

# Machine Learning-based Approaches for the Control of Reacting Flows

Anh Khoa Doan

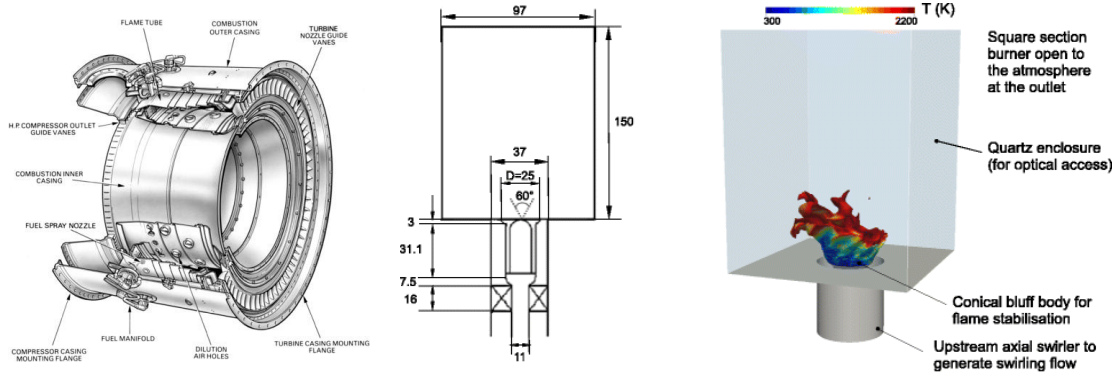
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# Performance and stability of combustor generally guaranteed by *design*

- Geometry and fuel/air conditions: dictates steady flame topology

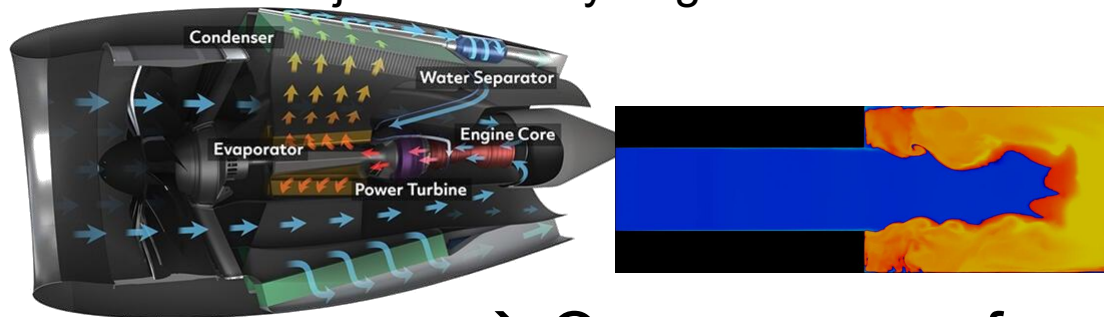


[Soares, Gas Turbines, Butterworth-Heinemann (2008)]  
 [Giusti et al., Flow Turbul. Combust. 97, 1165-1184 (2016)]

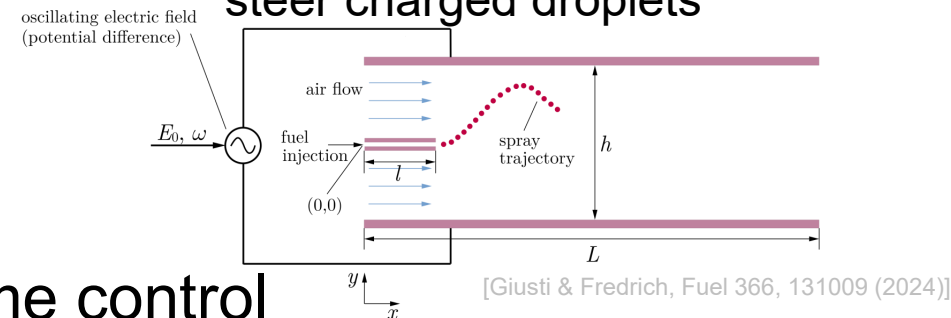
→ Limited operations to narrow fuel/condition ranges  
 → Limited adaptability to out of design operations

- Recent investigations of actuation in combustors

Water/steam injection for hydrogen combustion



Oscillating electric field: able to steer charged droplets



[Giusti & Fredrich, Fuel 366, 131009 (2024)]

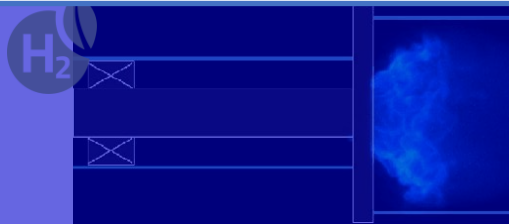
→ Opens avenue for *active* flame control

# Turbulent flames are high-dimensional complex multiphysics dynamical systems

- Turbulent flames
  - Complex chaotic dynamics



Leverage developments in machine learning to develop control framework for flame control



→Flashback



→Blow-off

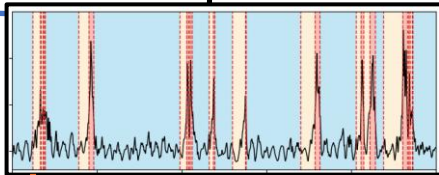
[Zhang et al., Proc. Comb. Inst., 2021]

→ Limited performance of traditional control

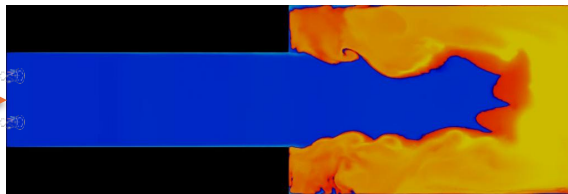
# Structure of the seminar



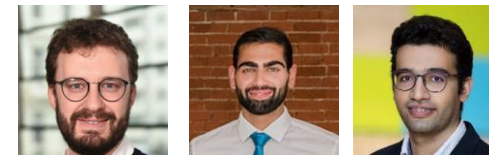
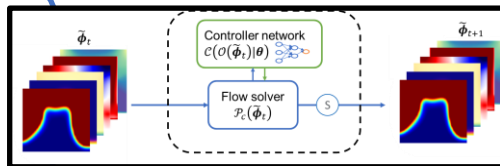
## 1. Machine Learning to prevent flashback with water injection



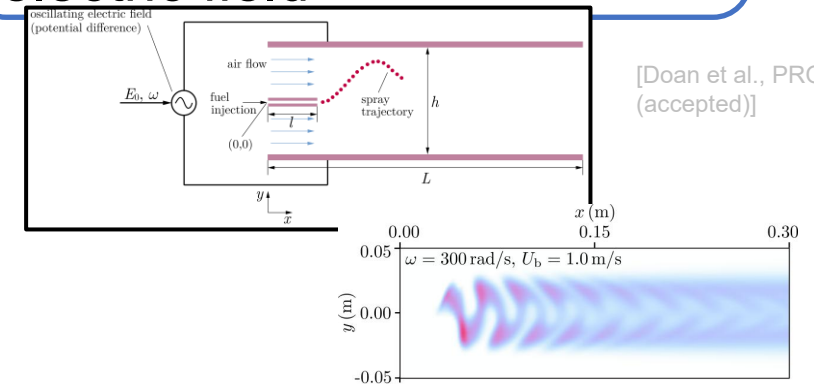
[Floris et al., Proc. Comb. Inst., 2024]  
[Pousouda et al., J. Eng. Gas Turbines Power, 2025]



## 3. Towards unified control development framework with differentiable solver



## 2. Machine Learning to control fuel mixing with electric field



[Doan et al., PROCI, 2026 (accepted)]

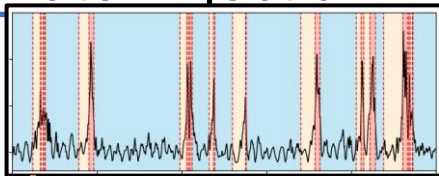


[Tathawadekar et al., Data-centric Eng., 2023]  
[Shehata & Doan, PRFluids, 2026 (under review)]

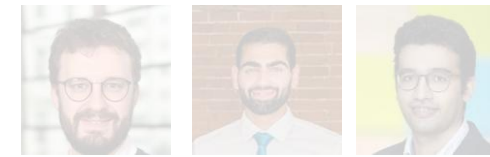
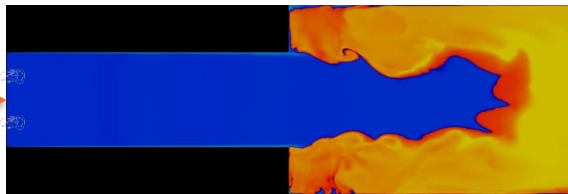
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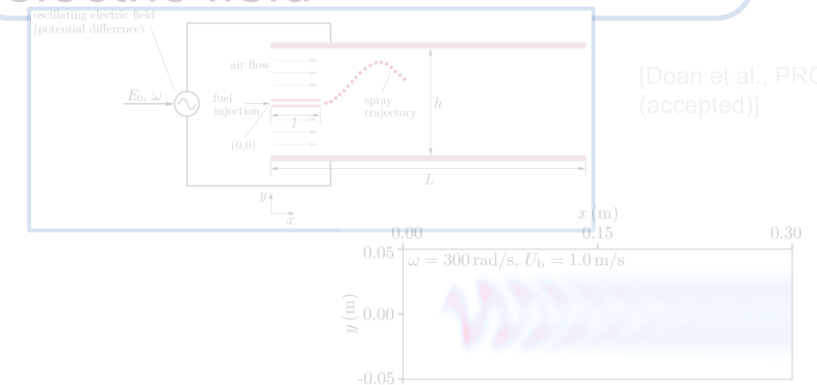
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[Floris et al., Proc. Comb. Inst., 2024]  
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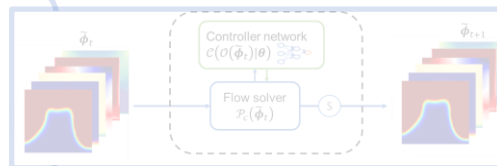


## 2. Machine Learning to control fuel mixing with electric field



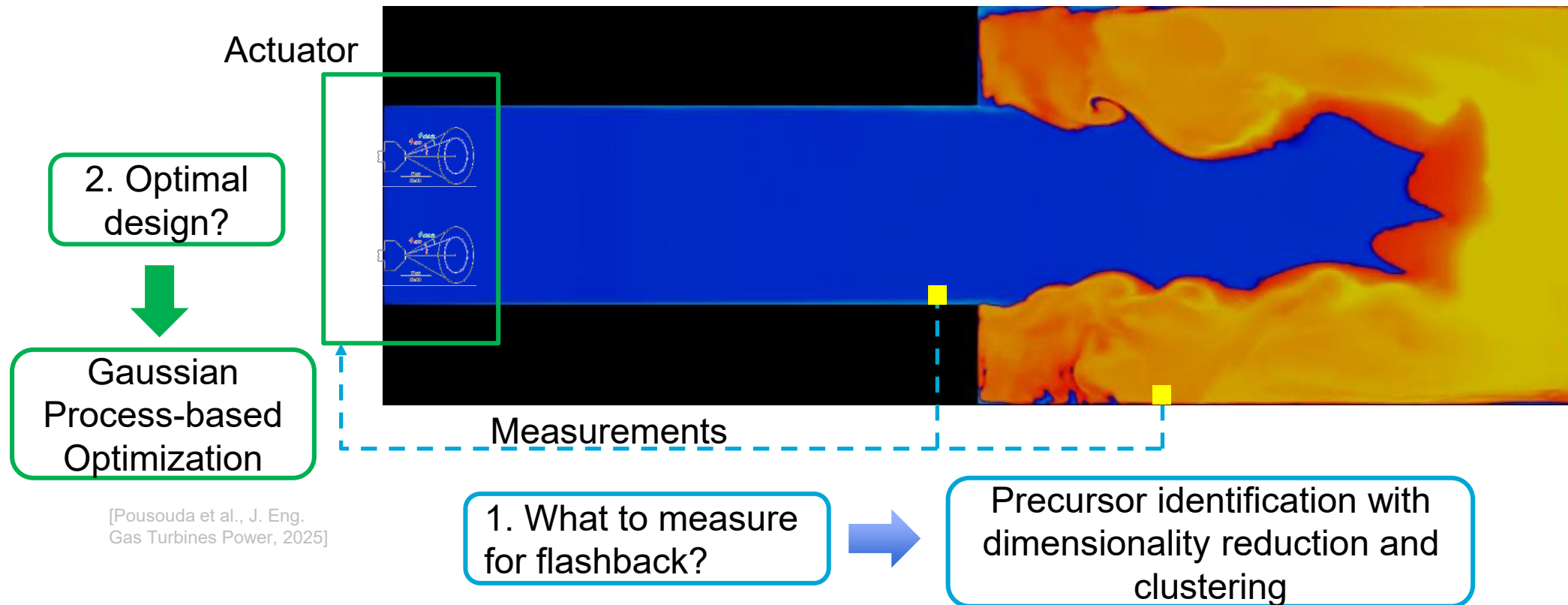
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## 3. Towards unified control development framework with differentiable solver



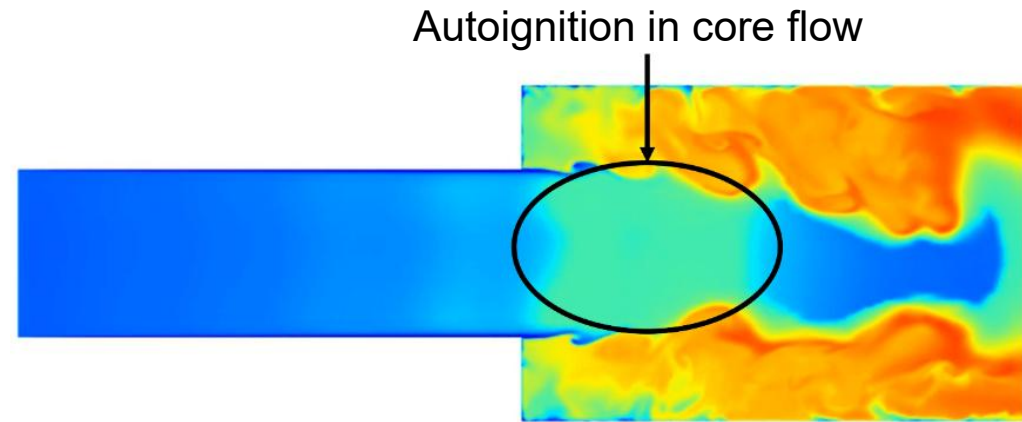
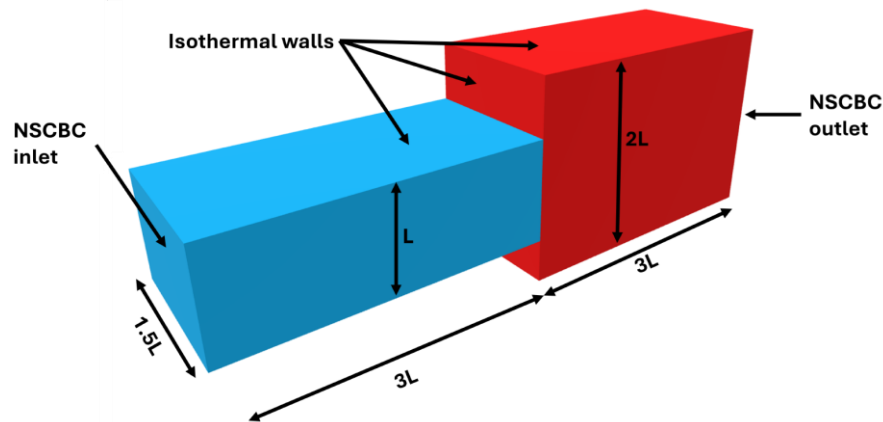
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# Flashback control framework



# Simulation of flashback in hydrogen reheat combustor

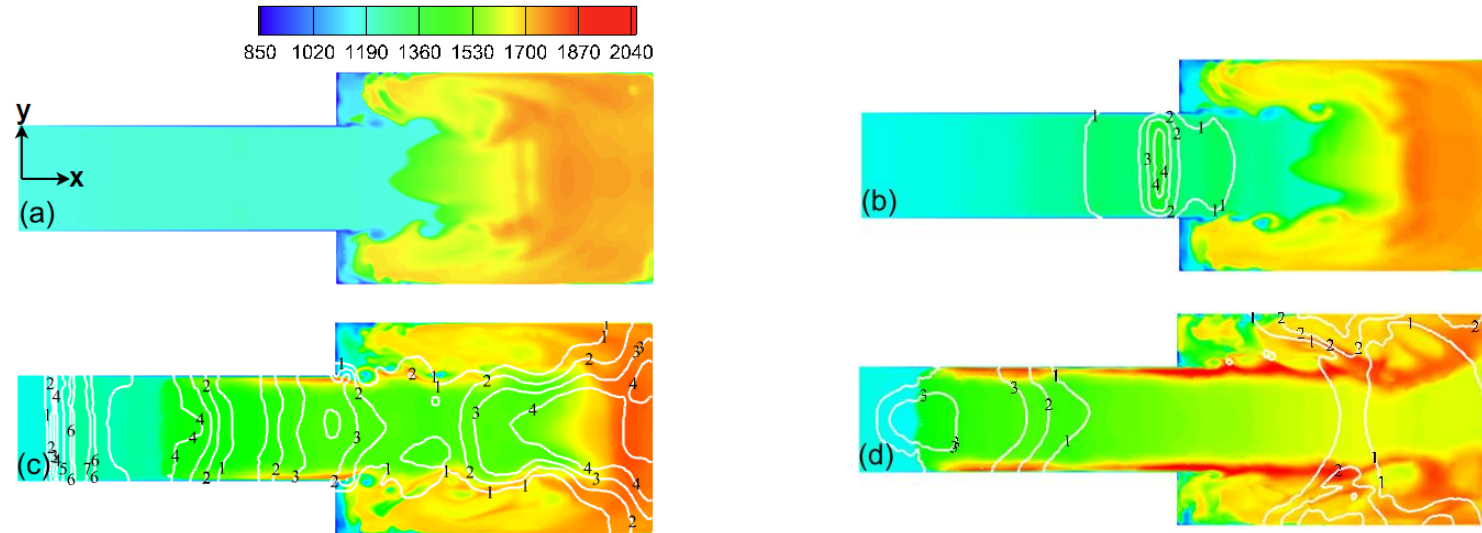
- Simplified model of Ansaldo GT36 reheat combustor
  - Lean hydrogen/air burner with  $\phi = 0.35$ ,  $p = 20$  atm,  $T_{in} = 1180$ K
  - $U_{in} = 200$ m/s
  - Normally stabilized by autoignition



- LES simulation – Converge CFD (thickened flame model, 11-species mechanism)
- Total thermochemical/flow state: 17 features

# Simulation of flashback in hydrogen reheat combustor

- Shows intermittent flashback due to early autoignition



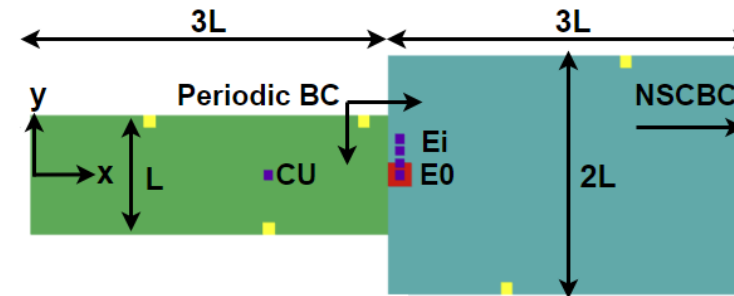
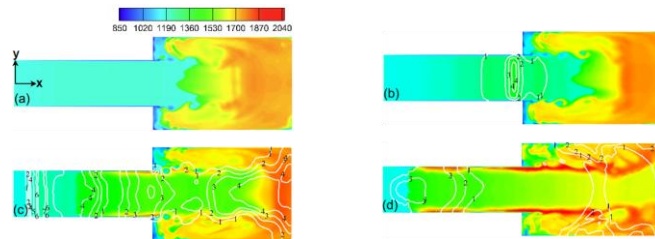
- Then the burner recovers



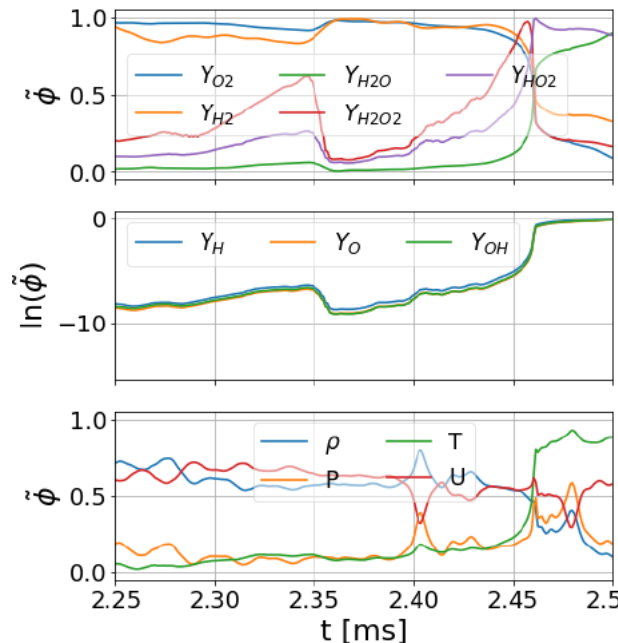
Total time series: 11 flashback events

# Data-driven analysis of hydrogen flashback mechanism

- Collection of thermochemical/flow state evolution



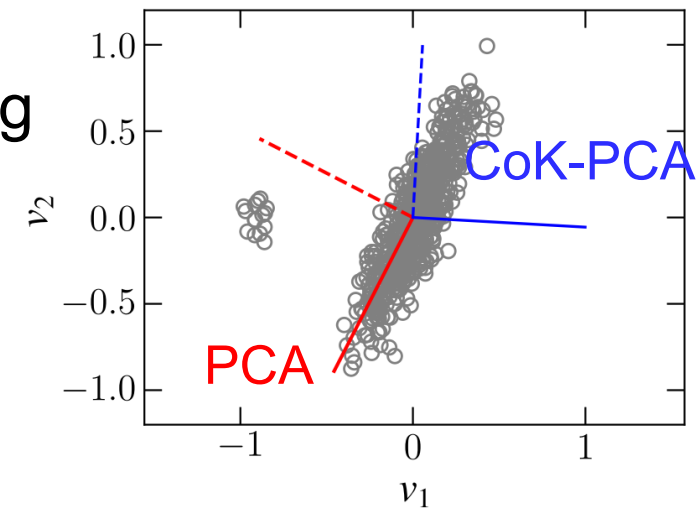
- : sampling locations
- : pressure probe locations
- : co-kurtosis blocks



1. Identification of relevant features for flashback with co-kurtosis PCA  
 → Provides indication of interesting physical features
2. Precursor identification with modularity clustering  
 → Provides precursors

# Co-kurtosis Principal Component Analysis consists in applying PCA on the co-kurtosis tensor

- Objective: identify most relevant features in thermochemical and flow state for flashback precursor
- Co-kurtosis PCA
  - Kurtosis: related to “fat tails”
  - Co-kurtosis: related to features undergoing extreme deviations simultaneously
  - PCA applied on the co-kurtosis tensor: sensitive to outlier apparition (precursor)
  - Can compute the relative contribution of features to the principal vector (feature moment matrix - FMM)

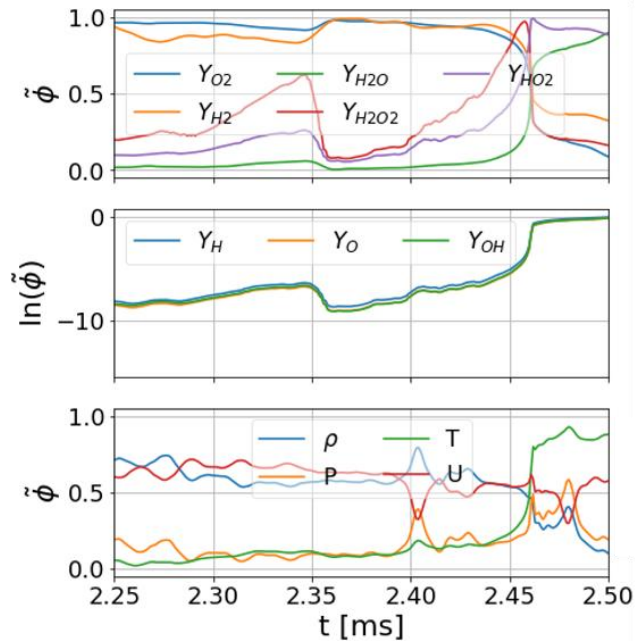


[Jonnalagadda et al., CnF 250, (2023)]

[Nayak et al., CnF 259, (2024)]

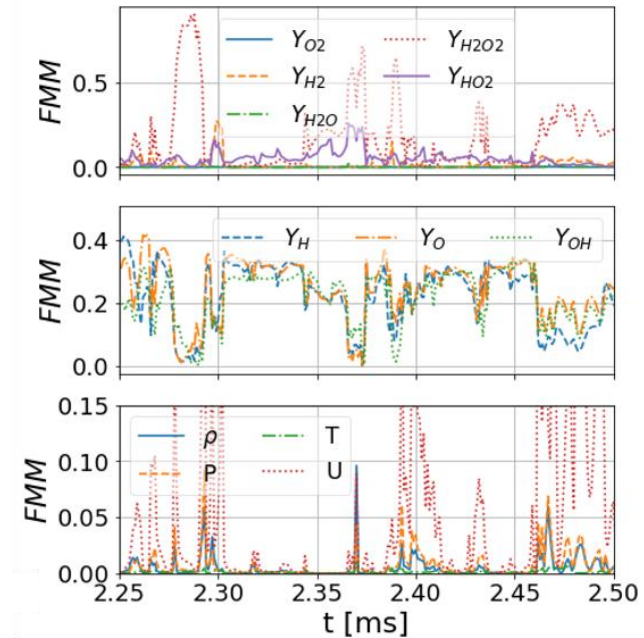
[Aditya et al., JCP 387, (2019)]

# Co-kurtosis PCA on reheat burner allows to identify important features for the onset of flashback



Co-kurtosis PCA

FMM calculation

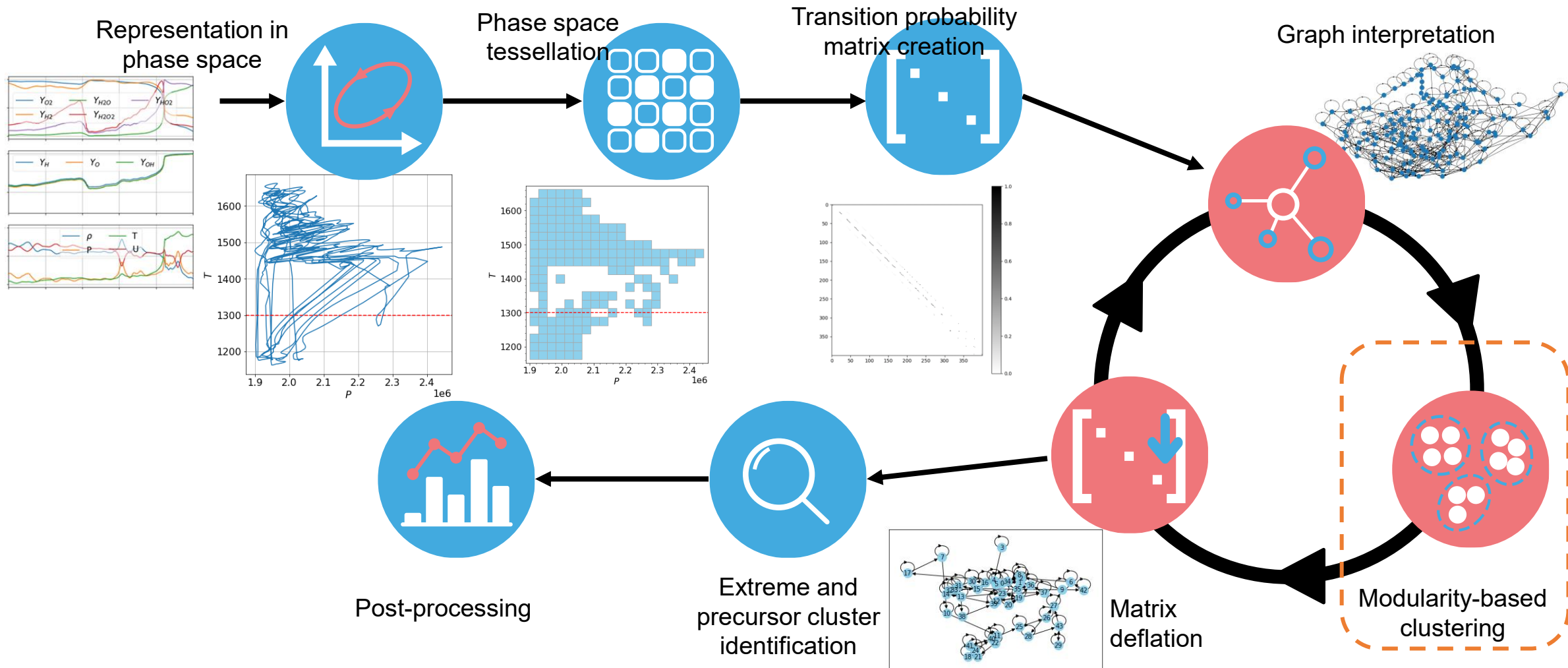


- Identified features:

- $p, \rho, V_x$
- OH, H, O: very similar behaviour  $\rightarrow$  OH kept
- Strong activity from  $HO_2, H_2O_2$
- $T$  also kept

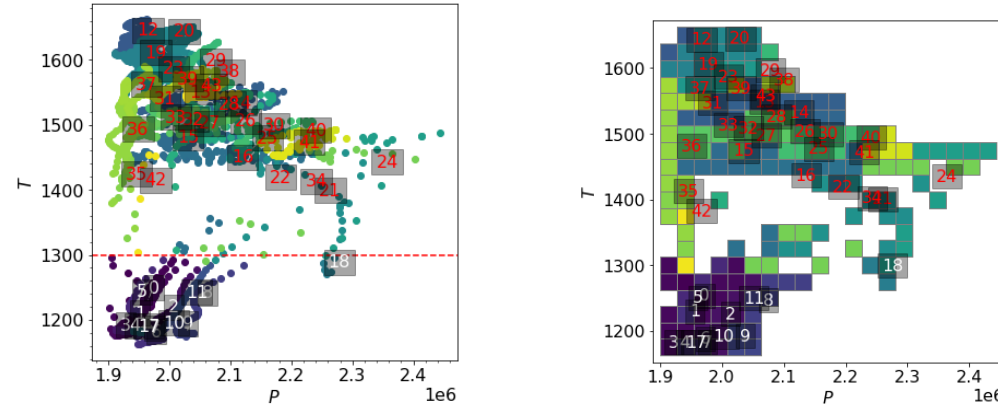
$\rightarrow$  Features reduced from 17 to 7

# Graph and clustering-based precursor identification method

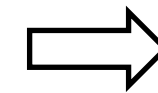
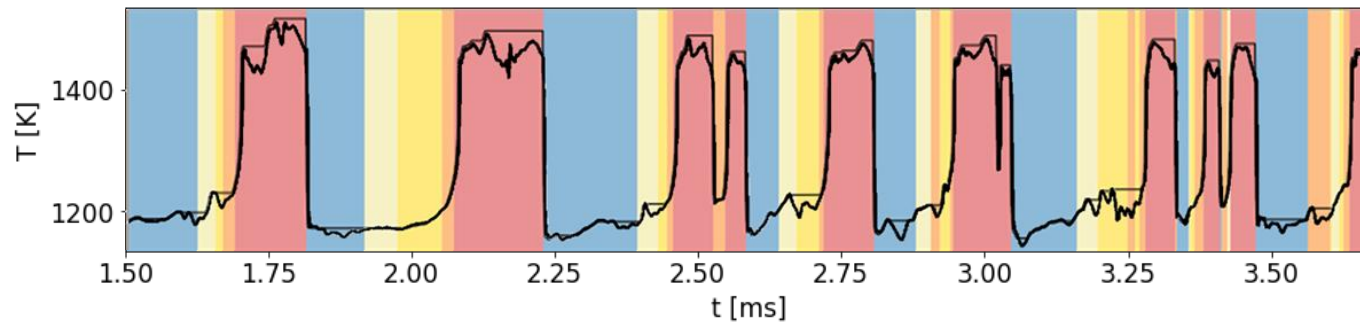


# Identified clusters during flashback provides a flashback prediction horizon

- Clusters based on the first 3 flashback events

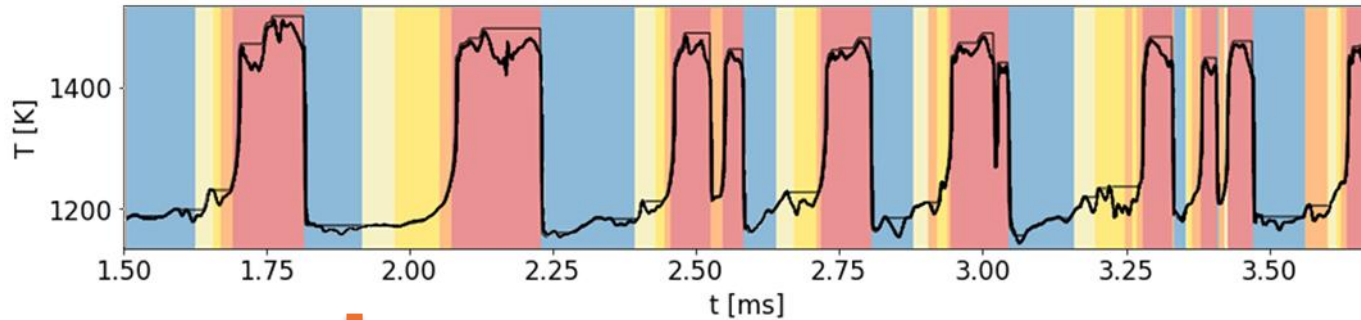


For the remaining flashback

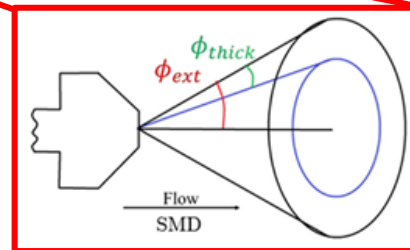
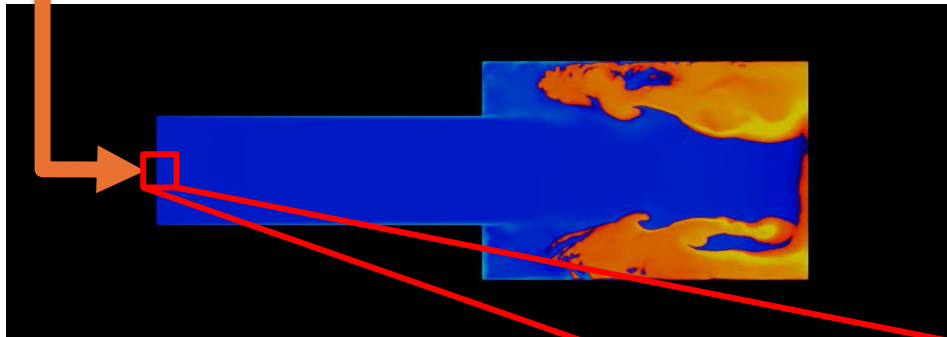


Precursor provide some flashback prediction horizon

# How can we design a flashback mitigation system?



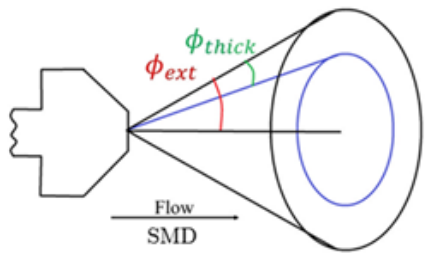
Water injection?



How can we design the water injection optimally?

# Development of a surrogate model to design water-injection to mitigate flashback

4 design variables



Performance parameters:

1. Flashback prevented
2. Thermal efficiency  $\eta_{th}$
3. Evaporation rate  $\eta_{vap}$
4. Pattern factor  $PF$
5. NOx emission  $E_{NO_x}$

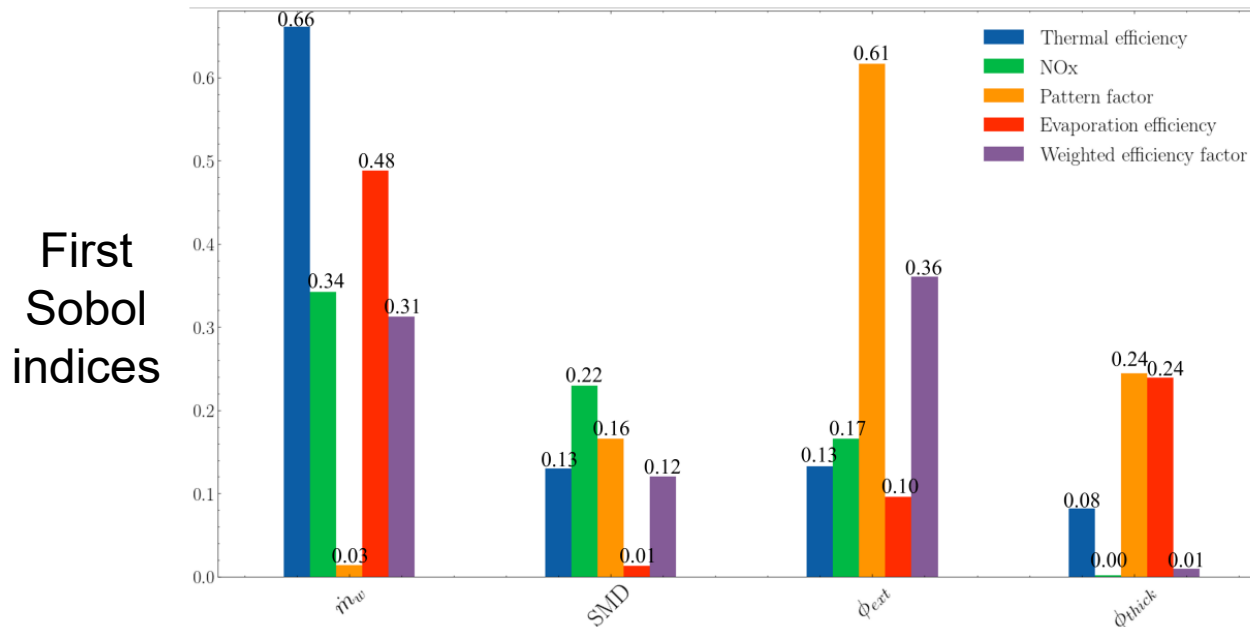
Design of a surrogate model

1. Generate database of 20 simulations
2. Gaussian process regression (one model per performance parameter)
3. Analyse the influence of the design variables based on the surrogate (with Sobol Index)

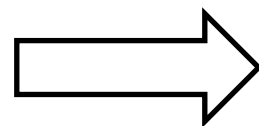
Design parameters	$\dot{m}_w$ ( $\mu\text{g}/\text{ms}$ )	SMD ( $\mu\text{m}$ )	$\phi_{ext}$ (deg)	$\phi_{thick}$ (deg)
Min. values	500	2	20	3
Max. values	15,000	20	55	18
Performance parameters	$\eta_{th}$	$\eta_{vap}$	NO <sub>x</sub>	PF

# Development of a surrogate model to design water-injection to mitigate flashback

Influence of design parameters deduced from surrogate

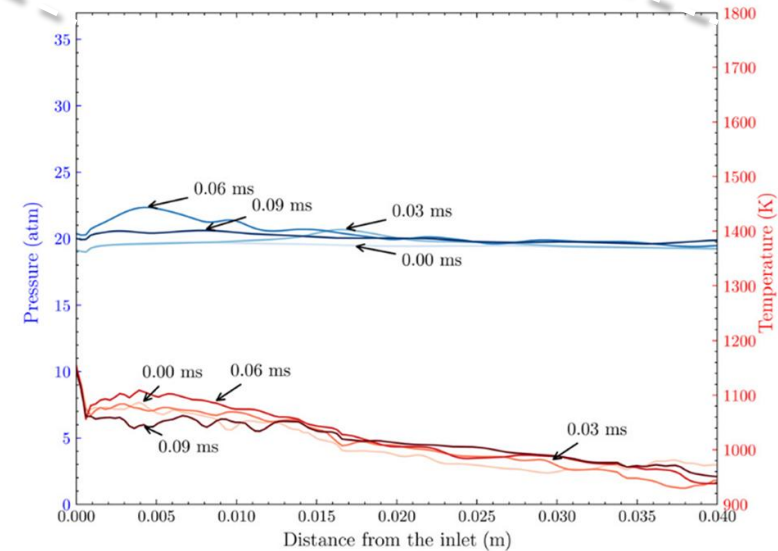
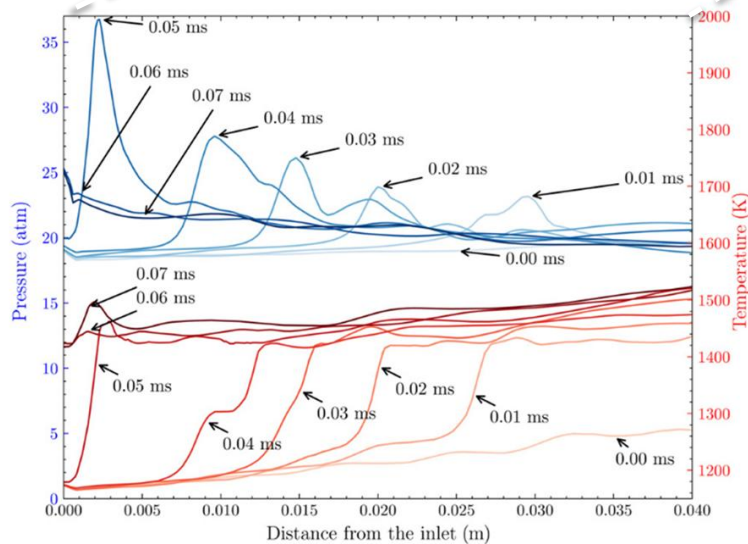
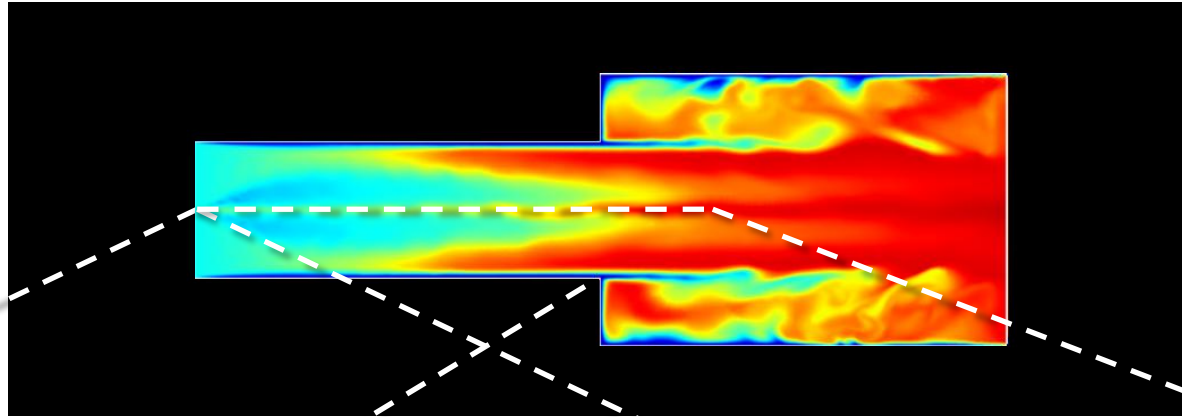


- $\eta_{th}$ : mostly influenced by  $\dot{m}_w$
- $E_{NO_x}$ : joint influence of  $\dot{m}_w$ , SMD and  $\phi_{ext}$
- $PF$ : mostly influenced by droplet distribution through  $\phi_{ext}$  and  $\phi_{thick}$
- $\eta_{vap}$ : mostly influenced by  $\dot{m}_w$  and  $\phi_{thick}$



Surrogate used for design optimization of performance  $\mathcal{L}(\eta_{th}, \eta_{vap}, PF, E_{NO_x})$

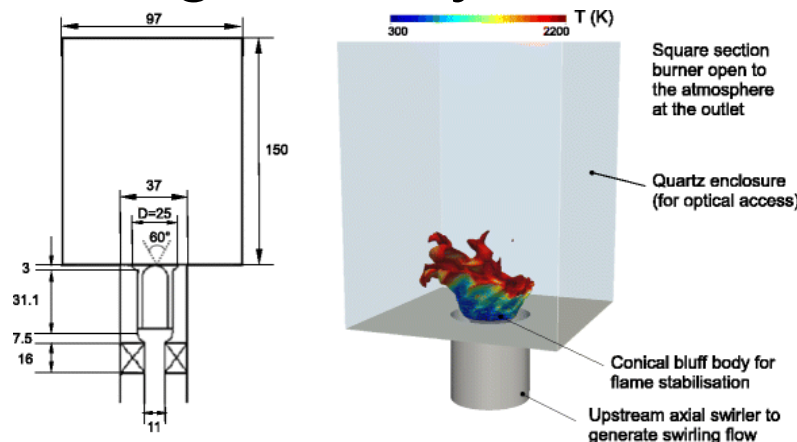
# Designed water injection system prevents flashback





# Fuel stratification control through charged droplet trajectory control

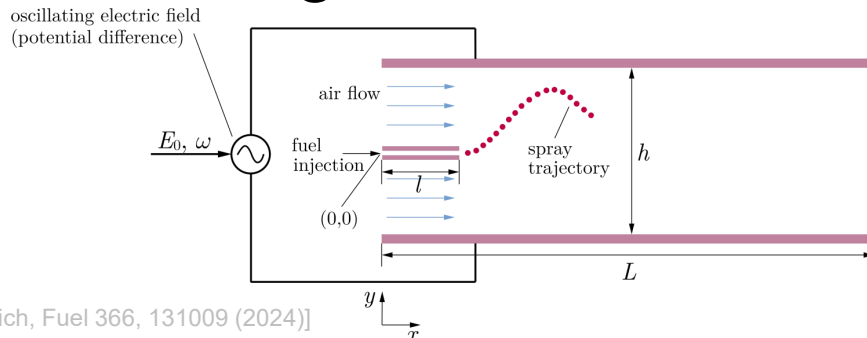
- Fuel-air mixing: constrained by combustor, injector and chamber geometry



[Giusti et al., Flow Turbul. Combust. 97, 1165-1184 (2016)]

→ Designed for specific conditions  
→ Limited operations to narrow fuel/condition ranges

- Oscillating electric field: able to steer charged droplets



→ Potential for fuel stratification control

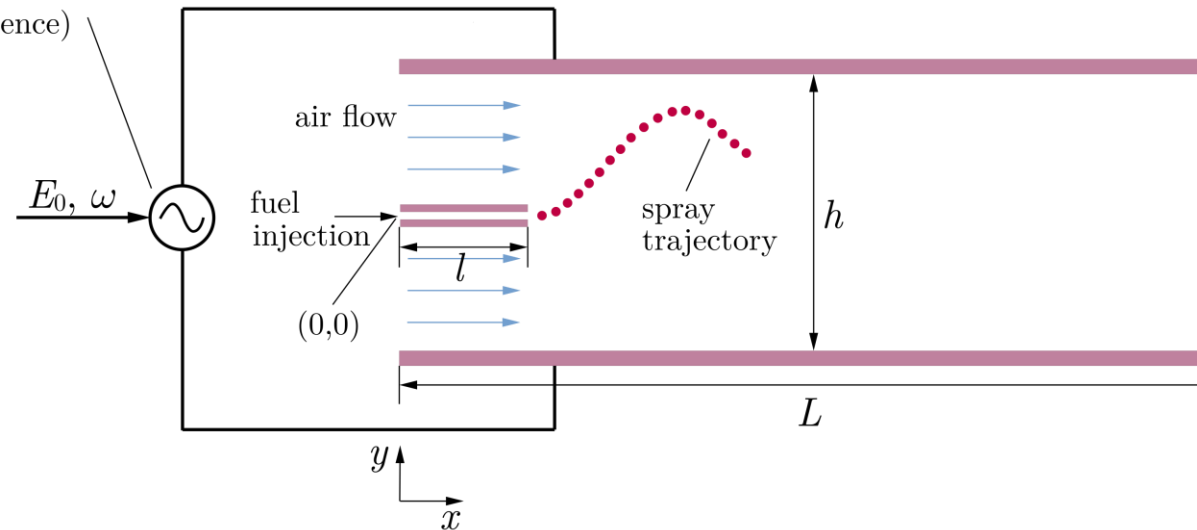
[Giusti & Fredrich, Fuel 366, 131009 (2024)]

# Simulation Framework

## Large Eddy Simulation

- Eulerian-Lagrangian framework for dilute sprays
- Channel Flow  $L = 0.3\text{m}$   $h = 0.1\text{m}$ , Grid:  $300 \times 50$
- Bulk velocity  $U_b = 1\text{-}3\text{ m/s}$ ,  $p_g = 1\text{atm}$ ,  $T_g = 600\text{K}$

oscillating electric field  
(potential difference)

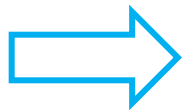
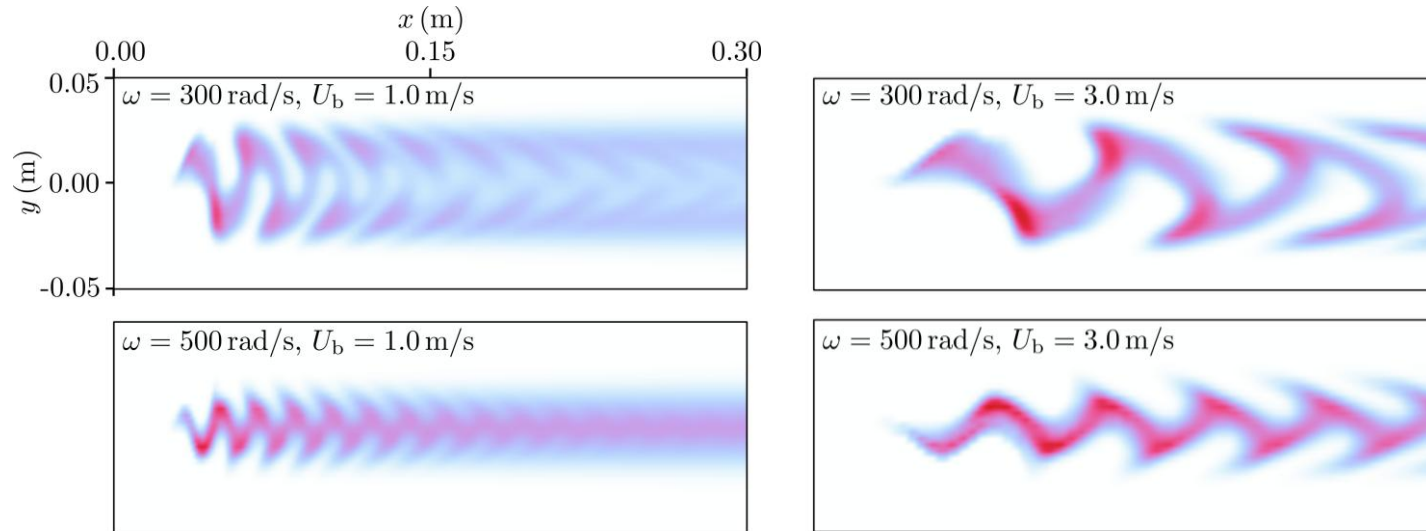


- Injection distance  $l = 0.025\text{m}$
- Fuel mass flow rate: JetA@ $0.0068\text{ g/s}$
- Droplet: droplet model from [1], Velocity  $1.5U_b$ ,  $d_0 = 50\mu\text{m}$ ,  $\rho_{q,d,0} = -1\text{ C/m}^3$

# Electric Field Effects on Fuel Vapour Profile

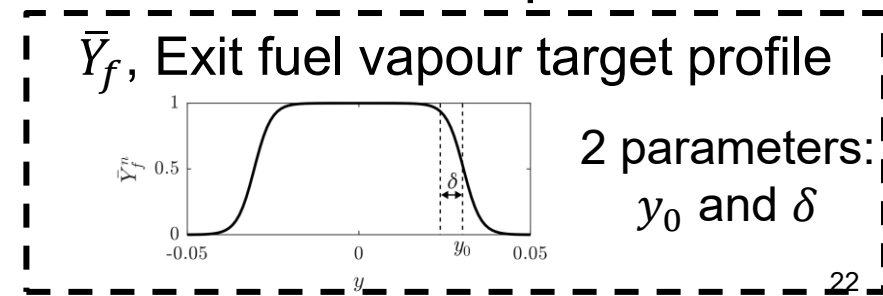
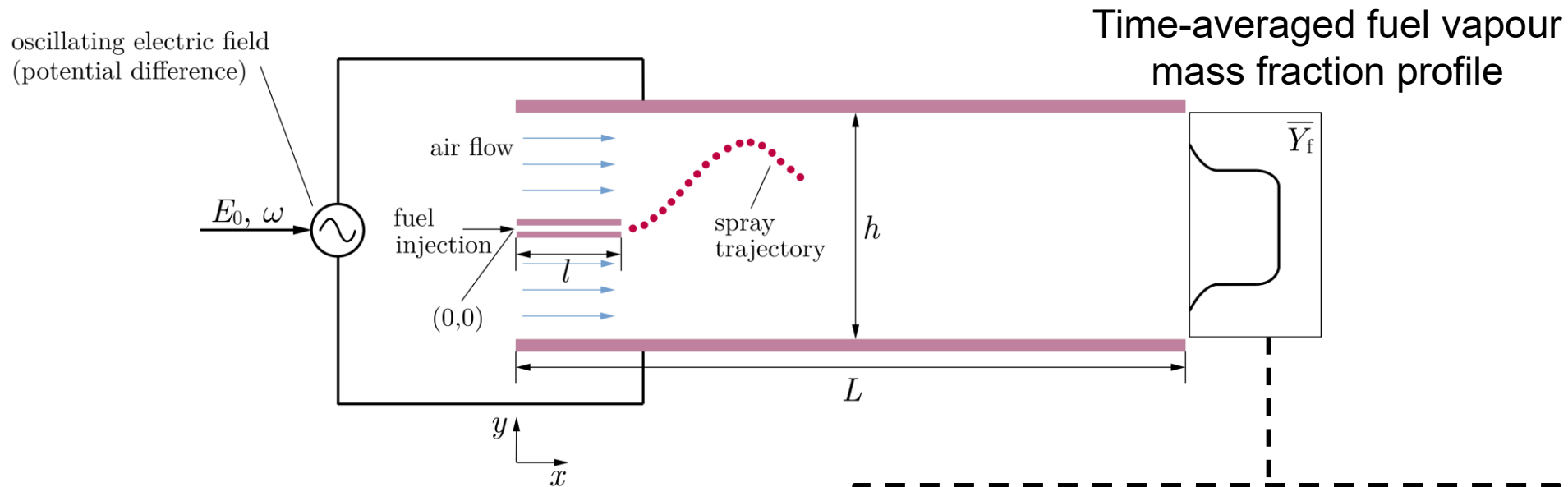
Instantaneous fuel mass fraction

$E_0 = 1 \text{ MV/m}$



- $U_b \uparrow$ : longer oscillation wavelength
- $\omega \uparrow$ : smaller oscillation wavelength and amplitude

# Control Framework

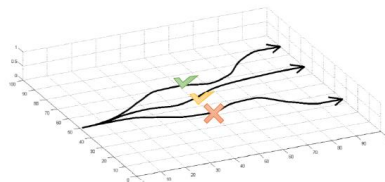
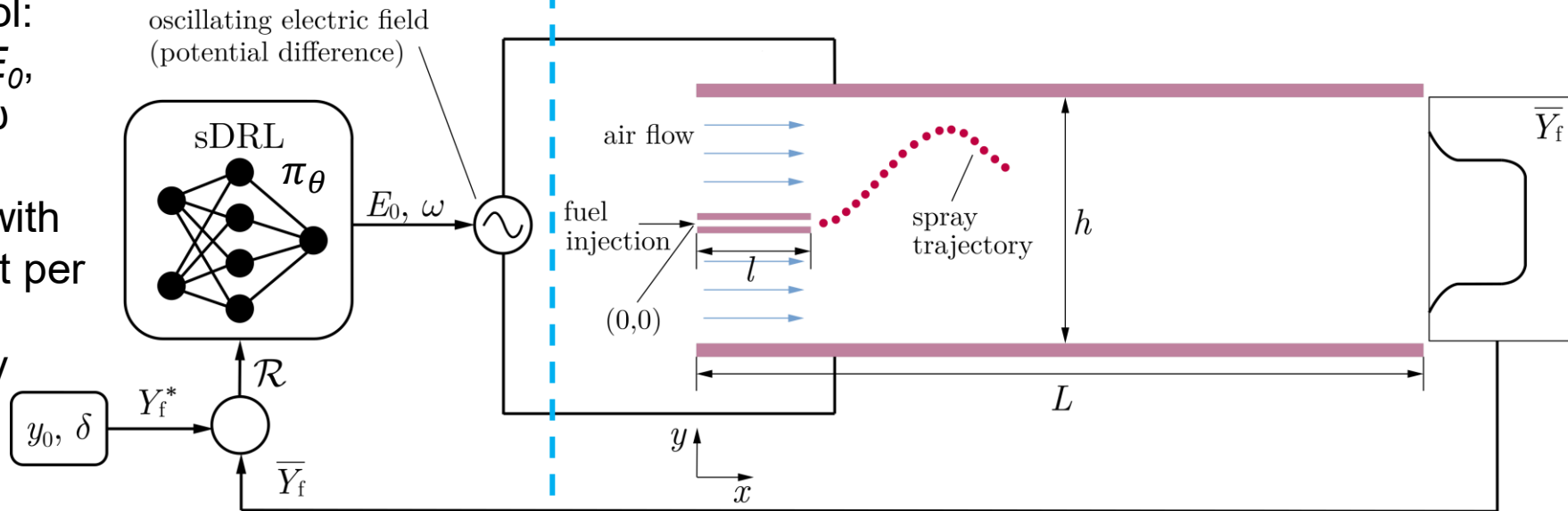


# Control Framework

## Single-step Deep Reinforcement Learning (sDRL)

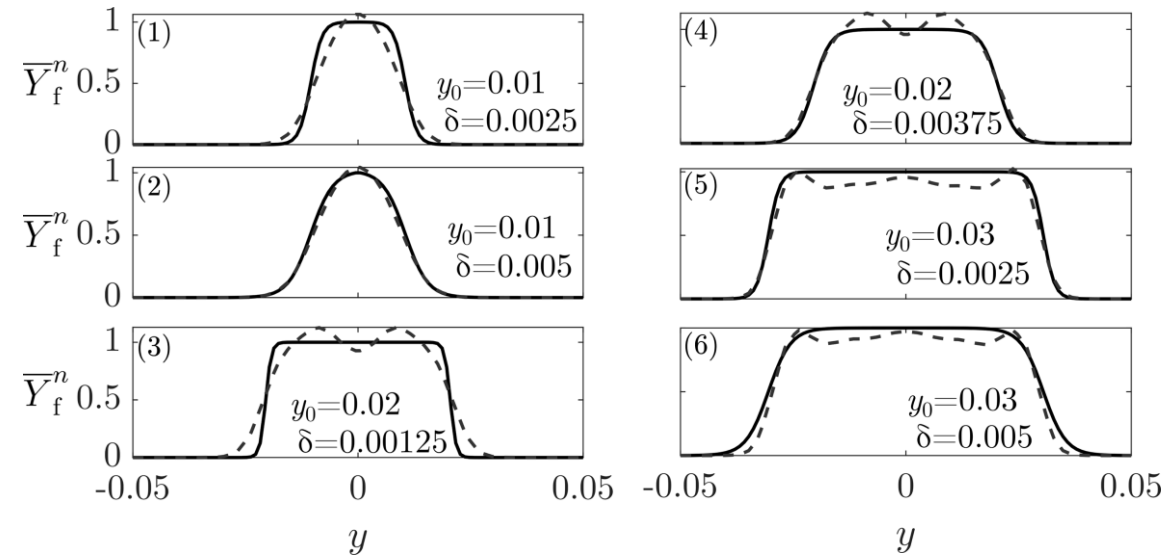
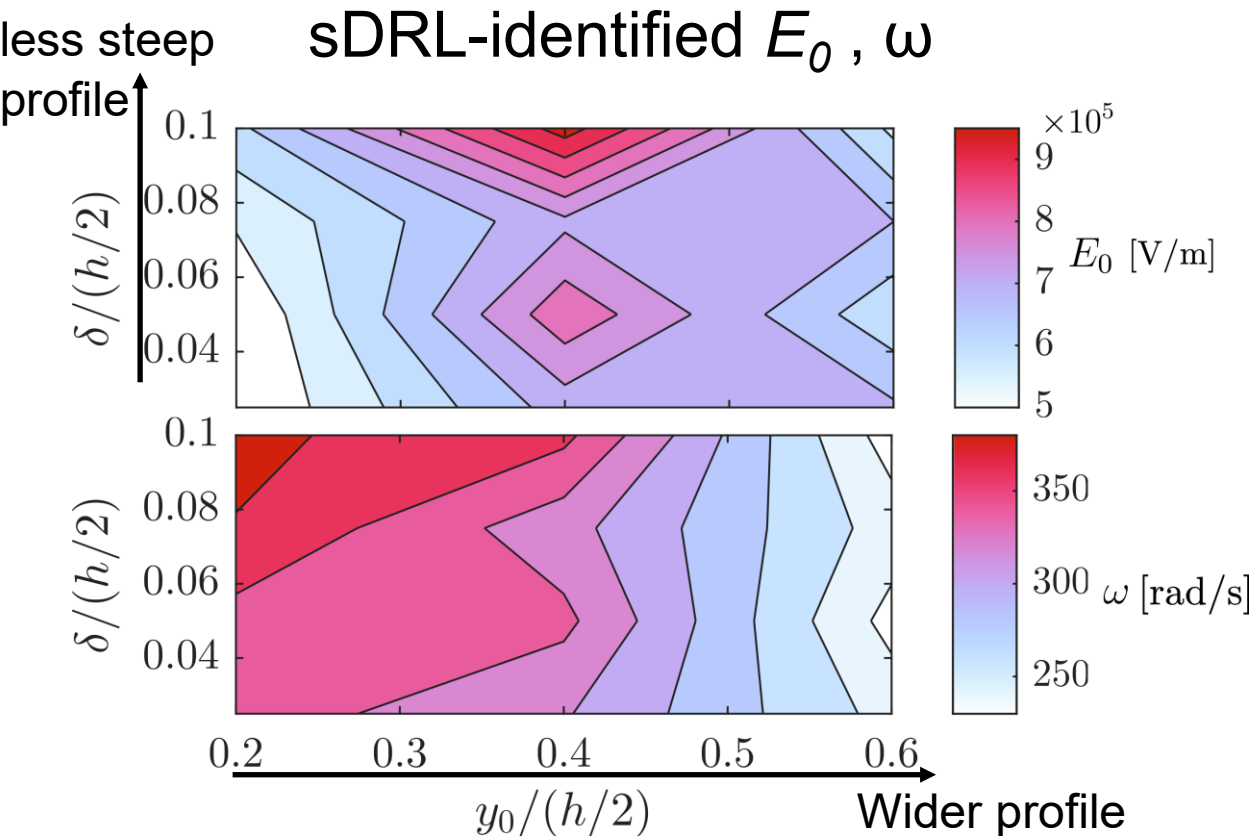
- sDRL control: Amplitude  $E_0$ , frequency  $\omega$
- One agent interaction with environment per episode
- Agent policy  $\pi_\theta$  trained through policy optimization

$$\nabla_\theta J(\theta) \approx \frac{1}{N} \sum_n \left[ \sum_{t=t_0}^T \nabla_\theta \log(\pi_\theta(a_{n,t} | s_{n,t})) R_n(\tau) \right]$$



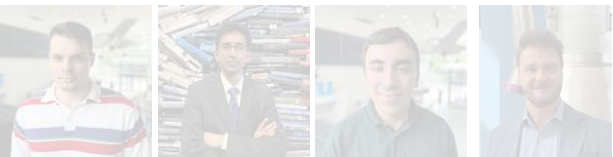
sDRL used to identify optimal  $E_0, \omega$  for given  $y_0, \delta$

# sDRL-identified optimal electric field parameters

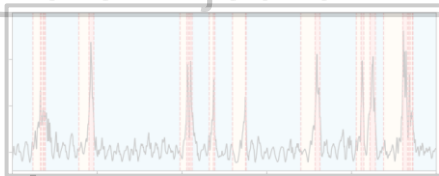


Also extended to 3D configuration

# Structure of the seminar



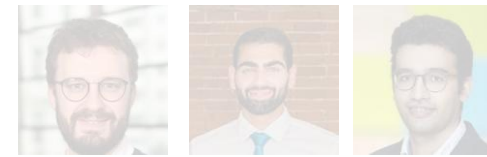
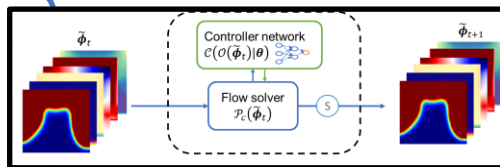
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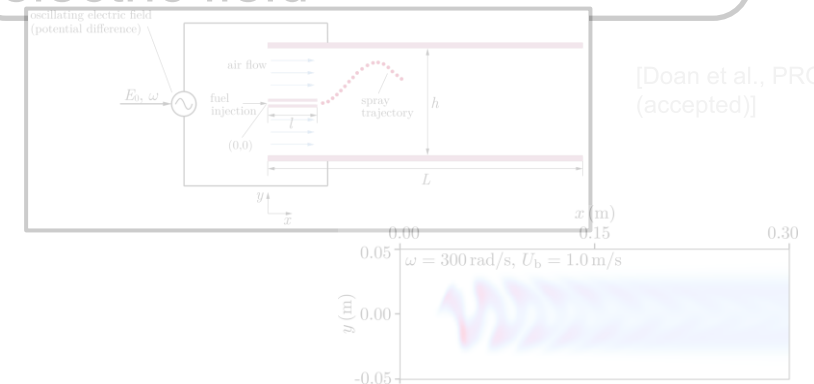
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## 3. Towards unified control development framework with differentiable solver



## 2. Machine Learning to control fuel mixing with electric field

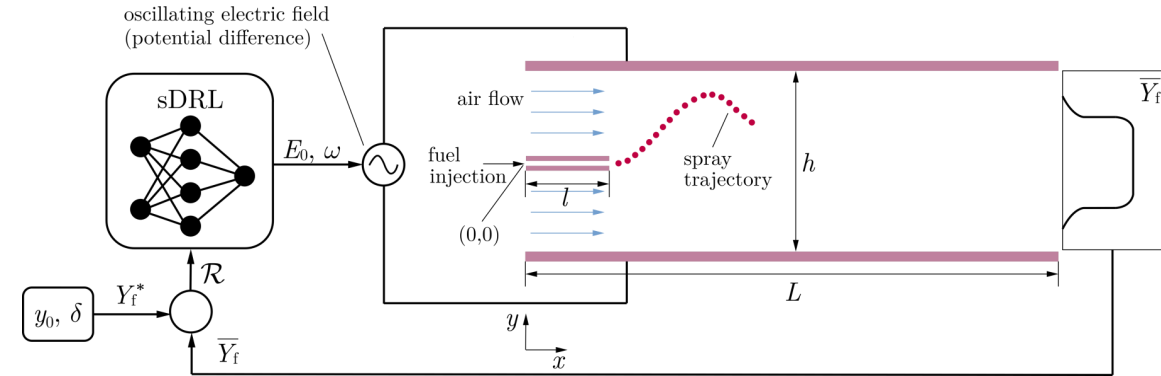
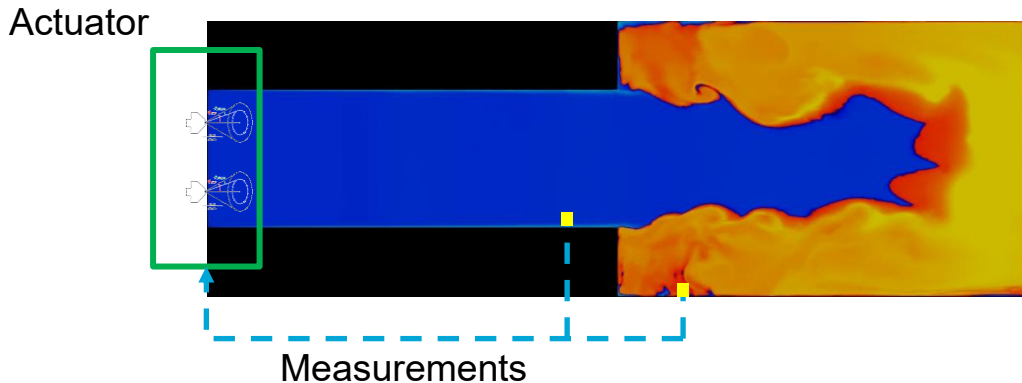


[Doan et al., PROCI, 2026 (accepted)]



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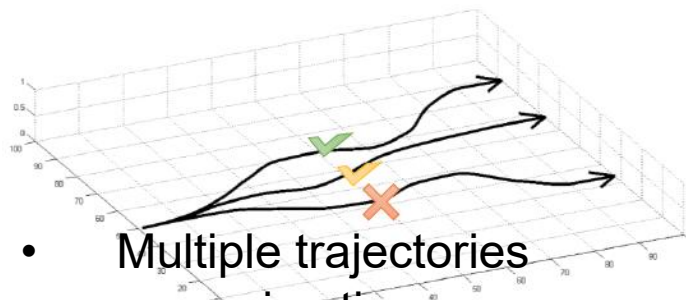
# Flame control poses large challenges for DRL



(Long) time-delay between actuator input and effect on flow  
 → Challenging for many control algorithms, including reinforcement learning

Approximated policy gradient for DRL:

$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_n \left[ \sum_{t=t_0}^T \nabla_{\theta} \log(\pi_{\theta}(a_{n,t} | s_{n,t})) R_n(\tau) \right]$$

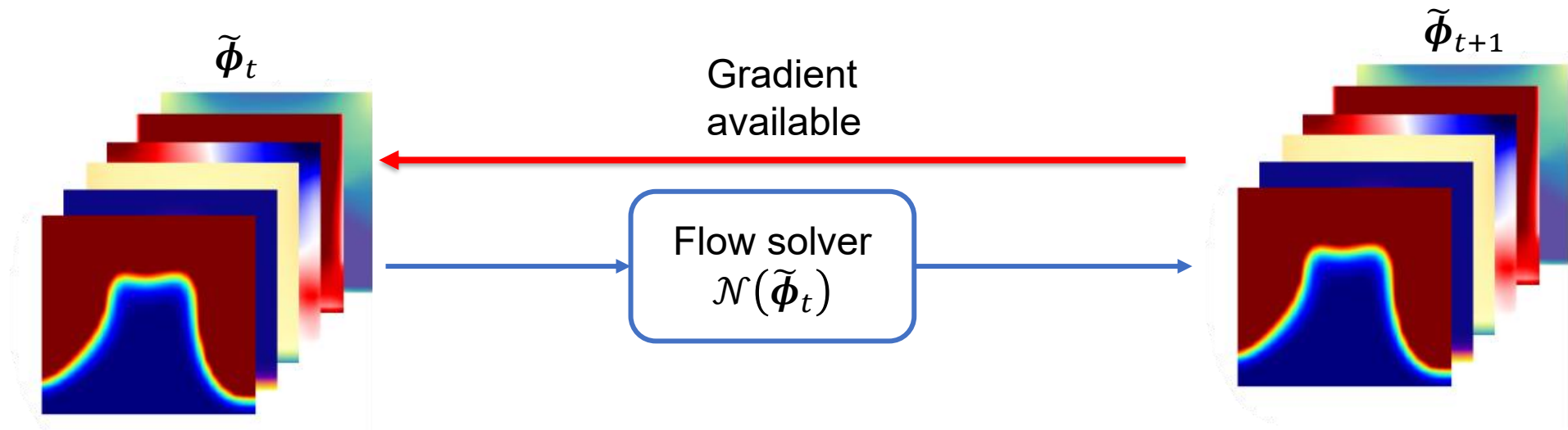


- Multiple trajectories approximation
- Mini-batch approximation

Extremely data-intensive

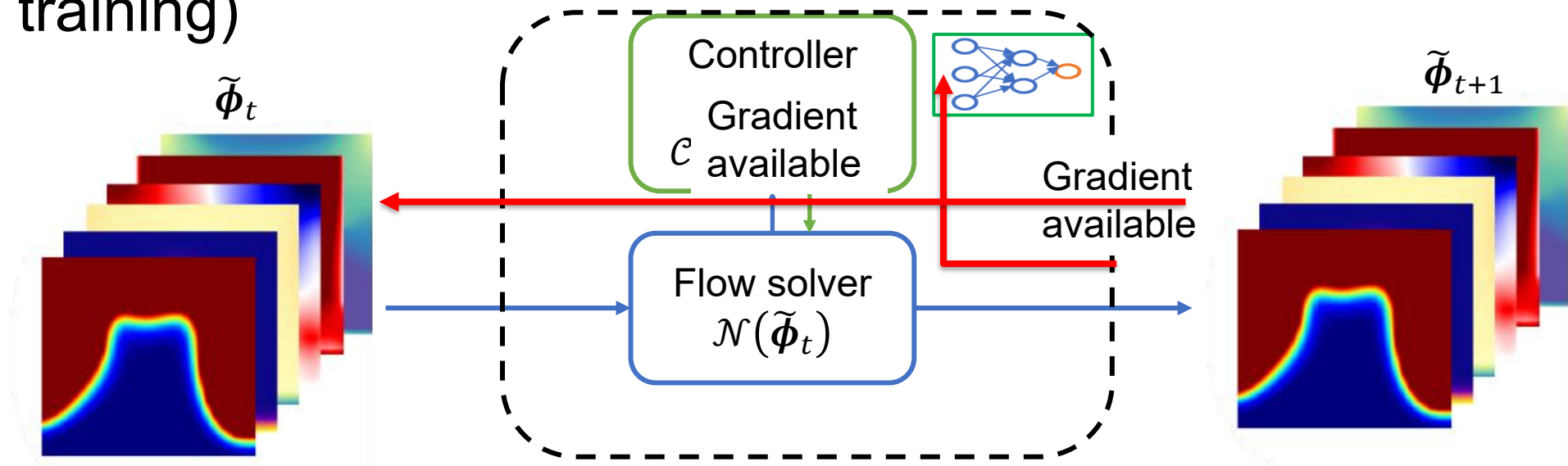
# Differentiable solver propagates gradient through its operations

- Recently, differentiable flow solver appeared
  - Jaxcfd, jaxfluids, phiflow, PICT, ...
  - Maintain automatic differentiation capabilities through solver operation
- Effectively, similar to algorithmic adjoint



# Differentiable solver provides seamless gradients for neural network training

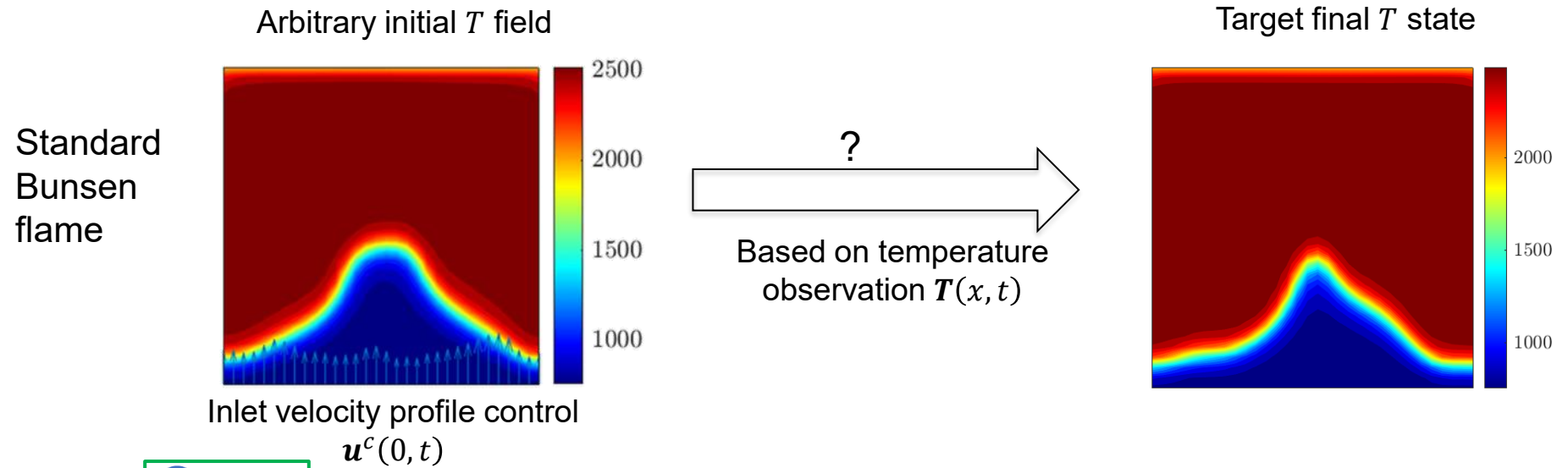
- Recently, differentiable flow solver appeared
  - Jaxcfd, jaxfluids, phiflow, ...
  - Maintain automatic differentiation capabilities through solver operation
- Effectively, similar to algorithmic adjoint
- Allows for seamless embedding of neural network (and their training)



# Differentiable solver leveraged for two flow control problems

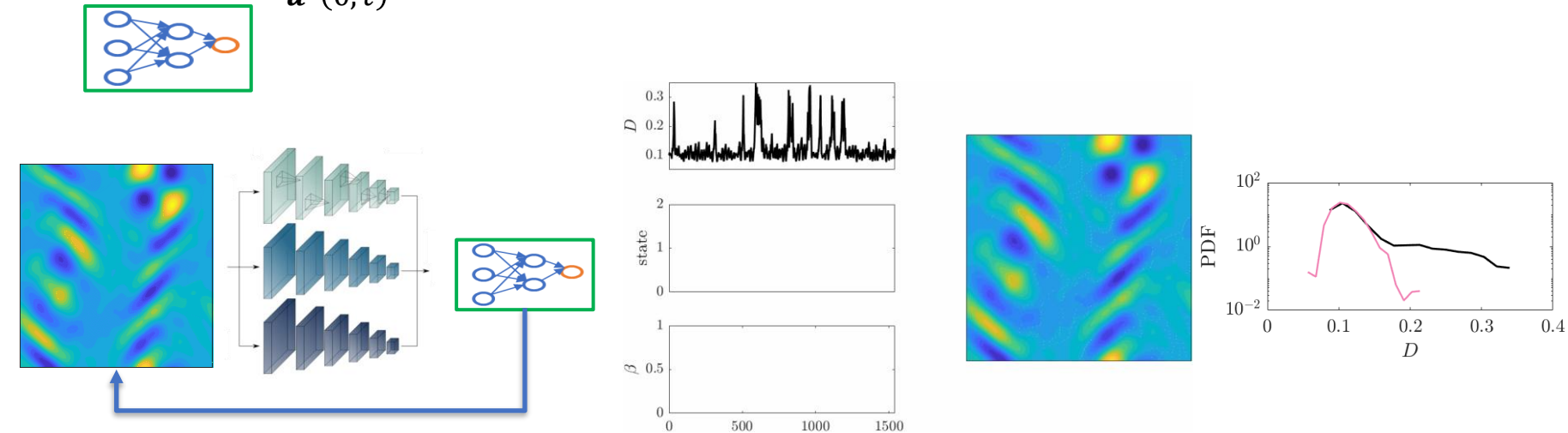
## Test case: flame shape control

[Tathawadekar et al., DCE, (2023)]



## Test case: Extreme events control in Kolmogorov flow

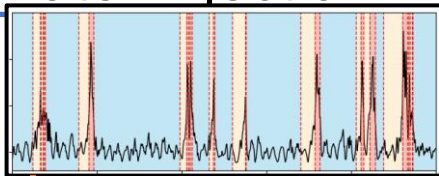
[Shehata & Doan., PRFluids, (under review)]



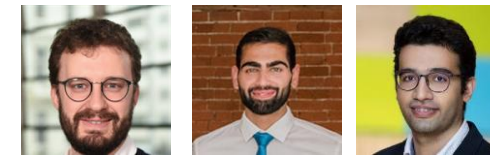
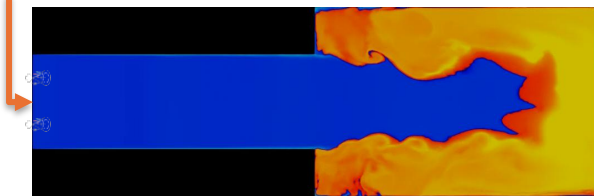
# Structure of the seminar



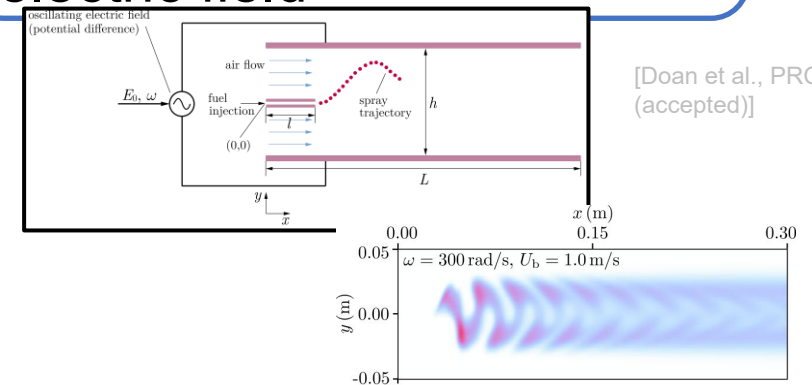
## 1. Machine Learning to prevent flashback with water injection



[Floris et al., Proc. Comb. Inst., 2024]  
 [Pousouda et al., J. Eng. Gas Turbines Power, 2025]

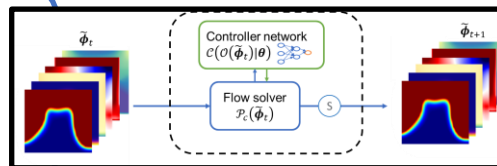


## 2. Machine Learning to control fuel mixing with electric field



[Doan et al., PROCI, 2026 (accepted)]

## 3. Towards unified control development framework with differentiable solver



[Tathawadekar et al., Data-centric Eng., 2023]  
 [Shehata & Doan, PRFluids, 2026 (under review)]

# Summary & Perspectives

- Machine learning: promising new approaches to exploit “actuators” for flame control
- Flashback prevention
  - Informed by precursors obtained with dimensionality reduction: CoK-PCA and modularity-based clustering
  - GP-based design of optimal water injection
- Fuel stratification control
  - Reinforcement Learning-control of electric field
- First step towards unified control framework development with differentiable solver

# Summary & Perspectives

- Still many challenges
  - Integration of precursor/control techniques into unified framework
  - Applicability to realistic configurations
  - Robustness of identified control approach?

# Thank you for your attention!

## Questions?

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Interested in this research?  
Postdoc position available soon

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