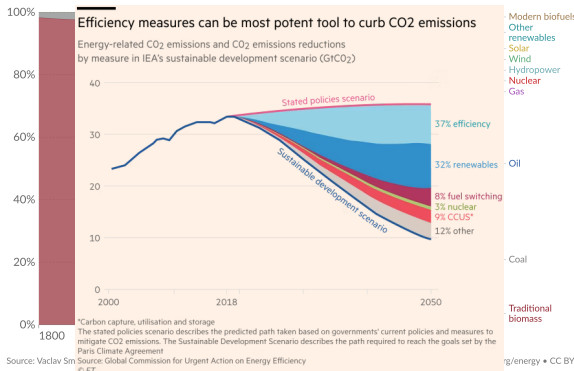
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# Is the future electric?

# Why combustion?

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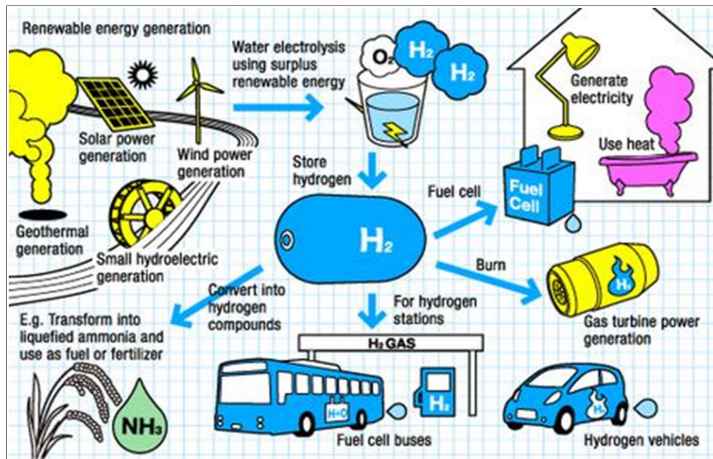
- Low-carbon bio-/H<sub>2</sub>-enriched
- Carbon-free (i.e., H<sub>2</sub>, NH<sub>3</sub>)

Is the future electric?  
rather *eclectic*<sup>1</sup>

<sup>1</sup>*adjective*. deriving ideas, style, or taste from a broad and diverse range of sources.

# Carbon-free combustion

Support the development of a **H<sub>2</sub> economy** to enable the global energy transition



Source : P.I. Jimenez-Calvo (2019) (Ph.D Thesis, Université de Strasbourg, FRA)

# Practical aspects

## Concerns with $H_2$ ?

- Wide flammability limits compared to hydrocarbons
  - In air:  $\%X_{H_2, vol} \sim 4 - 75$ ;  
( $\%X_{C_6H_{14}, vol} \sim 1.05 - 6.7$ ,  $\%X_{C_7H_{16}, vol} \sim 1.1 - 7.5$ ,  $\%X_{Jet-A, vol} \sim 0.6 - 4.9$ )
- Low ignition energy
  - In air:  $H_2 \sim 0.016 \text{ mJ @ } 28\%$ ;  
( $C_6H_{14} / C_7H_{16} \sim 0.24 \text{ mJ @ } 3.4\% / 3.8\%$ )
- Light (buoyant) and highly diffusive molecule
  - Difficult to store – as a gas at  $\uparrow p$  (safety); as a liquid at cryogenic conditions (expensive!)
  - Good for storage outdoors, issues with indoor storage / use (i.e. ceilings, tunnels, parking garages)



**Production** (electrolyzers)



**Storage** (Composite tanks)



**Handling** (General public)



# Accidental combustion events - safety



**Aircraft**



**Nuclear**



**Chemical**



**Mining**

# Accidental combustion events - safety

Large scale destruction + losses of lives +  
environmental impact



**Aircraft**



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**Mining**

# Accidental combustion events - safety

Large scale destruction + losses of lives +  
environmental impact

How to prevent these events?



Aircraft



Nuclear



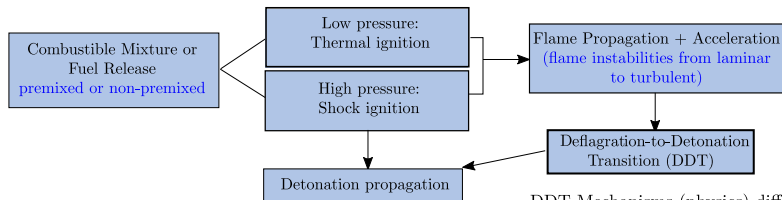
Chemical



Mining

# Accidental combustion events - research interests (so far)

## The big picture - typical accident scenario



+ Safety aspects

+ Harness high rate of energy release

DDT Mechanisms (physics) differ based on configuration

+ Smooth channels ( $h \sim \mathcal{O}(\delta)$ )

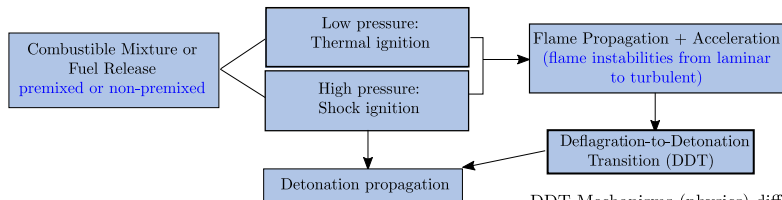
- Shock induced (between shock-flame)
- Shock-/flame-boundary layer interactions

+ Obstacle laden channels

- Shock-induced (upon reflection from obstacles)

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Courrières (1904)



Buncefield (2005)



Beyrouth (2020)



# Combustion 101 (1/4)

Reacting flow =

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fluid mechanics + heat/mass transfer +  
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But... how do we make sense of it? with Continuum Mechanics

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**Reacting flow =**  
**fluid mechanics + heat/mass transfer +**  
**thermodynamics + chemistry**

**But... how do we make sense of it?** with Continuum Mechanics

**Mathematical Description of Nature (AKA Conservation laws)**

$$\partial_t \rho + \nabla \cdot (\rho \mathbf{u}) = 0 \text{ (Mass)}$$

$$\partial_t (\rho \mathbf{u}) + \nabla \cdot (\rho \mathbf{u} \mathbf{u}) = -\nabla p + \nabla \cdot \boldsymbol{\tau} \text{ (Momentum)}$$

$$\partial_t (\rho Y_k) + \nabla \cdot (\rho \mathbf{u} Y_k) = -\nabla \cdot \mathbf{j}_k + \dot{\omega}_k \text{ (Species)}$$

$$\partial_t (\rho e_t) + \nabla \cdot (\rho \mathbf{u} (e_t + p)) = -\nabla \cdot \mathbf{j}_q \text{ (Energy)}$$

$$\text{with } e_t = \sum_{k=1}^N h_k Y_k - p/\rho + \frac{1}{2} \mathbf{u} \cdot \mathbf{u}; \quad \boldsymbol{\tau} = \mu(\nabla \mathbf{u} + \nabla \mathbf{u}^T) - \frac{2}{3} \mu(\nabla \cdot \mathbf{u}) \mathbf{I}$$

# Combustion 101 (2/4)

## Experimental and numerical challenges in reacting flow

### Wide range of temporal and spatial scales involved

- Size of experimental apparatus -  $\mathcal{O}(\text{m})$
- Hydrodynamic/thermal BL thickness -  $\mathcal{O}(\mu\text{m}) - \mathcal{O}(\text{mm})$
- Chemical induction/ignition times -  $\mathcal{O}(\text{s})/\mathcal{O}(\text{ms})$
- Induction length and flame thickness -  $\mathcal{O}(\mu\text{m})$

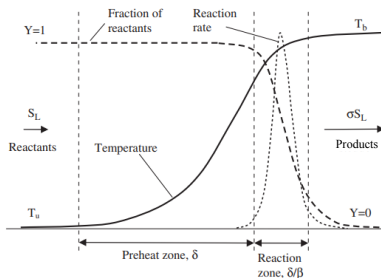
### Size of detailed chemical kinetic mechanisms

- Hydrocarbons commonly used for transportation

Fuel	Reactions	Species
<i>n</i> -hexane ( <i>n</i> -C <sub>6</sub> H <sub>14</sub> )	2271	508
ethylene (C <sub>2</sub> H <sub>4</sub> )	1016	169
hydrogen (H <sub>2</sub> )	21	9

# Combustion 101 (3/4)

## Deflagrations/Flames



Propagation physics

heat/mass diffusion

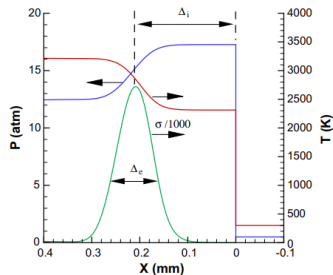
Across interface

$\rho \downarrow, p \sim \text{cte}$

Steady speed

$S_L \sim \mathcal{O}(\text{m/s})$

## Detonations



Propagation physics

shock-induced ignition

Across interface

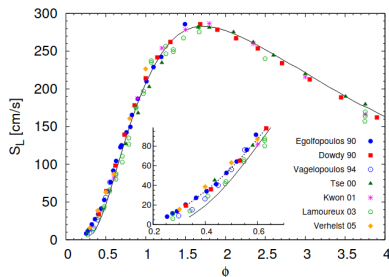
$\rho \uparrow, p, \uparrow$

Steady speed

$D_{CJ} \sim \mathcal{O}(\text{km/s})$

# Combustion 101 (4/4)

## Deflagrations/Flames



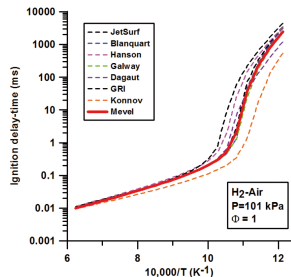
Propagation physics

heat/mass diffusion

Metric of interest

laminar burning velocity,  $s_L$

## Detonations



Propagation physics

shock-induced ignition

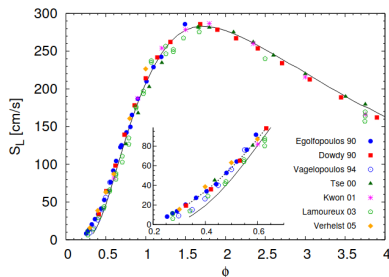
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Ignition delay time,  $\tau_{ign}$

(Effective activation energy,  $E_a/R_u T_{ref}$ )

# Combustion 101 (4/4)

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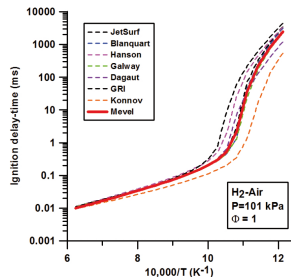
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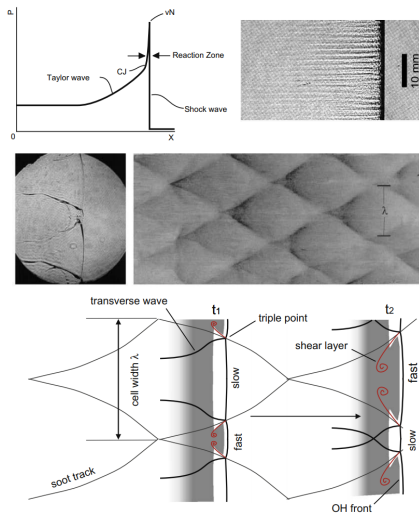
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**Fundamental properties - both experimentally determined**

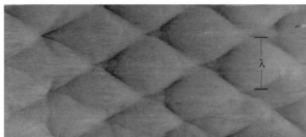
# Detonation fundamentals<sup>2</sup> (1/4)



<sup>2</sup>Shepherd, J. E. (2009). Detonation in gases. Proc. Combustion Inst., 32(1), 83-98.

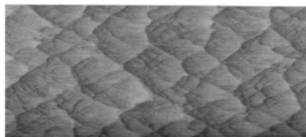
# Detonation fundamentals (2/4)

$\lambda$  is used to classify detonations



Regular

( $\downarrow E_a/R_u T_{vN}$ )



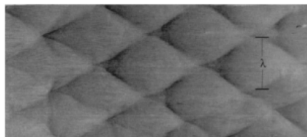
Irregular

( $\uparrow E_a/R_u T_{vN}$ )



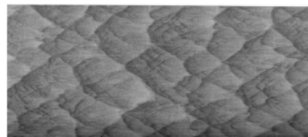
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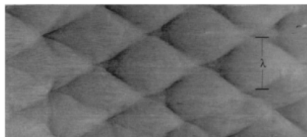
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Unless highly diluted in Ar,  $\lambda$  is not a single well-defined quantity!

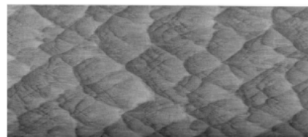
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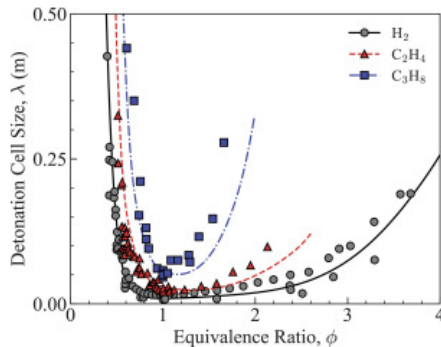
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Unless highly diluted in Ar,  $\lambda$  is not a single well-defined quantity!

$\lambda$  is a function of the chemistry ( $E_a/R_u T_{vN}$ ), i.e.,  $\phi$ ,  $p_0$ ,  $T_0$

# Detonation fundamentals (3/4)

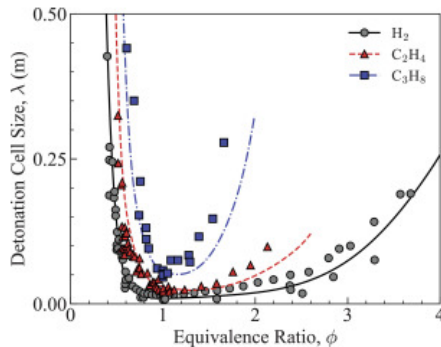


Source : Bauwens, C. R. L., & Dorofeev, S. B. (2020)  
Combustion and Flame, 221, 338-345.

<sup>3</sup> $\lambda \sim 10$  mm ( $H_2$ -Air) /  $\lambda \sim 300$  mm ( $CH_4$ -Air); Conditions:  $p_0 = 100$  kPa and  $\phi = 1$

Source: Caltech's Detonation Database

# Detonation fundamentals (3/4)



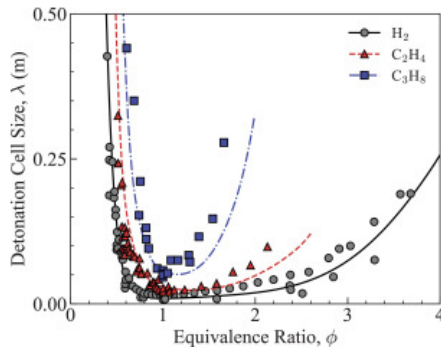
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$\lambda$  useful for explosion hazards & safety evaluations/engineering<sup>3</sup>

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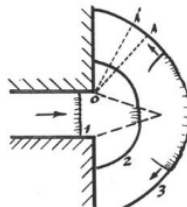
**Limiting behavior (propagation, transmission, re-initiation)  
given as  $f(L/\lambda)$ ;  $L$ : geometrical scale**

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Source: Caltech's Detonation Database

# Detonation fundamentals (4/4)

## Propagation/transmission limits<sup>4</sup>



### Propagation

**Tubes:**  $L = d \sim \lambda/\pi$

**Square channels:**  $L = h > \lambda$

### Transmission

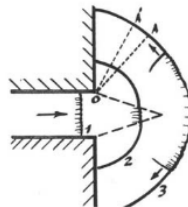
**Tubes:**  $L = d \sim 13\lambda$

**Square channels:**  $L = h > 10\lambda$

<sup>4</sup>Caltech's Detonation Database ([https://shepherd.caltech.edu/detn\\_db/html/db.html](https://shepherd.caltech.edu/detn_db/html/db.html))

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## Propagation/transmission limits<sup>4</sup>



### Propagation

**Tubes:**  $L = d \sim \lambda/\pi$

**Square channels:**  $L = h > \lambda$

### Transmission

**Tubes:**  $L = d \sim 13\lambda$

**Square channels:**  $L = h > 10\lambda$

Depends on mixture type *regular* vs. *irregular* and BCs

(Reported values as high as  $40\lambda$  and as low as  $3\lambda$ )

<sup>4</sup>Caltech's Detonation Database ([https://shepherd.caltech.edu/detn\\_db/html/db.html](https://shepherd.caltech.edu/detn_db/html/db.html))

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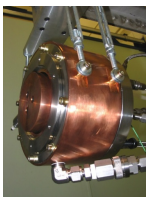
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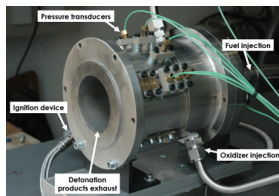
# Non-ideal detonation propagation

# Transportation - detonation in propulsion (1/2)

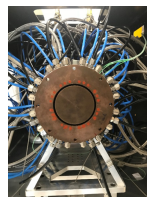
## Rotating Detonation Engines Research at *l'Institut Pprime*<sup>5</sup>



Canteins (2006)



Hansmetzger (2018)



Zitoun (2019)

**Working on detonative propulsion since 1996 (PDE and RDE)**  
(mostly on applied studies of feasibility)

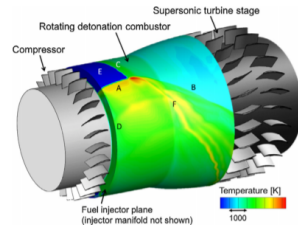
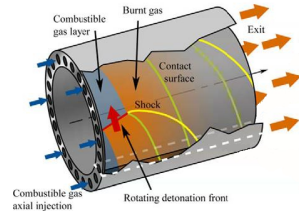
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<sup>5</sup>Detonation team works mostly on fundamental (exp., num., theor.) studies on detonation and deflagration dynamics, and  $\uparrow p / \uparrow T$  constitutive relations

# Transportation - detonation in propulsion (2/2)

## Rotating Detonation Engines (RDE)

- Injection at the bottom-end
- Detonation propagation along the circumference
- Burned gases at  $\uparrow p \rightarrow$  thrust



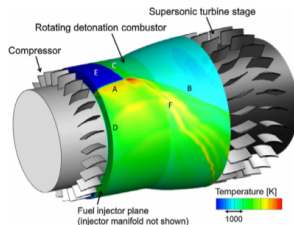
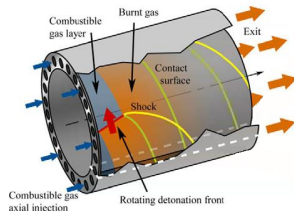
# Transportation - detonation in propulsion (2/2)

## Rotating Detonation Engines (RDE)

- Injection at the bottom-end
- Detonation propagation along the circumference
- Burned gases at  $\uparrow p \rightarrow$  thrust

### Key issue - highly non-ideal flow with

- Mixing with fuel/burned gases
- 3-D effects
- Discrete injection at high pressure
- Confinement by burned/inert gases
- Chamber curvature
- Propagation in narrow spaces



# Overarching goal

## Fundamental understanding of non-ideal detonation propagation

### How?

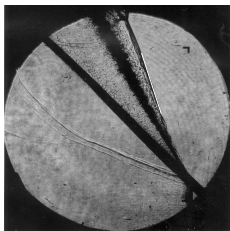
- Through careful experimental and numerical efforts
- Analysis of canonical configurations, i.e., isolating individual effects

### Questions

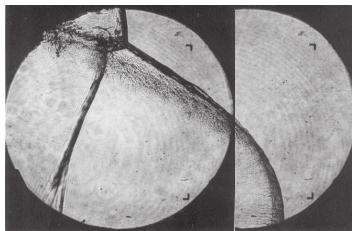
- Can we predict experimental quenching limits?
- Can we reproduce the experimentally observed transmission and propagation dynamics?

# Background - sharp vs. diffuse interfaces

## Flow fields upon interaction - schlieren images<sup>6</sup>



Sharp interface  
 $\lambda \gg \delta$



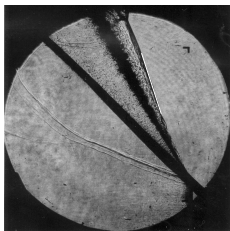
Diffuse interface  
 $\lambda \ll \delta$  or  $\lambda \sim \delta$

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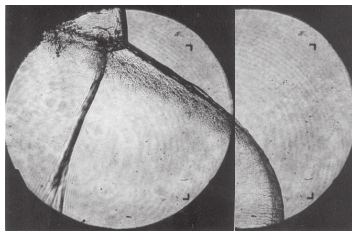
<sup>6</sup>Lieberman, D. (2006). Detonation interaction with sharp and diffuse interfaces. *Doctoral Dissertation*. California Institute of Technology.

# Background - sharp vs. diffuse interfaces

## Flow fields upon interaction - schlieren images<sup>6</sup>



Sharp interface  
 $\lambda \gg \delta$



Diffuse interface  
 $\lambda \ll \delta$  or  $\lambda \sim \delta$

**Diffuse interfaces more likely upon accidental fuel leaks!**

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<sup>6</sup>Lieberman, D. (2006). Detonation interaction with sharp and diffuse interfaces. *Doctoral Dissertation*. California Institute of Technology.

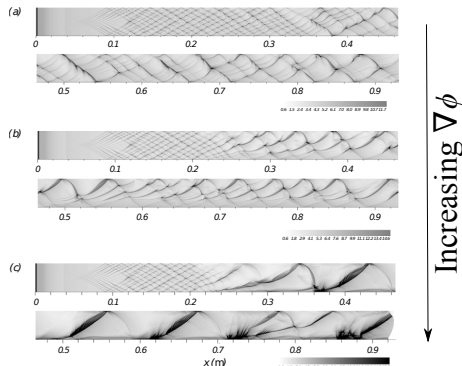
# Background - challenges

## with using $\lambda$ to characterize behavior

- Difficult to measure experimentally within layers/interfaces
- $\lambda$  not uniquely defined even in the absence of gradients
- Properly capturing  $\lambda$  variation in the interface,  $\delta$ ?
- Need to resolve the detonation front!

## with inviscid models

- Lack of energy dissipation mechanisms/diffusive processes
- Not adequate for highly unstable mixtures (i.e. moderate to high  $E_a$ )
- Solutions do not converge with resolution



Han, W. et al. (2019). JFM, 865, 602-649.



# Detonation-diffuse interface interaction

$\Delta\lambda_{\text{crit}}$  for quenching<sup>7</sup>

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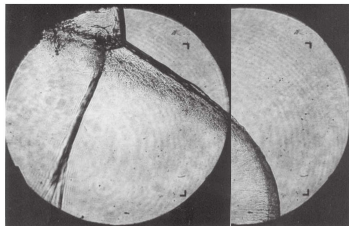
<sup>7</sup>**Melguizo-Gavilanes, J.**, Peswani, M., & Maxwell, B. M. (2021). Detonation-diffuse interface interactions: failure, re-initiation and propagation limits. Proceedings of the Combustion Institute, 38(3), 3717-3724.

# Goal of the study

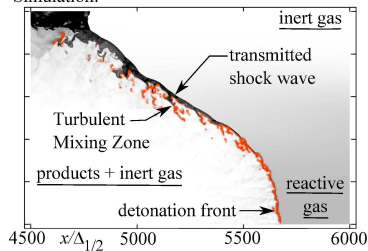
## Objective

To examine failure/re-initiation mechanisms for detonation-diffuse interface<sup>8</sup> interactions, and determine critical cell size gradients,  $\nabla \lambda_{\text{crit}}$ , for quenching

Experiment (Lieberman, 2006):



Simulation:



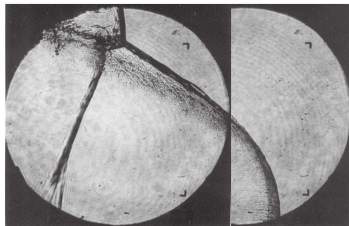
<sup>8</sup>Interface,  $\delta$ , is **diffuse** if  $\lambda \ll \delta$  or  $\lambda \sim \delta$

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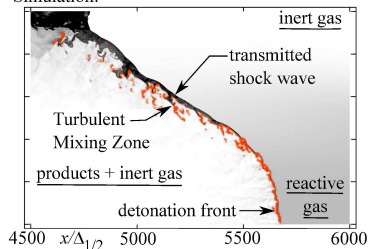
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## How?

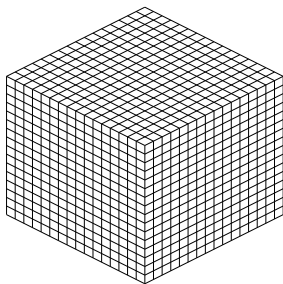
- Numerical simulations using the CLEM-LES methodology

<sup>8</sup>Interface,  $\delta$ , is **diffuse** if  $\lambda \ll \delta$  or  $\lambda \sim \delta$

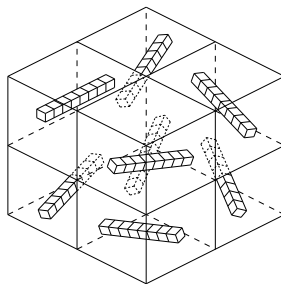
# Physical model - proposed methodology

## Compressible Linear Eddy Model (CLEM)

- Grid within a grid approach based on the Linear Eddy Model (LEM)<sup>9</sup> - reformulated for compressible flows
- Reduce small scales to 1-D diffusion/reaction problem
- Validated for premixed detonations in channels<sup>10</sup> and DDT<sup>11</sup>



VS



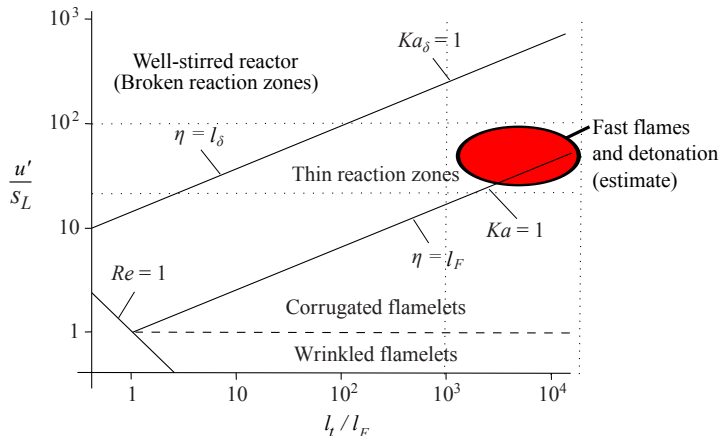
<sup>9</sup>S. Menon and A. R. Kerstein (2011) Turbulent Combustion Modeling: Advances, New Trends and Perspectives, Springer, 2011, Ch. 10: The Linear-Eddy Model, pp. 221-247.

<sup>10</sup>Maxwell, B. et al. (2017). JFM, 818, 646-696.

<sup>11</sup>Maxwell, B. et al (2018). CNF, 192, 340-357.

# Physical model - detonation combustion regimes

## Borghi-Peters diagram



$$\frac{u'}{S_L} = \frac{\text{turbulence intensity}}{\text{laminar burning velocity}}$$

$$\frac{l_t}{l_F} = \frac{\text{turbulence macroscale}}{\text{reaction zone thickness}}$$

# Physical model - LES formulation

## On the large scales

$$\frac{\partial \bar{\rho}}{\partial t} + \nabla \cdot (\bar{\rho} \tilde{\mathbf{u}}) = 0 \quad (\text{Mass})$$

$$\frac{\partial (\bar{\rho} \tilde{\mathbf{u}})}{\partial t} + \nabla \cdot (\bar{\rho} \tilde{\mathbf{u}} \otimes \tilde{\mathbf{u}}) + \nabla \bar{p} - \nabla \cdot \bar{\rho}(\nu + \nu_t) \underline{\mathbf{S}} = 0 \quad (\text{Momentum})$$

$$\frac{\partial (\bar{\rho} \tilde{e})}{\partial t} + \nabla \cdot \left( (\bar{\rho} \tilde{e} + \bar{p}) \tilde{\mathbf{u}} - \tilde{\mathbf{u}} \cdot \tilde{\underline{\tau}} \right) - \left( \frac{\gamma}{\gamma - 1} \right) \nabla \cdot \left( \bar{\rho} \left( \frac{\nu}{P_r} + \frac{\nu_t}{P_{r,t}} \right) \nabla \tilde{T} \right) = -Q \bar{\omega} \quad (\text{Energy})$$

with

$$\tilde{e} = \frac{\bar{p}}{\bar{\rho}(\gamma - 1)} + \frac{1}{2}(\tilde{\mathbf{u}} \cdot \tilde{\mathbf{u}}) + k^{sgs} \quad \text{and} \quad \bar{p} = \bar{\rho} \tilde{T}$$

## Momentum closure

$$\frac{\partial (\bar{\rho} k^{sgs})}{\partial t} + \nabla \cdot (\bar{\rho} \tilde{\mathbf{u}} k^{sgs}) - \nabla \cdot \left( \frac{\bar{\rho} \nu_t}{P_{r,t}} \nabla k^{sgs} \right) = \underbrace{\bar{\rho} \nu_t \underline{\mathbf{S}} \cdot (\nabla \tilde{\mathbf{u}})}_{\text{production rate}} - \underbrace{\bar{\rho} \epsilon}_{\text{dissipation rate}} \quad (\text{subgrid KE})$$

where

$$\nu_t = \frac{1}{\pi} \left( \frac{2}{3C_\kappa} \right)^{3/2} \sqrt{k^{sgs}} \bar{\Delta} \quad \text{and} \quad \epsilon = \pi \left( \frac{2}{3C_\kappa} \right)^{3/2} (k^{sgs})^{3/2} / \bar{\Delta}$$

# Physical model - CLEM formulation

## Reaction rate closure on the small scales

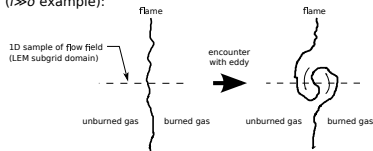
$$\rho \frac{DT}{Dt} = \left( \frac{\gamma - 1}{\gamma} \right) \dot{p} + \rho \frac{\partial}{\partial m} \left( \rho \alpha \frac{\partial T}{\partial m} \right) - \left( \frac{\gamma - 1}{\gamma} \right) Q \dot{\omega} + \dot{F}_T \text{ (Enthalpy)}$$

$$\rho \frac{DY}{Dt} = \rho \frac{\partial}{\partial m} \left( \rho \frac{\alpha}{Le} \frac{\partial Y}{\partial m} \right) + \dot{\omega} + \dot{F}_Y \text{ (Reactant mass fraction)}$$

where  $\dot{\omega} = -\rho A Y \exp(E_a/T)$ ;  $m(x, t) = \int_{x_o}^x \rho(x, t) dx$ ;  $D_T = f(k^{sgs}) = f(C_\kappa)$

## Turbulent stirring

Effect of eddies on flow field  
( $l \gg \delta$  example):



Equivalent 1-D domain  
temperature profile:



# Challenges and physical model recap

## Challenges

- Interest in industrially relevant scales
- $\lambda$  not uniquely defined even in absence of reactivity gradients!

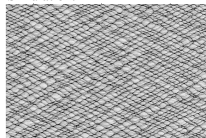
## Physical model

- LES-filtered Navier-Stokes for a reactive, calorically perfect gas
- 1-step Arrhenius kinetics (closure of  $\bar{\omega}$  through CLEM subgrid modeling)

## Model calibration

- $2.5\text{C}_2\text{H}_4 + 3\text{O}_2$  at  $p_0 = 11$  kPa and  $T_0 = 300$  K (moderately unstable)<sup>12</sup>
- Kinetic and transport parameters fitted at vN-state (i.e.,  $\tau_{\text{ind}}$ ,  $\Delta_{1/2}$ );  $s_L$  at postshock state for  $M_s = 0.5M_{\text{CJ}}$
- $\nu_t$  and  $\epsilon$  are  $f(C_k, \bar{\Delta}, k^{sgs})$ ; ( $C_k$  and  $\bar{\Delta}$  calibrated to reproduce  $\lambda_{\text{exp}}$ <sup>13</sup>)

Simulation:



Experiment:



<sup>12</sup>  $E_a/R_u T_{\text{vN}} = 28$ ;  $Q/R_u T_{\text{vN}} = 116$ ;  $\gamma = 1.33$

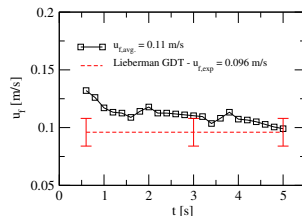
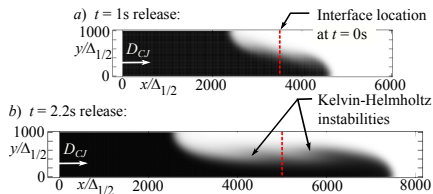
<sup>13</sup>  $\lambda_{\text{exp}} \sim 2$  mm



# Domain, initial and boundary conditions

## 2D simulations carried out in two steps

- **Step 1** : Compute gravity current for a  $2.5\text{C}_2\text{H}_4 + 3\text{O}_2 / \text{N}_2$  interface  $p_0 = 11 \text{ kPa}$  and  $T_0 = 300 \text{ K}$ ;  $L_x \sim 1.0 \times L_y \sim 0.15 \text{ m}$  (5 s/1 m) - **OpenFOAM**
- **Step 2** : Take fields as initial condition, map  $\text{N}_2$  field to mass fraction  $Y = 1 - Y_{\text{N}_2}$ ;  $L_x \sim 0.8 \times L_y \sim 0.1 \text{ m}$  - **non-ideal detonation/CLEM-LES**<sup>14</sup>

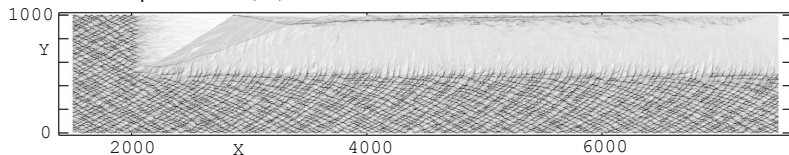


<sup>14</sup>**Resolution:**  $\bar{\Delta}_{\text{LES}} = \Delta_{1/2}/8$ ,  $N = 16$  subgrid elements per cell ( $\bar{\Delta}_{\text{eff}} = \Delta_{1/2}/128$ )  
(Scale: 1 cm =  $100\Delta_{1/2}$ )

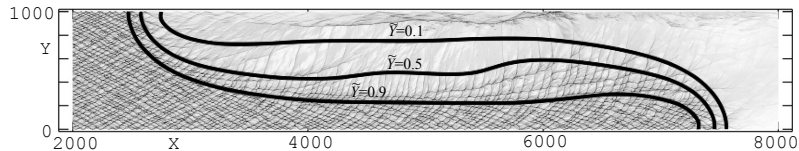
# Results - overall dynamics

## Soot foils

CASE 2: Sharp interface ( $0^\circ$ )



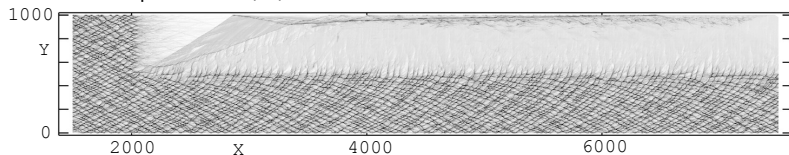
CASE 3: Diffuse interface



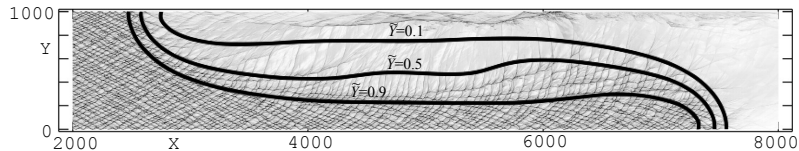
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## Soot foils

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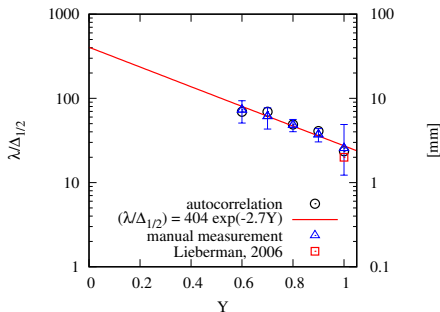
CASE 3: Diffuse interface



Diffuse interface case exhibits quenching and re-initiation in  $\delta$ !

# Results - overall dynamics

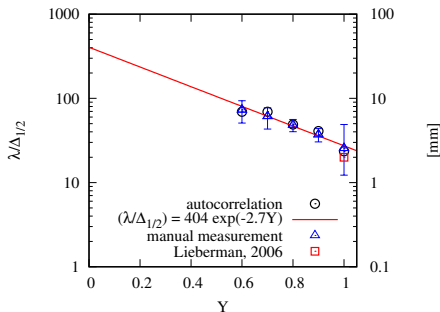
Mapping  $Y$  to  $\lambda$  to capture proper cell size dynamics<sup>15</sup>



<sup>15</sup>Required separate premixed detonation simulations

# Results - overall dynamics

Mapping  $Y$  to  $\lambda$  to capture proper cell size dynamics<sup>15</sup>



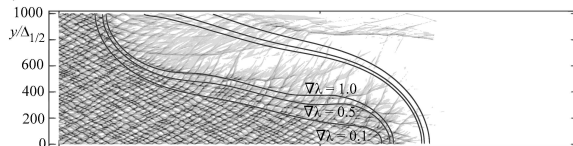
Cell size gradient can be computed via  $\nabla \lambda = (d\lambda/dY)\nabla Y$

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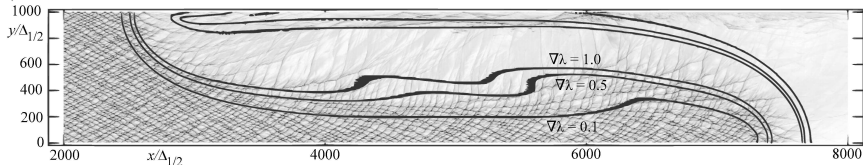
# Results - overall dynamics

## Cell size gradient superimposed on soot foils

a)  $t = 1\text{s}$ :



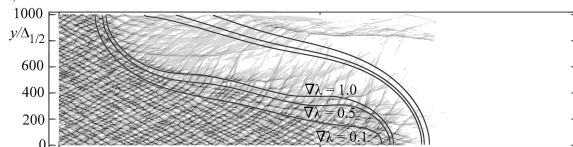
b)  $t = 2.2\text{s}$ :



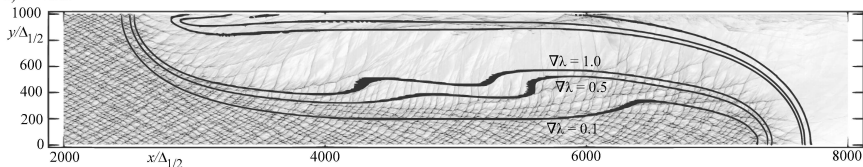
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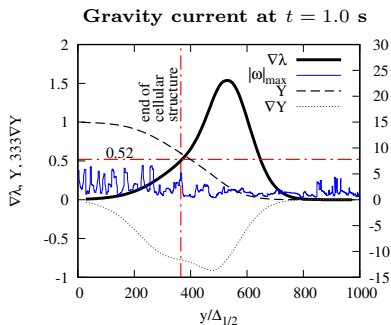
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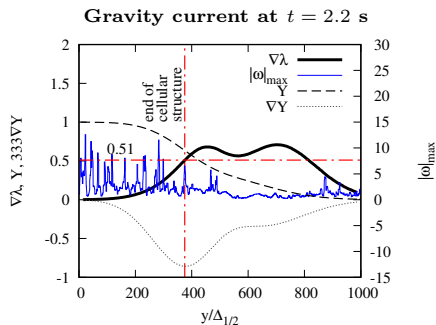
$\overline{\nabla\lambda_{\text{crit}}} \sim 0.5 \rightarrow$  direct consequence of cellular dynamics within the interface

# Results - critical conditions

## Determination of $\nabla\lambda_{\text{crit}}$



$$x = 4000\Delta_{1/2} \text{ (40 cm)}$$

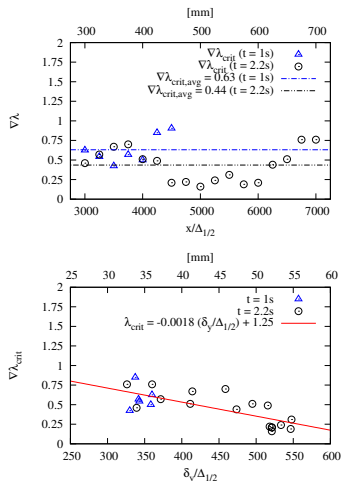


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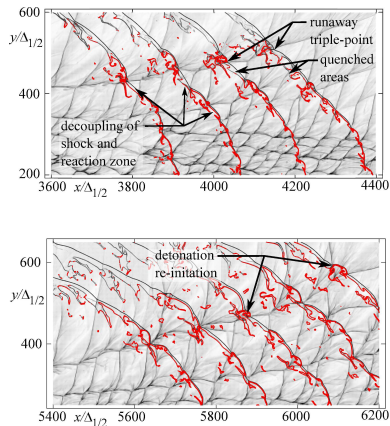
# Results - $\nabla\lambda_{\text{crit}}$ , quenching and re-initiation

## Critical detonation cell size gradient



↑  $\delta$  favors detonation transmission

## Quenching, re-initiation within $\delta$



Triple point transmission characteristic of  
deto-diffuse interface interactions

# Discussion and closing remarks

## Applicability of reported $\nabla\lambda_{\text{crit}}$

- In agreement with previous work -  $\uparrow \delta$  favors detonation transmission

---

<sup>16</sup>Kryuchkov, S. I. et al. (1996). PROCI (Vol. 26, No. 2, pp. 2965-2972);  
Kuznetsov, M. S. et al. (1998). PROCI (Vol. 27, No. 2, pp. 2241-2247)

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- Investigation of more canonical configurations (i.e., constant  $\delta$ )

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- Influence of chemical modeling and 3-D effects on  $\nabla\lambda_{\text{crit}}$ .

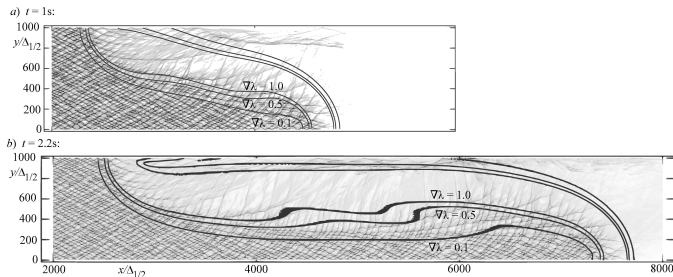
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# Deto-diffuse interface interaction - main take away<sup>17</sup>

Detailed investigation of  $\nabla\lambda_{\text{crit}}$  for quenching at industrially relevant scales using CLEM-LES

## Soot foils for detonation-diffuse interface interaction



**Key result:**  $\overline{\nabla\lambda_{\text{crit}}} \sim 0.5 > 0.1$  (value reported in literature)  $\rightarrow$  direct consequence of cellular dynamics within the interface

<sup>17</sup>Melguizo-Gavilanes, J., Peswani, M., & Maxwell, B. M. (2021). Detonation-diffuse interface interactions: failure, re-initiation and propagation limits. Proceedings of the Combustion Institute, 38(3), 3717-3724.

# Acknowledgments

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**Special thanks to**  
Prof. Dirk Roekaerts and the Dutch Section of the Combustion Institute